

Cuprate high- T_c superconductivity: Insights from a model system

李源

北京大学量子材料科学中心



Outline

□ Introduction

- HTSC and the cuprates
- Spectroscopic methods applied to the high- T_c problem

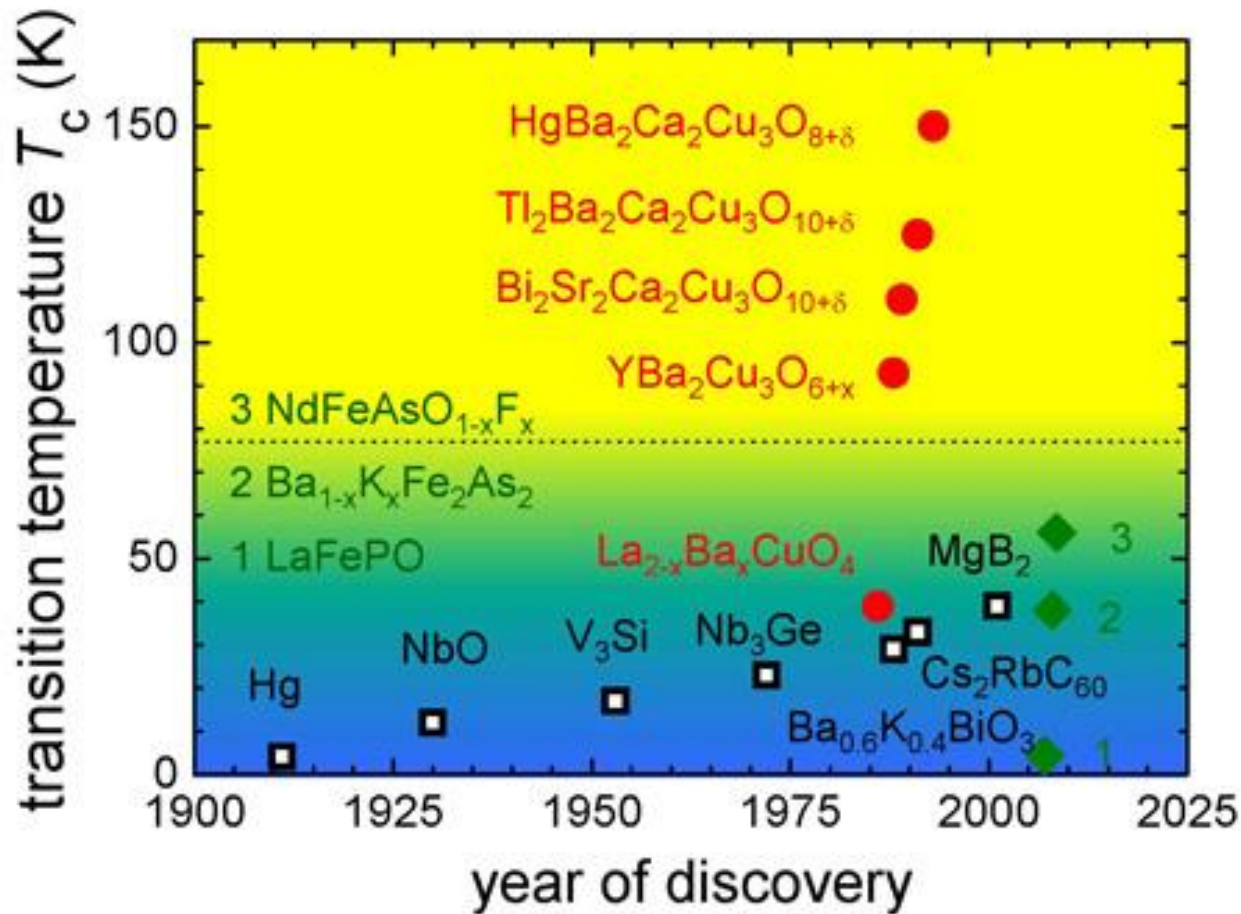
□ Model system $\text{HgBa}_2\text{CuO}_{4+\delta}$

□ Topics:

1. The neutron resonant mode
2. Pseudogap magnetism
3. Energy $2\Delta_{\text{sc}}$ and above

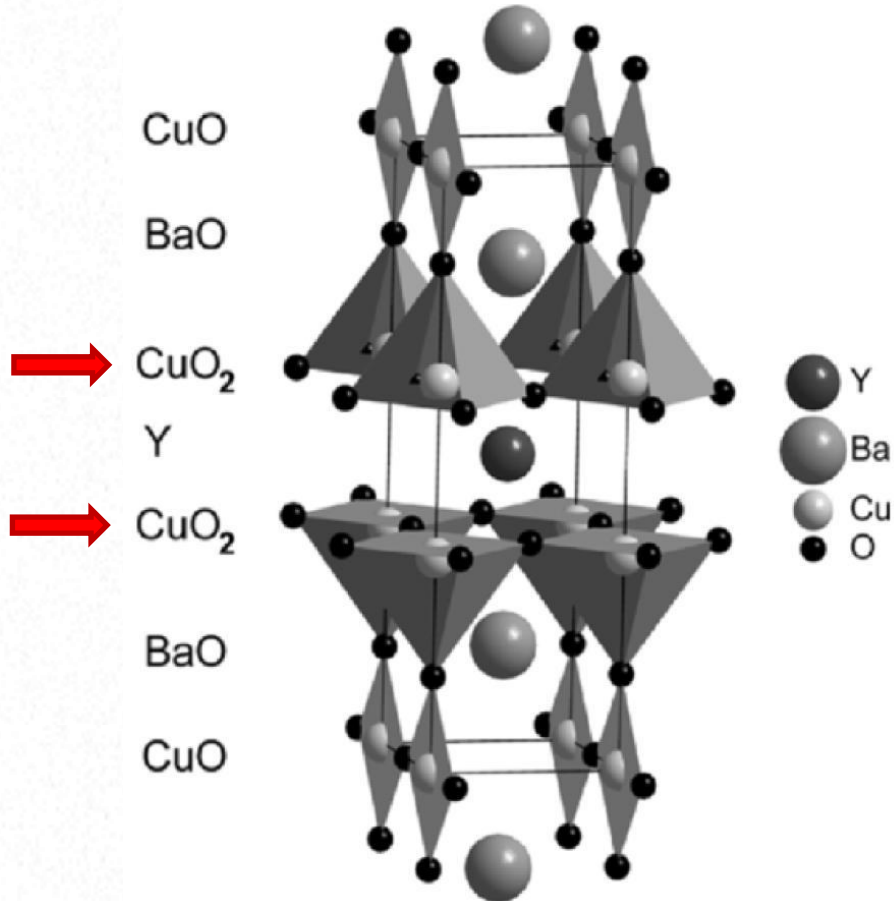
□ Summary

T_c over the years

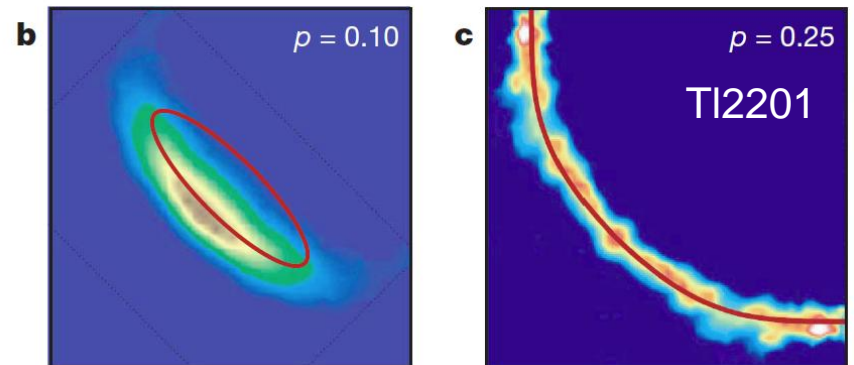
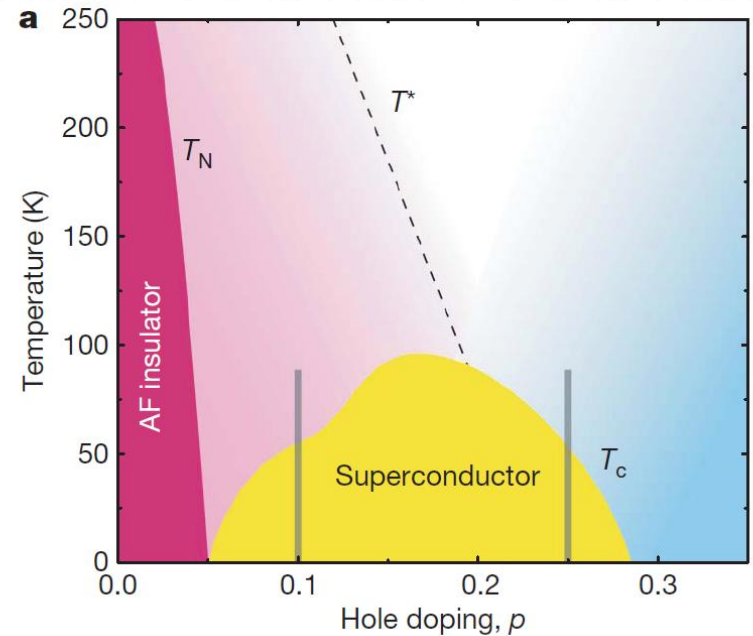


courtesy of Rudi Hackl

Cuprates: crystal and electronic structure

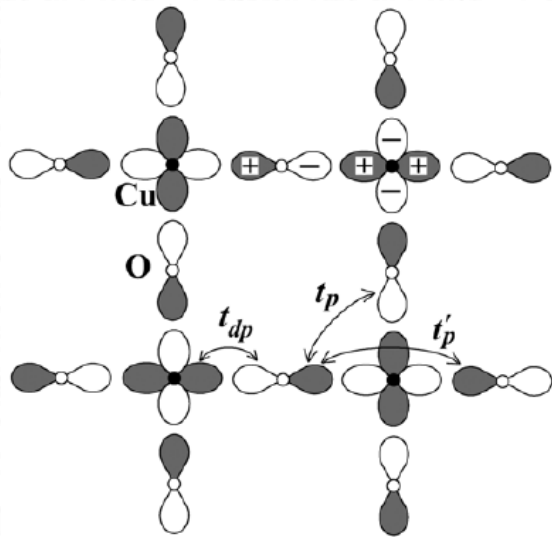


Fisher et al., in *Handbook of high-temperature superconductivity*, Springer (2007)



Doiron-Leyraud et al., *Nature* **447**, 565 (2007)

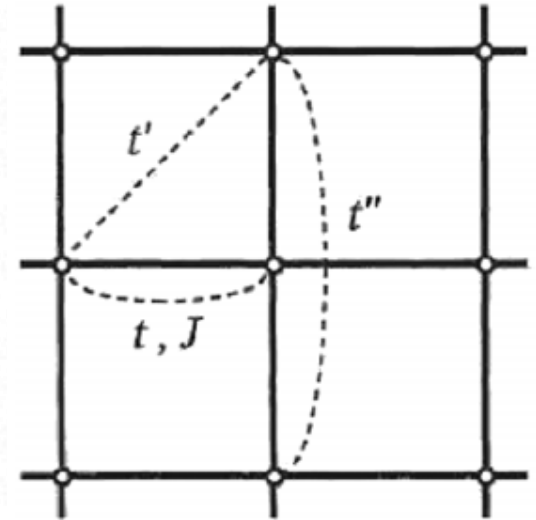
Cuprates: crystal and electronic structure



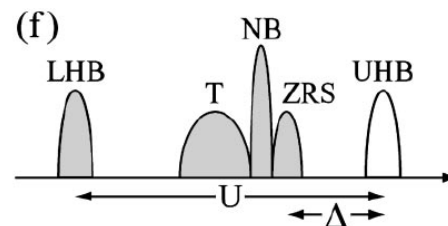
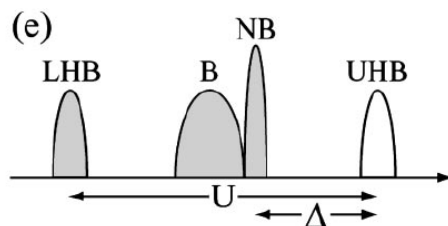
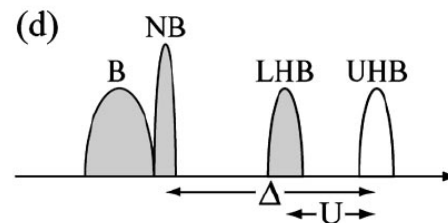
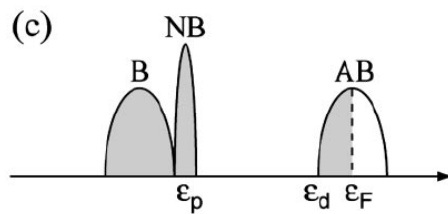
three-band model

$$t_{dp} \ll U, t_{dp} \ll \Delta_{dp}$$

$$t_p, t'_p \text{ negligible}$$



t - J model



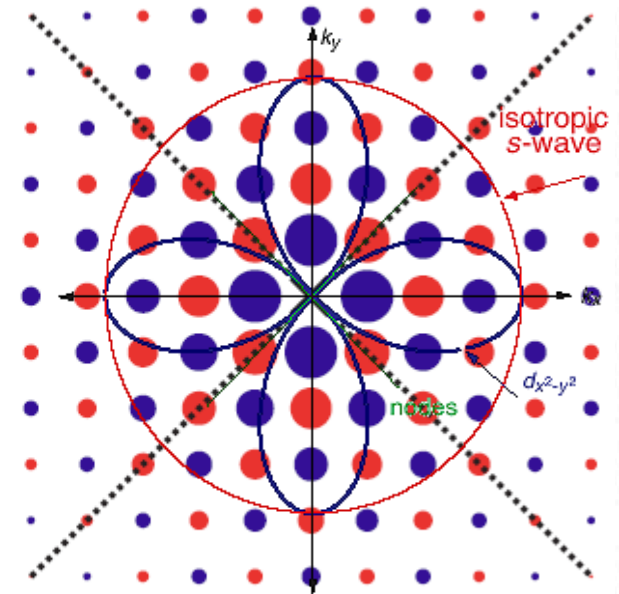
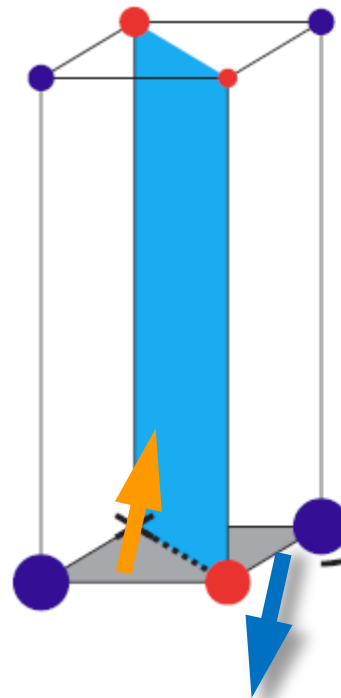
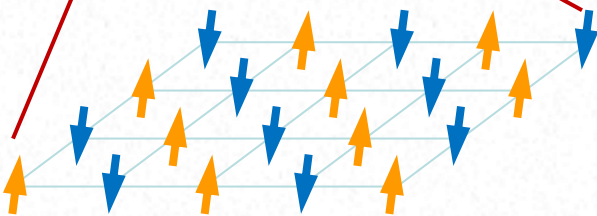
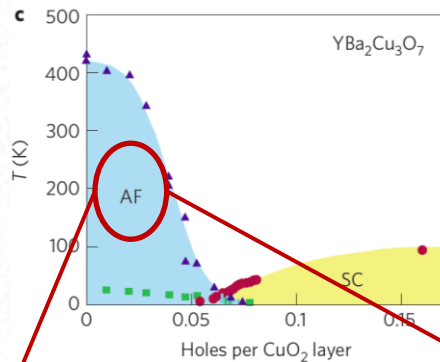
d -wave pairing near a spin-density-wave instability

D. J. Scalapino, E. Loh, Jr.,* and J. E. Hirsch†

Institute for Theoretical Physics, University of California, Santa Barbara, California 93106

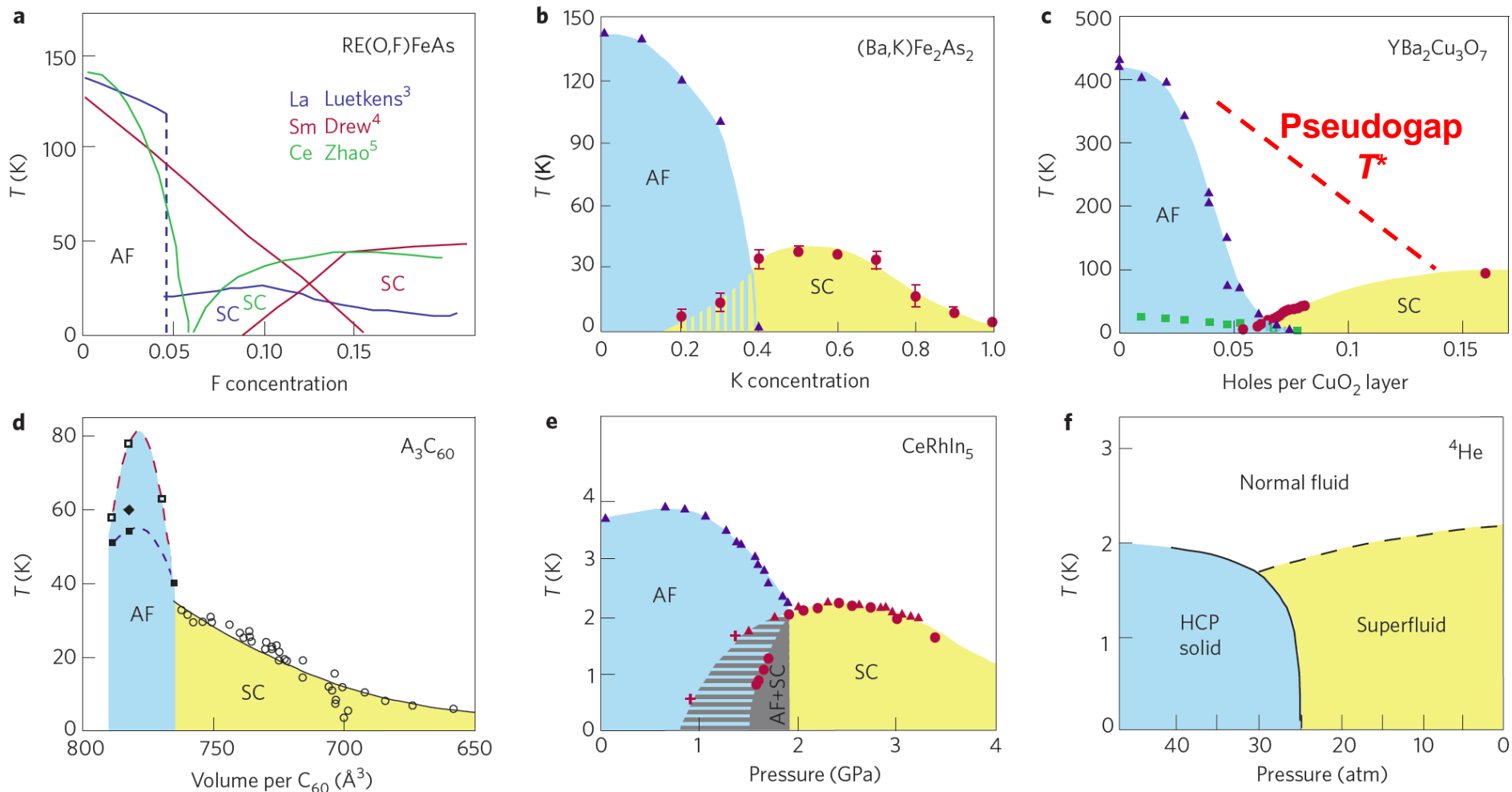
(Received 23 June 1986)

We investigate the three-dimensional Hubbard model and show that paramagnon exchange near a spin-density-wave instability gives rise to a strong singlet d -wave pairing interaction. For a cubic band the singlet ($d_{x^2-y^2}$ and $d_{3z^2-r^2}$) channels are enhanced while the singlet (d_{xy}, d_{xz}, d_{yz}) and triplet p -wave channels are suppressed. A unique feature of this pairing mechanism is its sensitivity to band structure and band filling.



● Repulsion ● Attraction

Unconventional SC near AF instability



Uemura, *Nature Materials* **8**, 253 (2009)

Some important questions

- ❑ Q: What's the pairing symmetry?
- ❑ Q: What causes the pseudogap above T_c ?
- ❑ Q: Is there a competing order other than AFM?
- ❑ Q: Which bosonic modes are important?
- ❑ Q: What's the minimal microscopic model?

Outline

□ Introduction

- HTSC and the cuprates
- Spectroscopic methods applied to the high- T_c problem

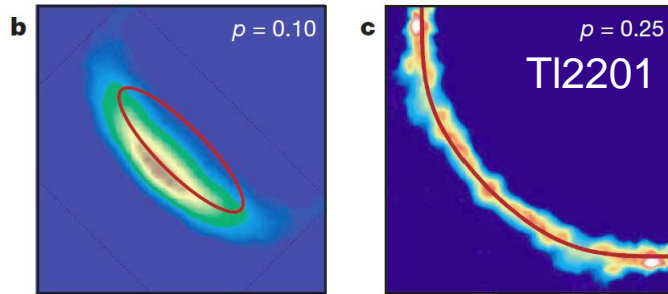
□ Model system $\text{HgBa}_2\text{CuO}_{4+\delta}$

□ Topics:

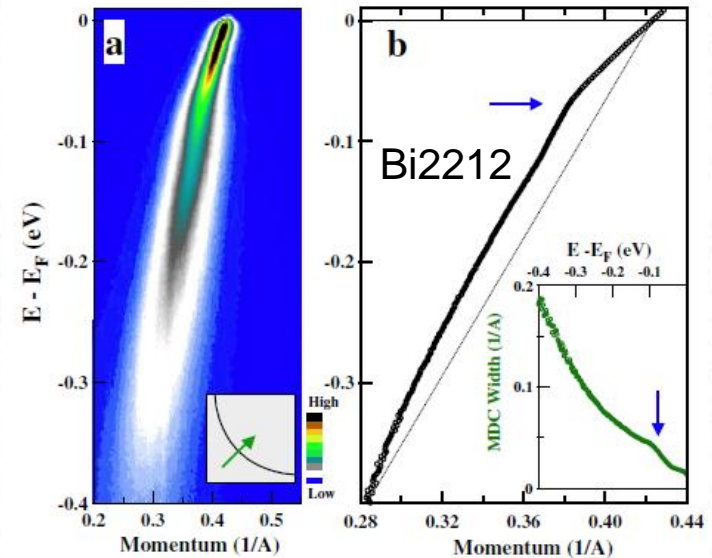
1. The neutron resonant mode
2. Pseudogap magnetism
3. Energy $2\Delta_{\text{sc}}$ and above

□ Summary

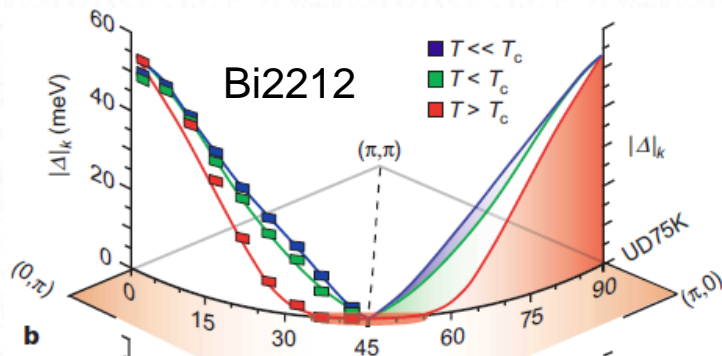
ARPES



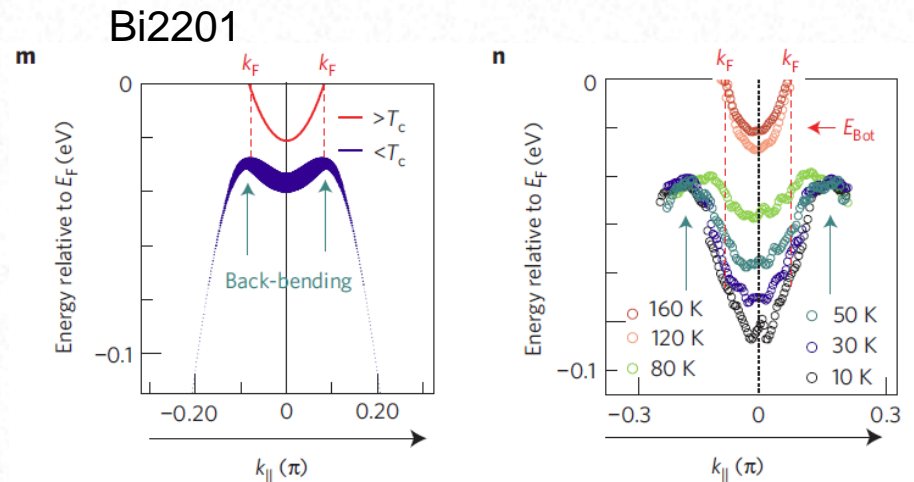
Doiron-Leyraud *et al.*, *Nature* **447**, 565 (2007)



Zhang *et al.*, *PRL* **100**, 107002 (2008)

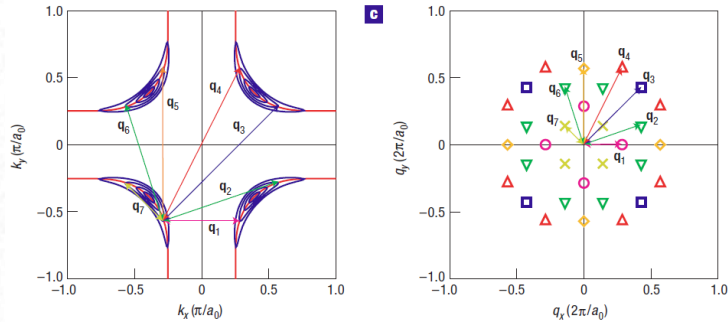


Lee *et al.*, *Nature* **450**, 81 (2007)



Hashimoto *et al.*, *Nat. Phys.* **6**, 414 (2010)

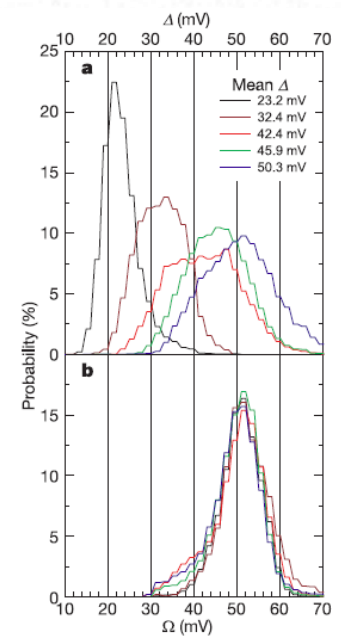
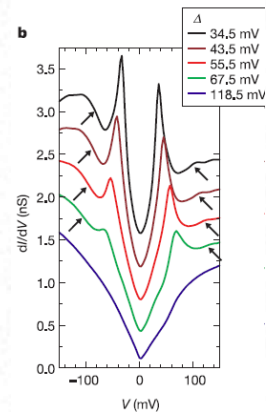
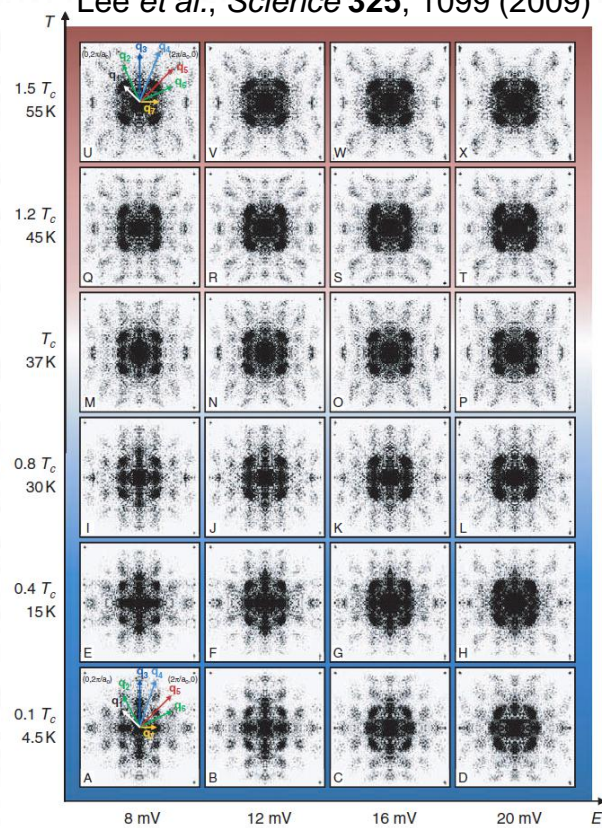
STM/STS



Doiron-Leyraud *et al.*, *Nature* **447**, 565 (2007)

Lee *et al.*, *Science* **325**, 1099 (2009)

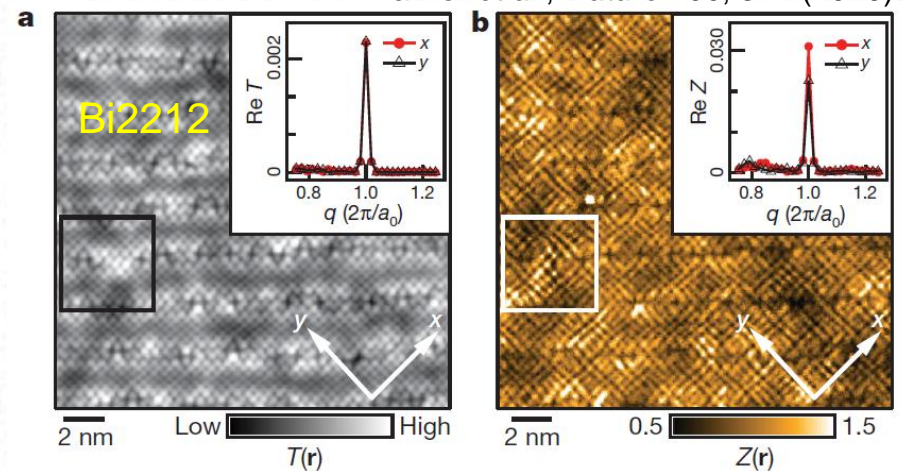
Bi2212



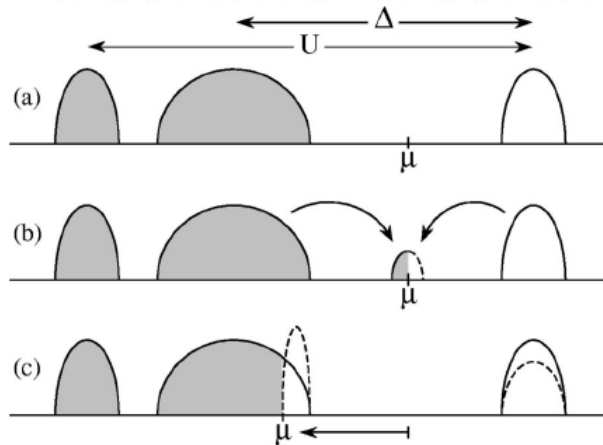
Bi2212

Lee *et al.*, *Nature* **442**, 546 (2006)

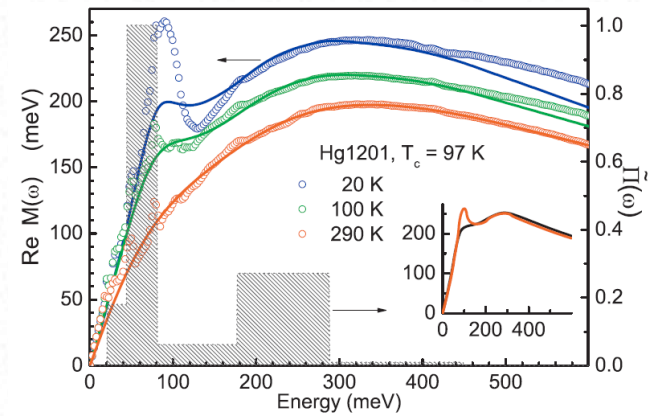
Lawler *et al.*, *Nature* **466**, 347 (2010)



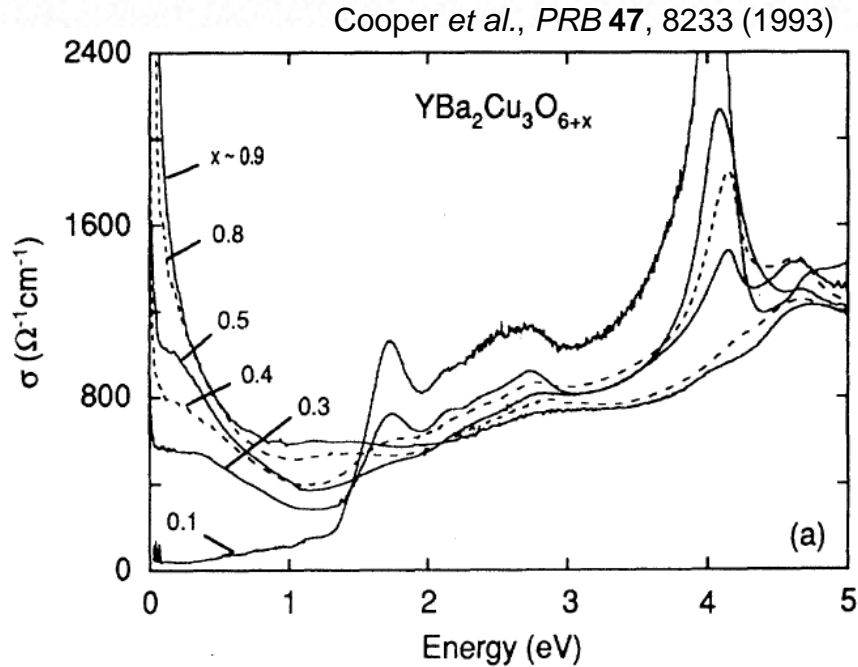
Optical conductivity



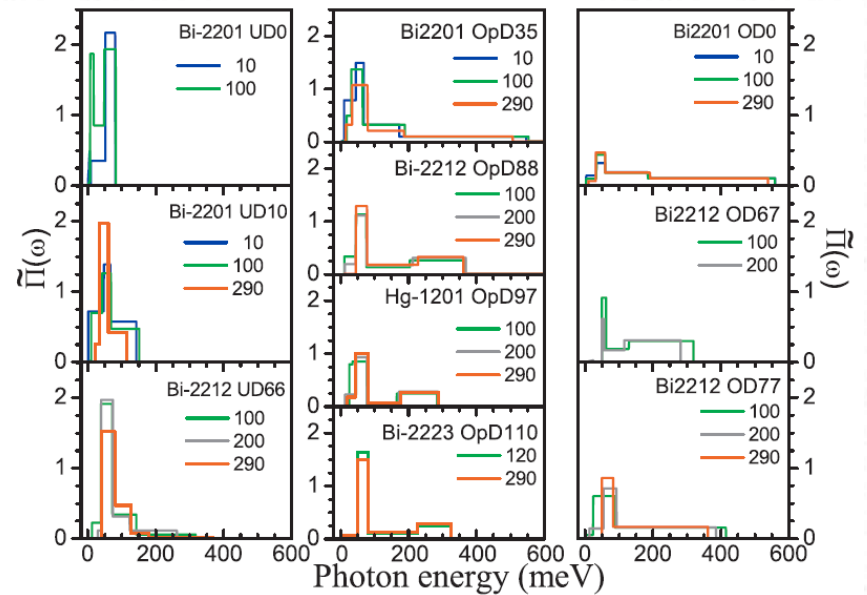
Damascelli, Hussain and Shen, *RMP* **75**, 473 (2003)



$$4\pi\sigma(\omega) = \frac{i\omega_p^2}{\omega + \hat{M}(\omega)}$$

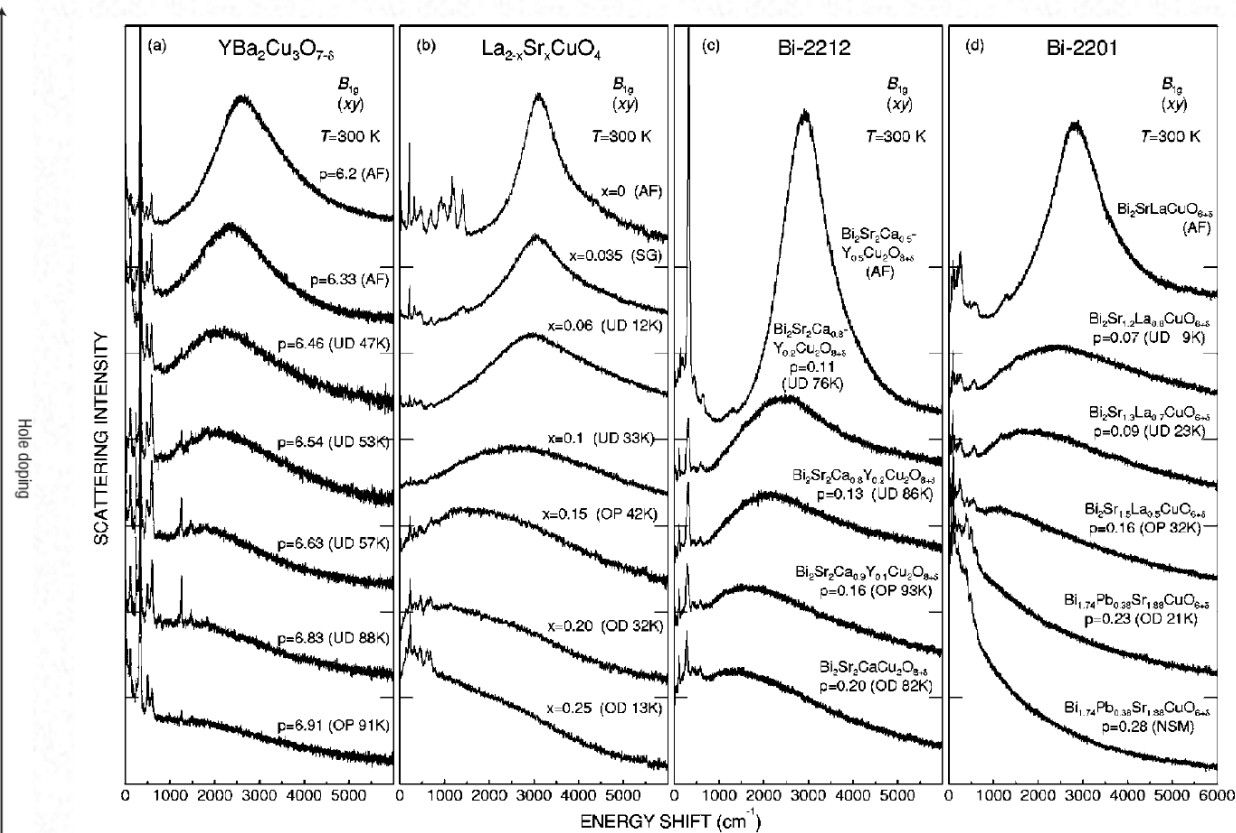
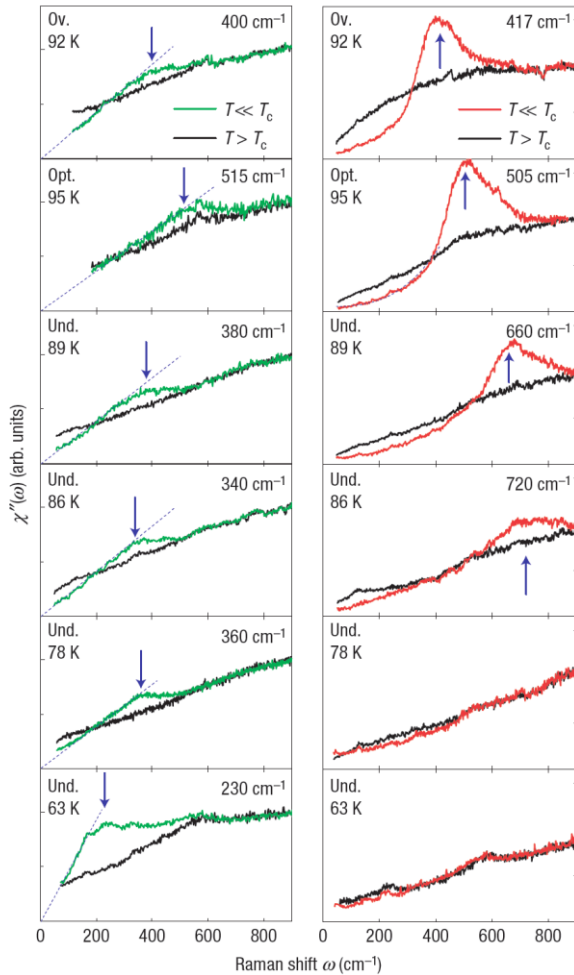
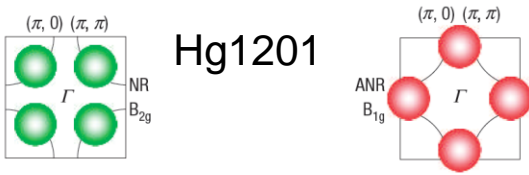


Cooper *et al.*, *PRB* **47**, 8233 (1993)



van Heumen *et al.*, *PRB* **79**, 184512 (2009)

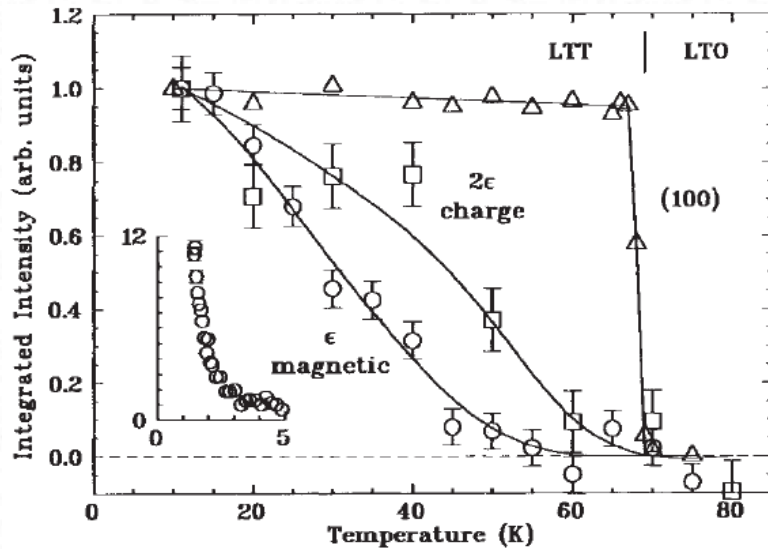
Raman scattering



Sugai et al., PRB 68, 184504 (2003)

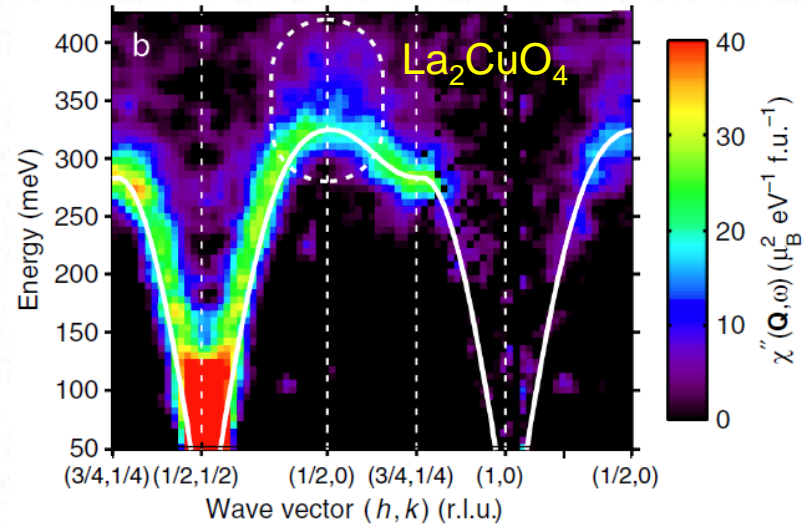
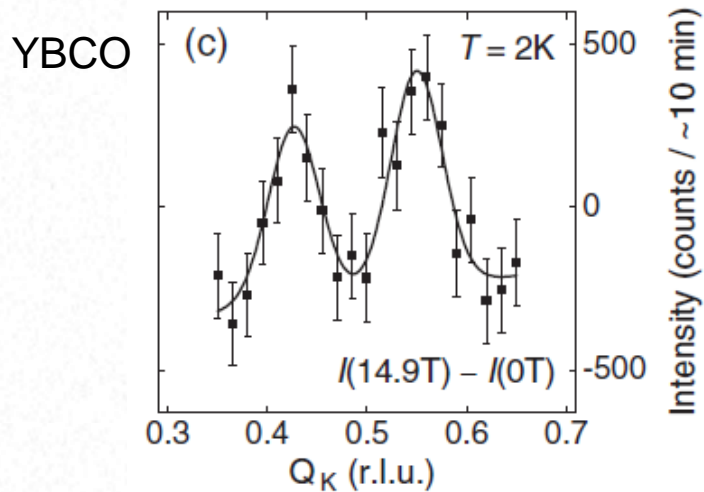
Le Tacon et al., Nat. Phys. 2, 537 (2006)

Neutron scattering



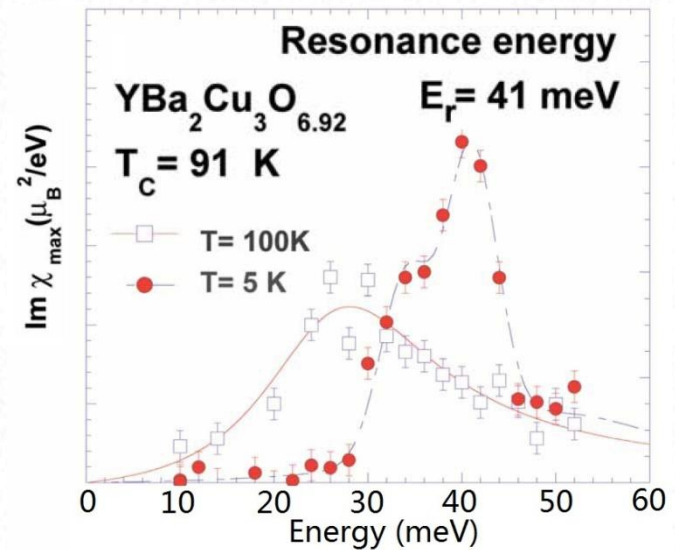
Nd-LSCO Tranquada *et al.*, *Nature* **375**, 561 (1995)

Haug *et al.*, *PRL* **103**, 017001 (2009)

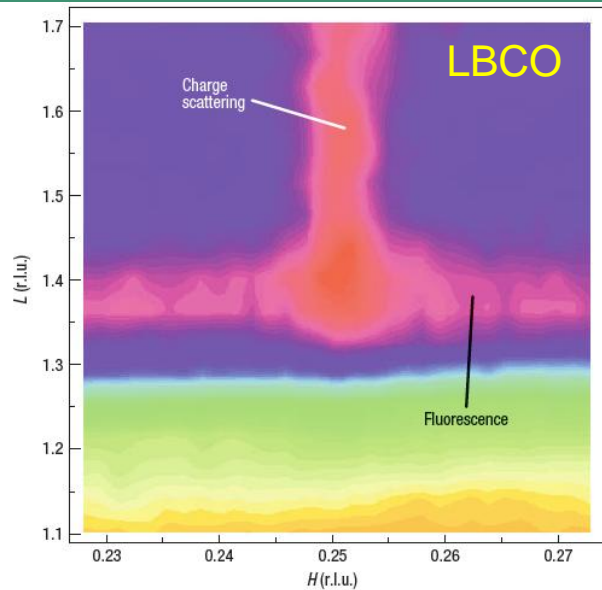


Headings *et al.*, *PRL* **105**, 247001 (2010)

Eschrig *et al.*, *Adv. Phys.* **55**, 47 (2006)

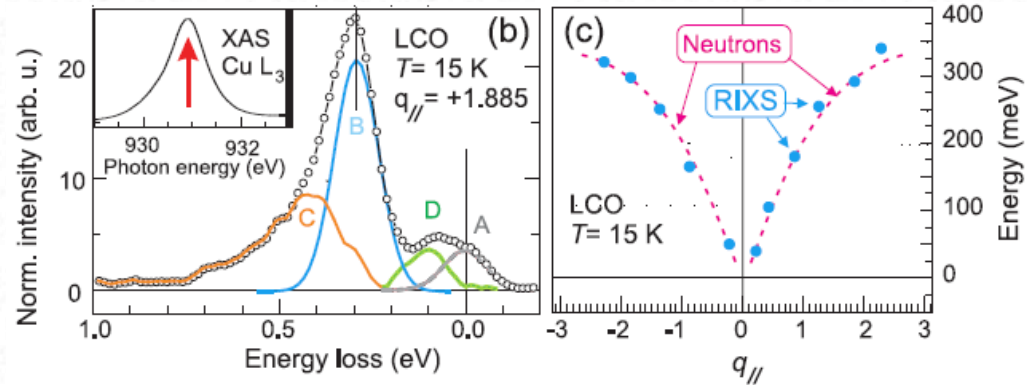


(Resonant) X-ray scattering

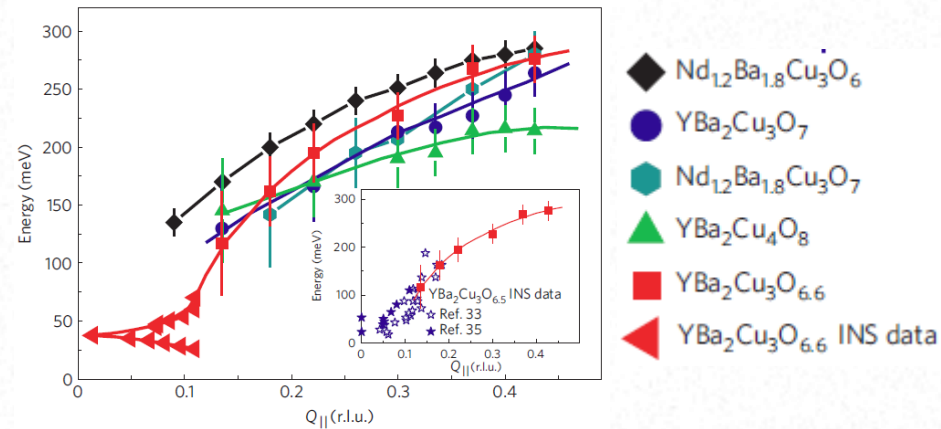
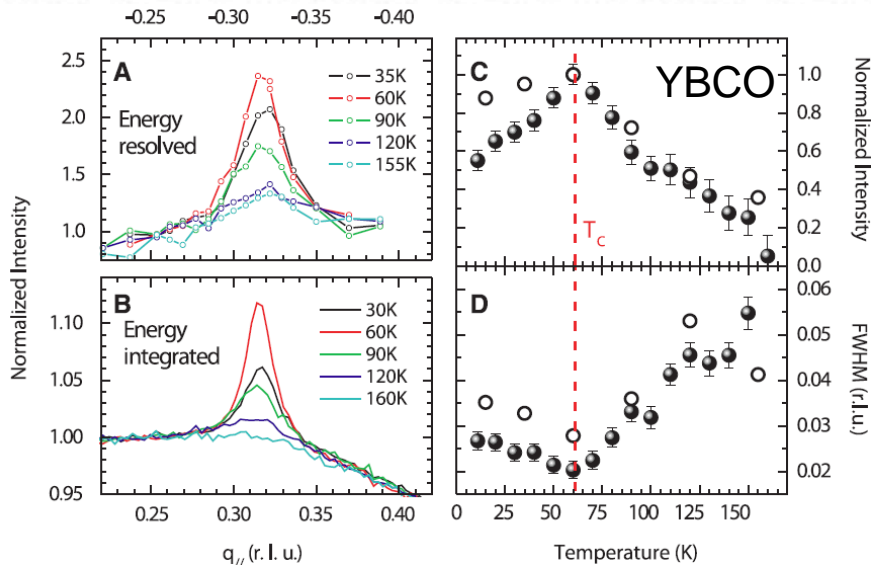


Abbamonte *et al.*, *Nat. Phys.* **1**, 155 (2005)

Ghiringhelli *et al.*, *Science* **337**, 821 (2012)



Braicovich *et al.*, *PRL* **104**, 077002 (2010)



Le Tacon *et al.*, *Nat. Phys.* **7**, 725 (2011)

Some important questions

❑ Q: What's the pairing symmetry?

A: *d*-wave.

❑ Q: What causes the pseudogap above T_c ?

A: There is evidence for both pre-formed pairs and competing order.

❑ Q: Is there a competing order other than AFM?

A: CDW, SDW, intra-unit-cell order are all possible.

❑ Q: Which bosonic modes are important?

A: Both magnetic excitations and phonons are prominent.

(Which one is the "pairing glue" is a separate question!)

❑ Q: What's the minimal microscopic model?

A: Single-band models are accepted as there is no strong violation.

Outline

□ Introduction

- HTSC and the cuprates
- Spectroscopic methods applied to the high- T_c problem

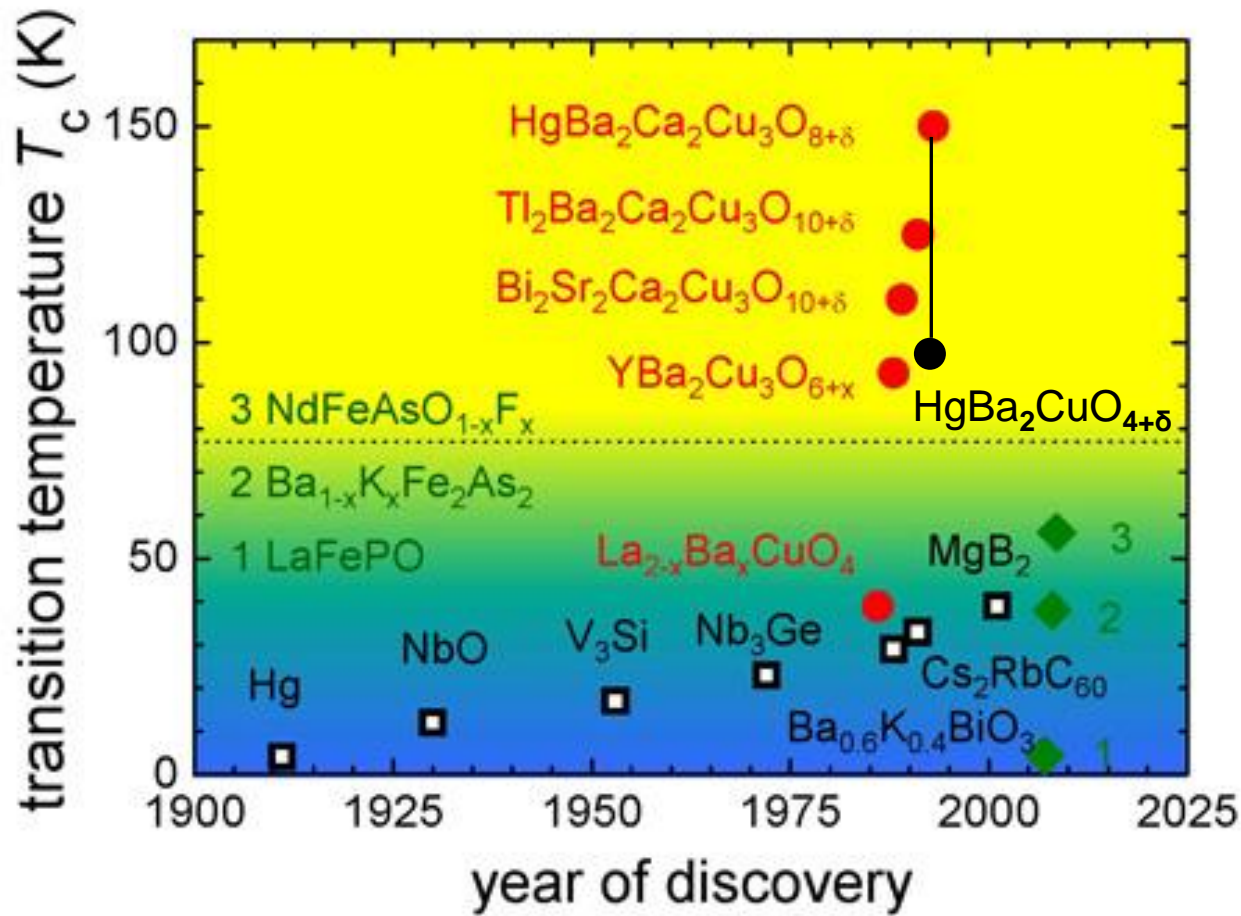
□ Model system $\text{HgBa}_2\text{CuO}_{4+\delta}$

□ Topics:

1. The neutron resonant mode
2. Pseudogap magnetism
3. Energy $2\Delta_{\text{sc}}$ and above

□ Summary

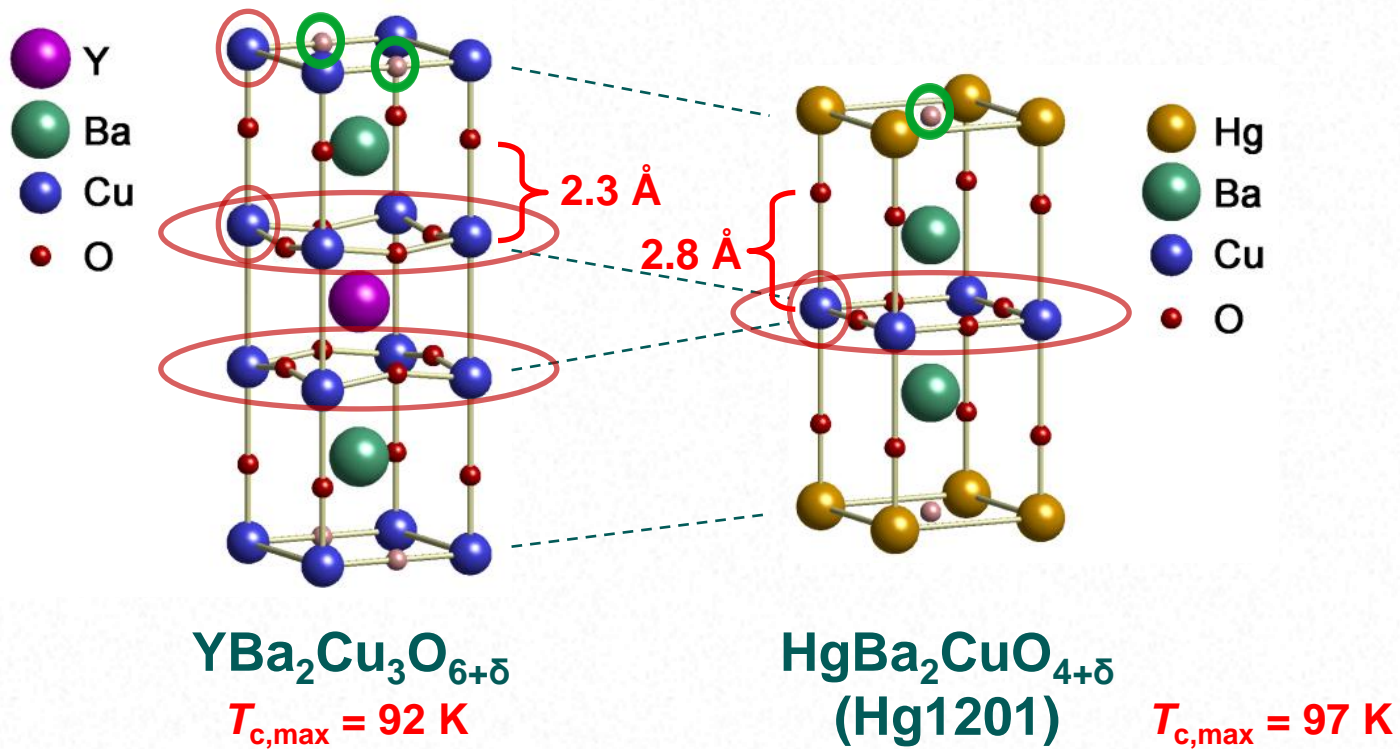
T_c over the years



Putilin *et al.*, *Nature*
362, 226 (1993)

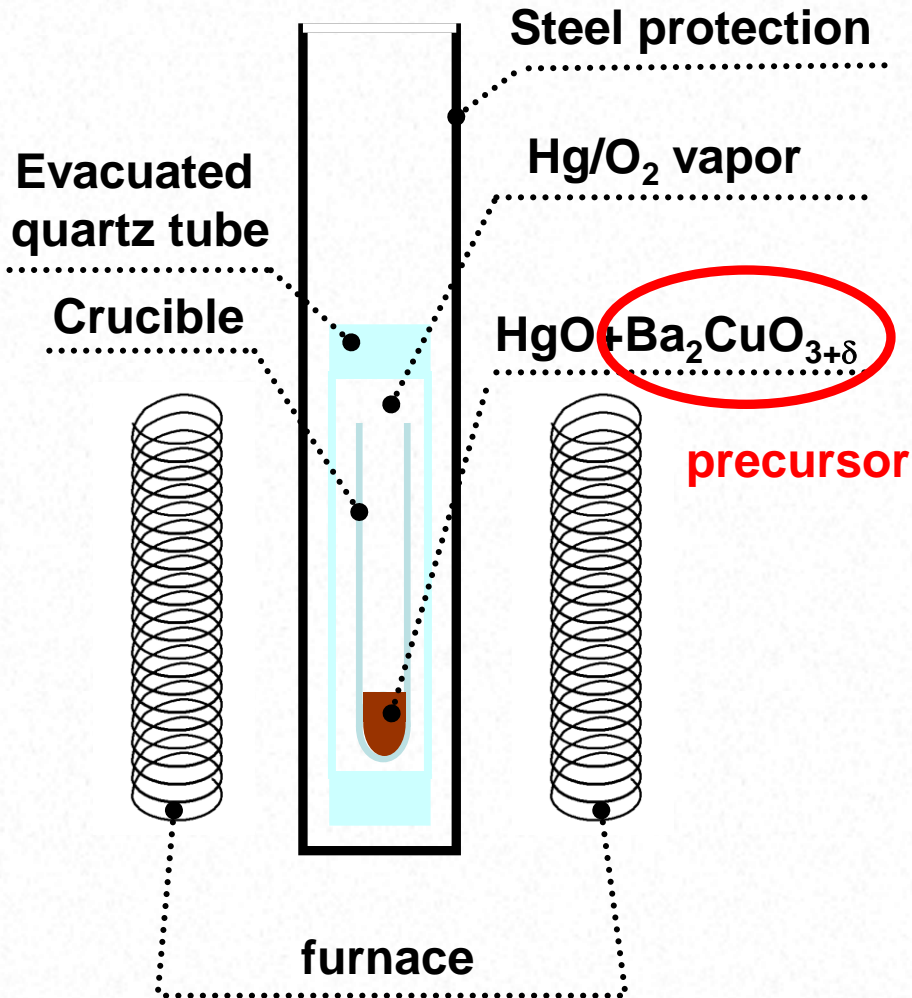
courtesy of Rudi Hackl

Model system $\text{HgBa}_2\text{CuO}_{4+\delta}$

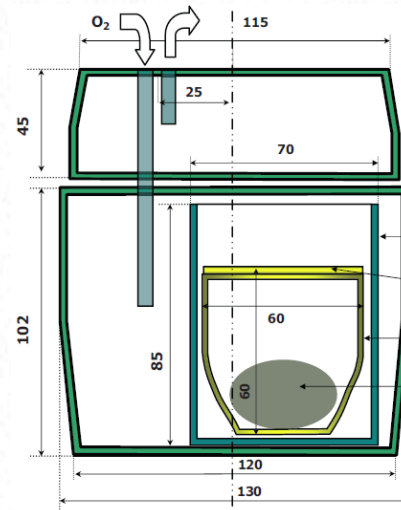


- ❑ Single layer, tetragonal
- ❑ Single Cu site, flat Cu-O sheet
- ❑ Doping disorder confined to far away from the Cu-O sheets
- ❑ Highest T_c (max. 97 K) among single-layer compounds

Challenges from the synthesis

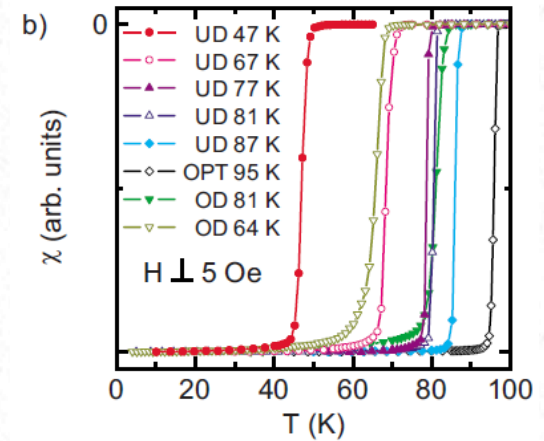
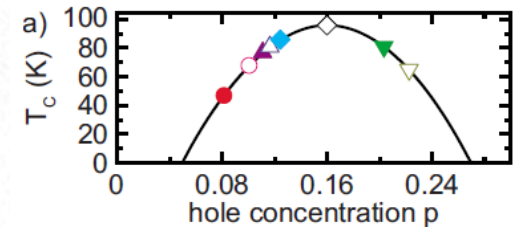
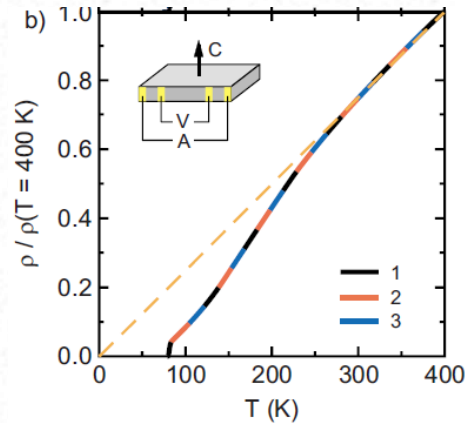
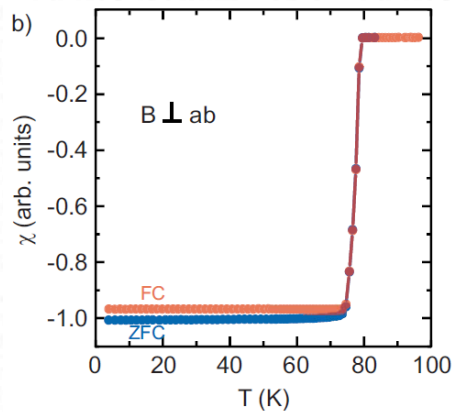


- ❑ Mercury is toxic ☹️
- ❑ Synthesis requires high pressure
- ❑ Purity against crystal size



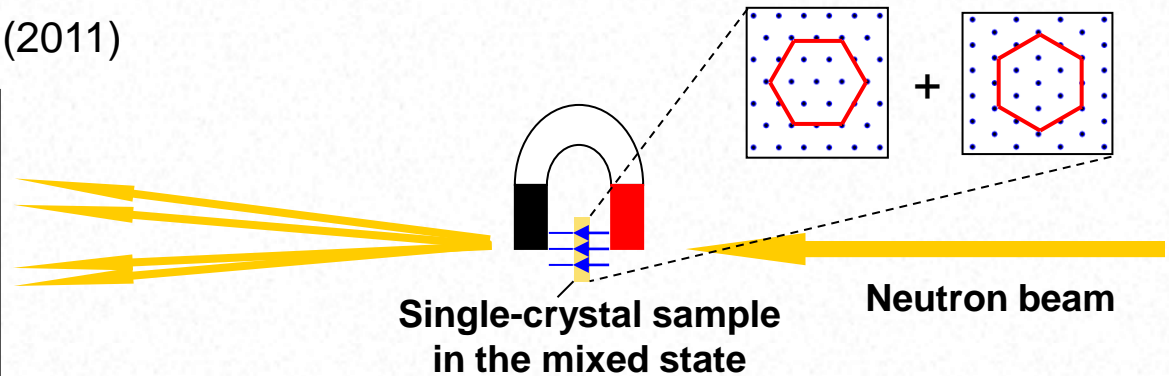
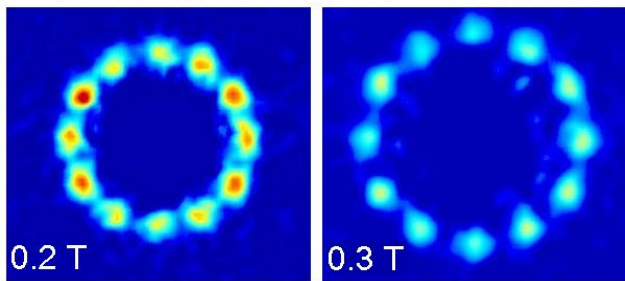
Principles of synthesis:
Zhao, *et al.*, *Adv. Mater.* **18**, 3243 (2006)

Pure and big single crystals

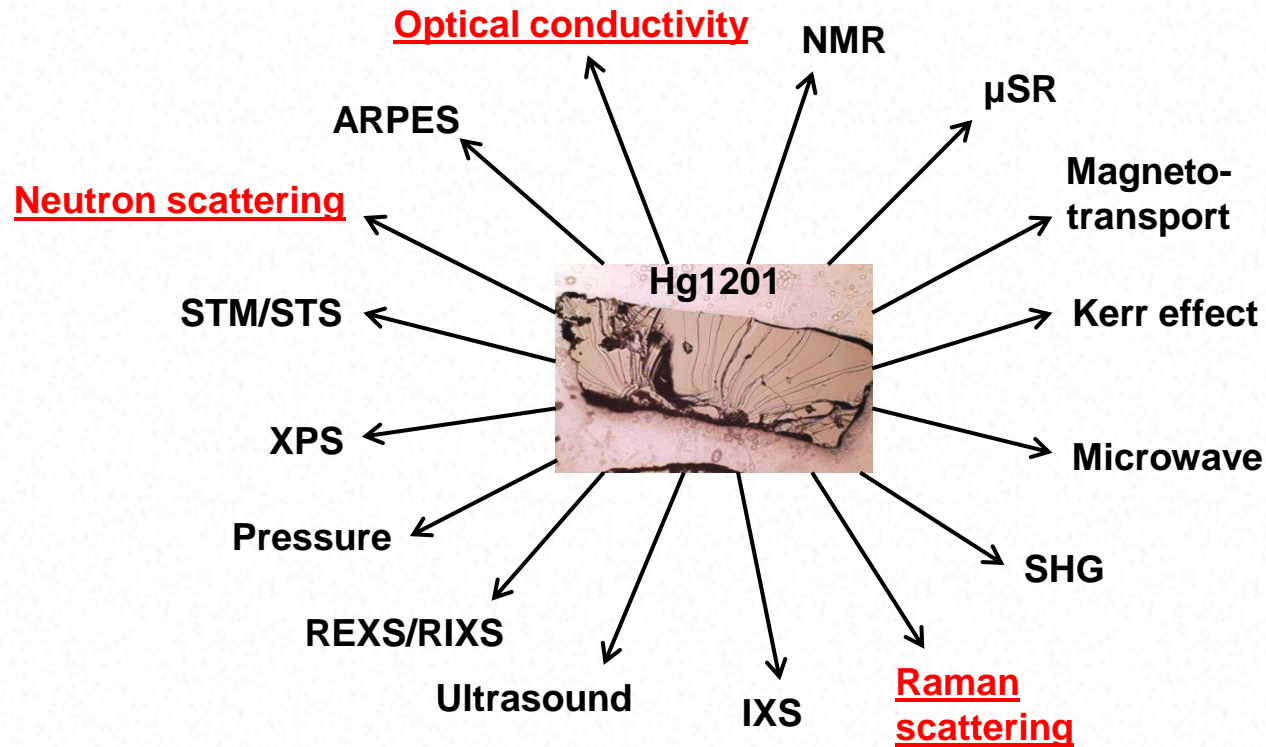


Barišić, YL, *et al.*, *PRB* **78**, 054518 (2008)

YL *et al.*, *Phys. Rev. B* **83**, 054507 (2011)



Work since 2008



Neutron scattering

Properties of neutron

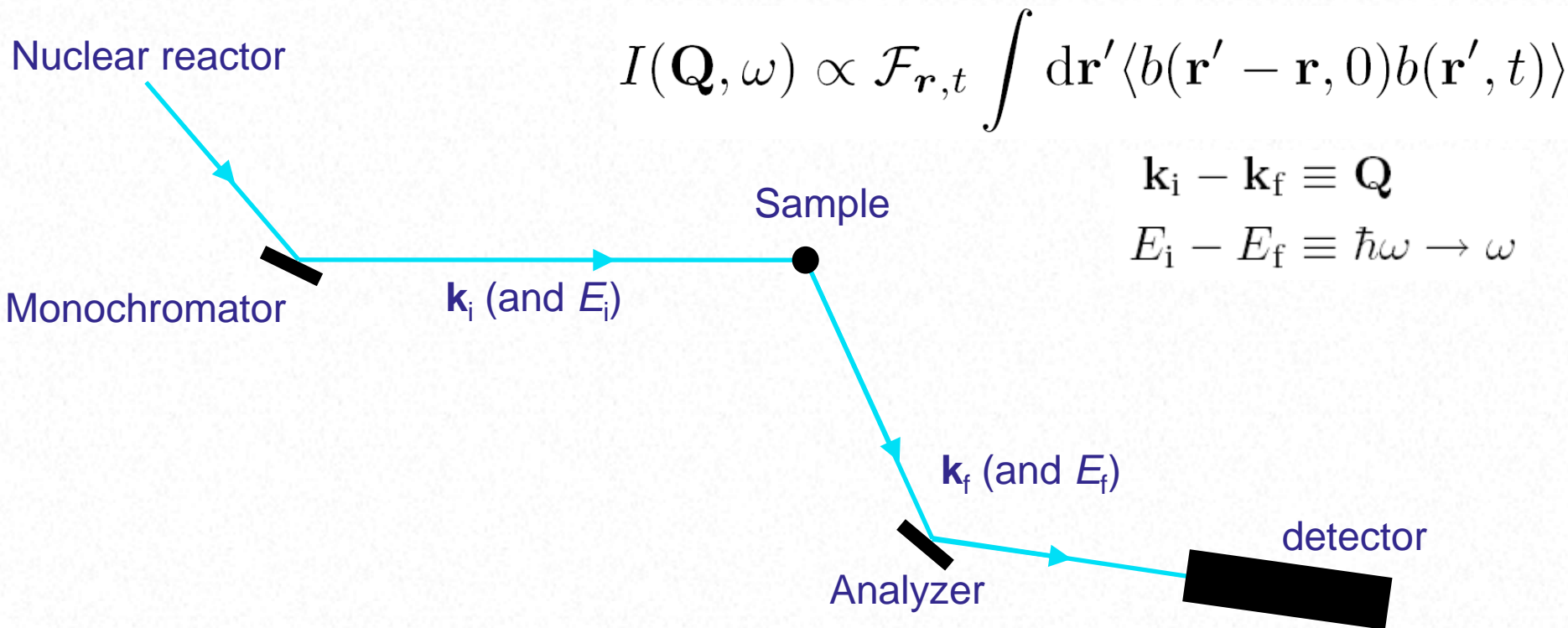
charge 0, spin 1/2
magnetic moment (P), energy (E)
and momentum (k)

scattering due to nuclear and
electromagnetic interaction

Thermal neutron

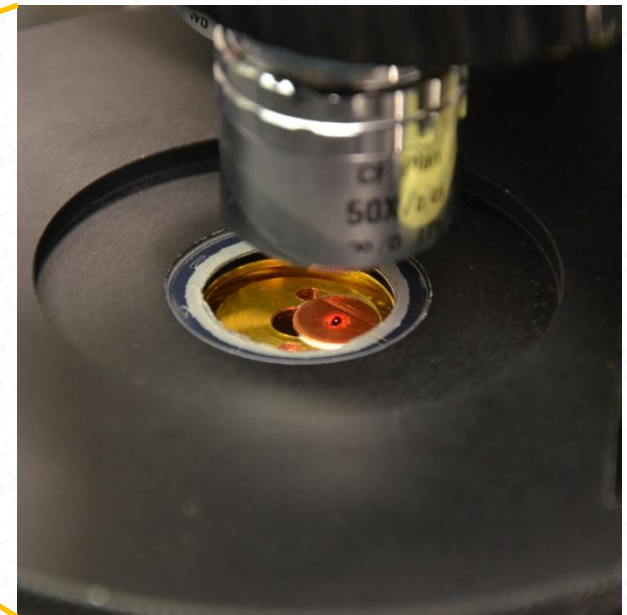
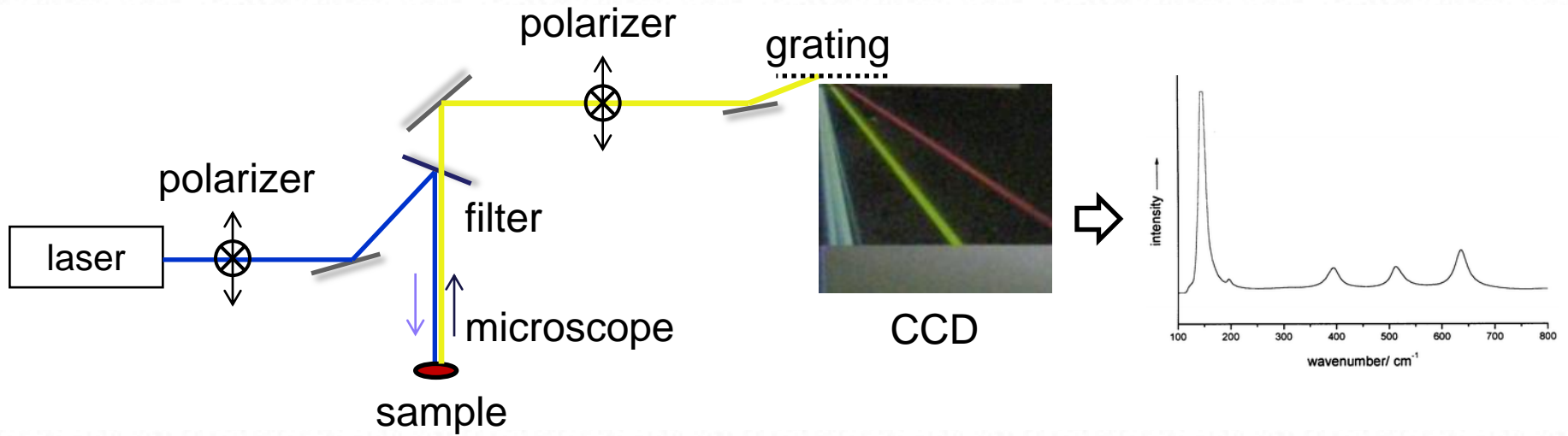
$E = 10\text{--}100\text{ meV}$, $k = 2\text{--}7\text{ \AA}^{-1}$

match typical energy and
momentum in solid state physics

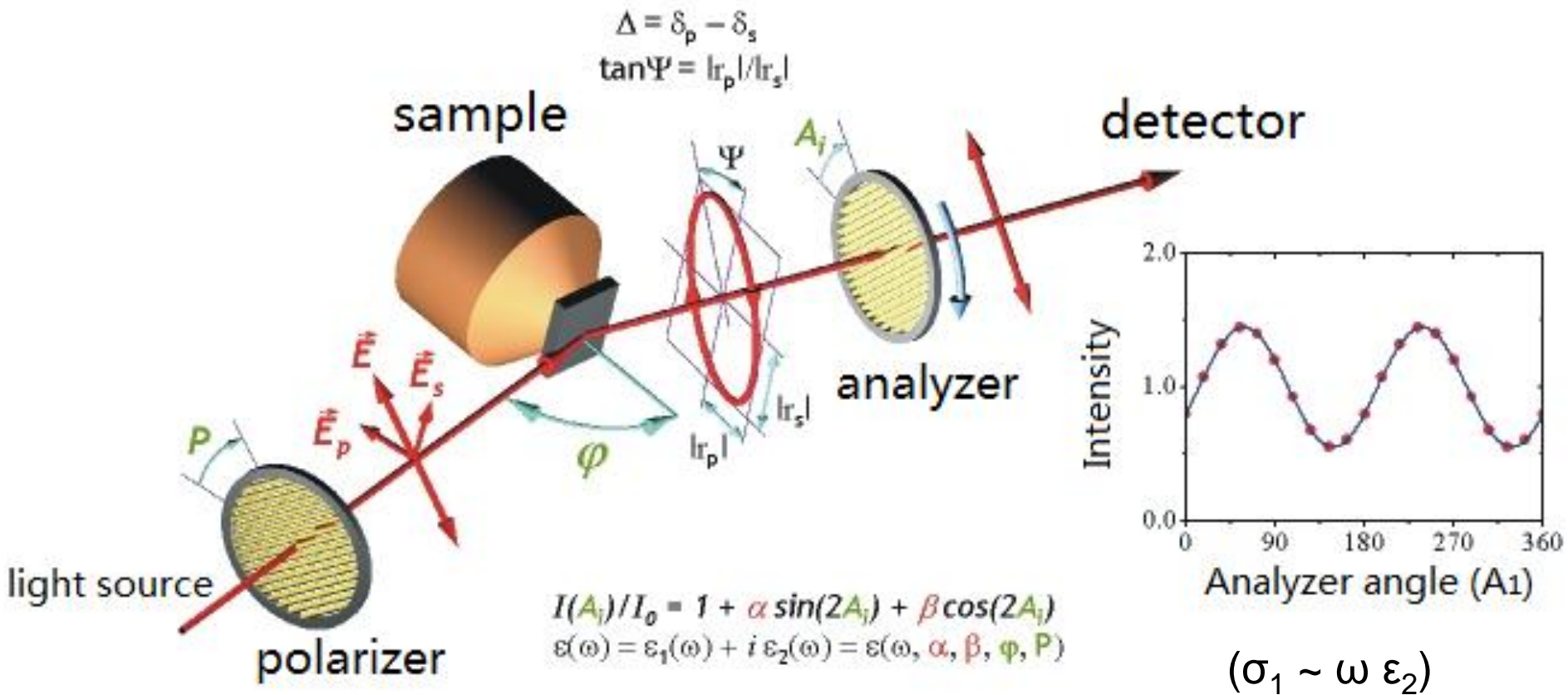




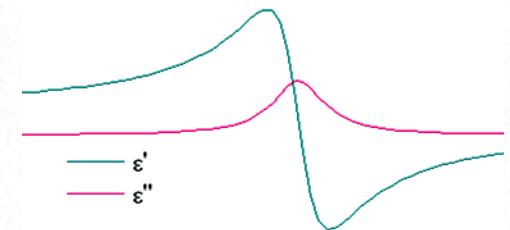
Raman scattering



Optical ellipsometry



$$\epsilon(\omega) = (n + i\kappa)^2 = 1 + \frac{e^2 N}{\epsilon_0 m V} \frac{1}{(\omega_0^2 - 2i\beta\omega - \omega^2)}$$



Outline

□ Introduction

- HTSC and the cuprates
- Spectroscopic methods applied to the high- T_c problem

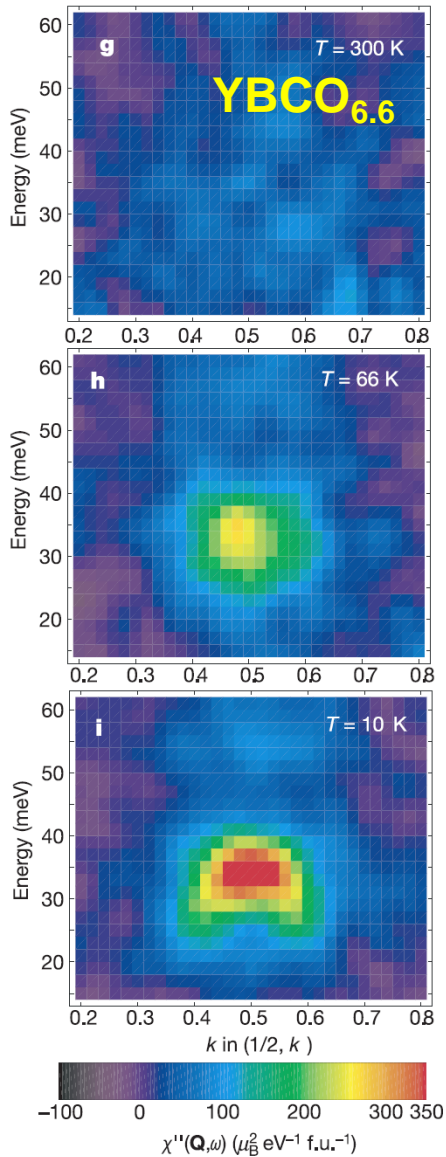
□ Model system $\text{HgBa}_2\text{CuO}_{4+\delta}$

□ Topics:

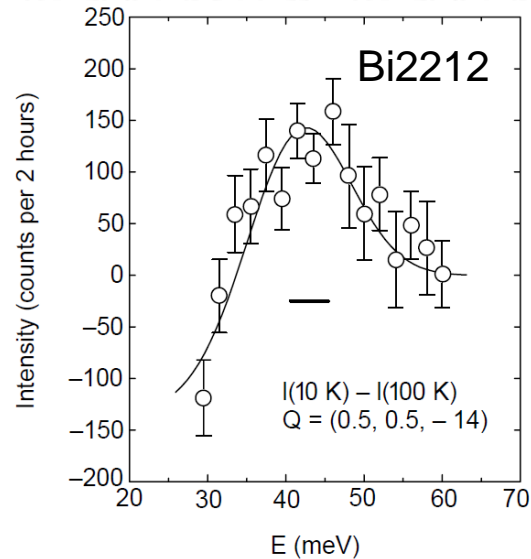
1. The neutron resonant mode
2. Pseudogap magnetism
3. Energy $2\Delta_{\text{sc}}$ and above

□ Summary

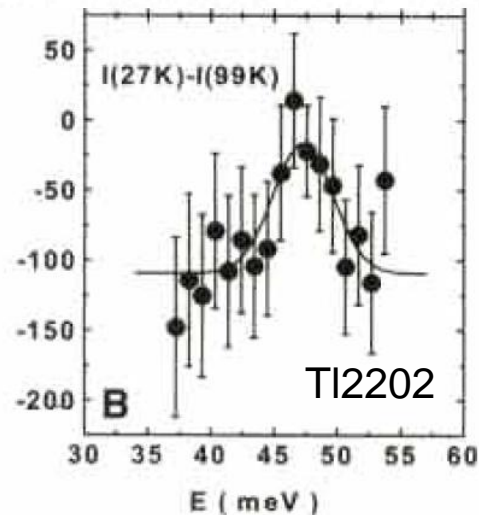
The neutron resonant mode



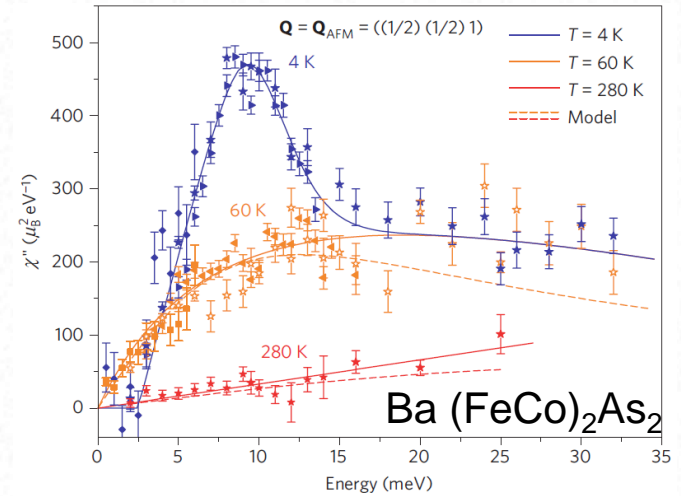
Hayden *et al.*, *Nature* **429**, 531 (2004)



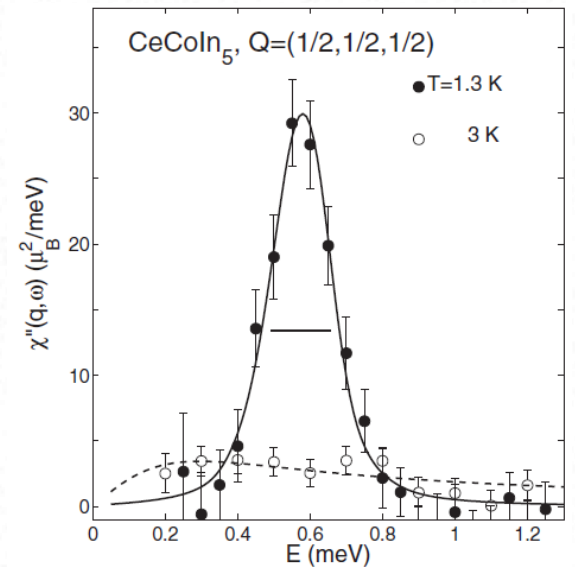
Fong *et al.*, *Nature* **398**, 588 (1999)



He *et al.*, *Science* **295**, 1045 (2002)

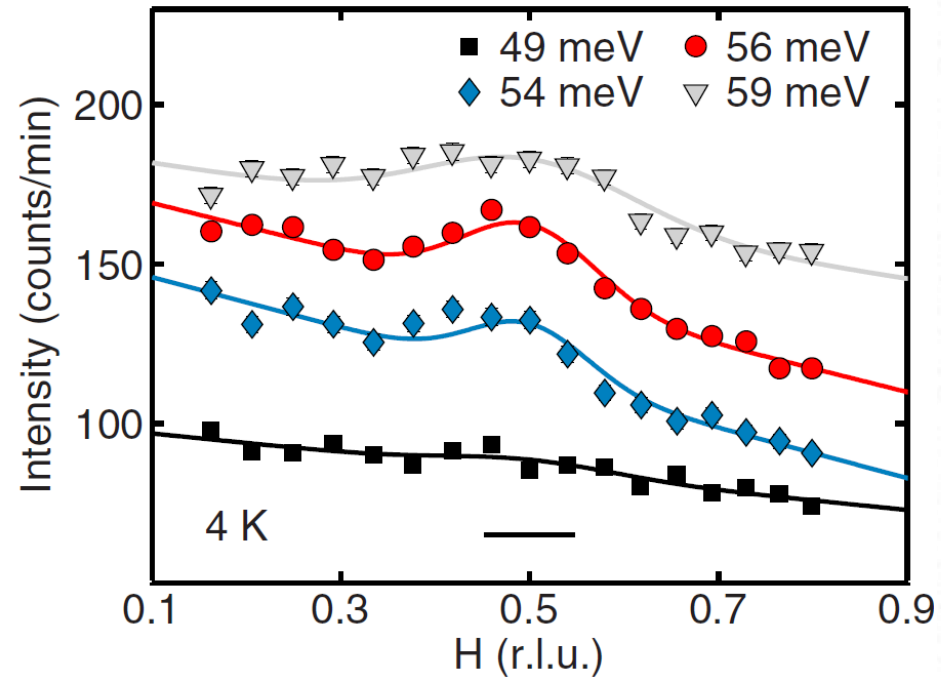
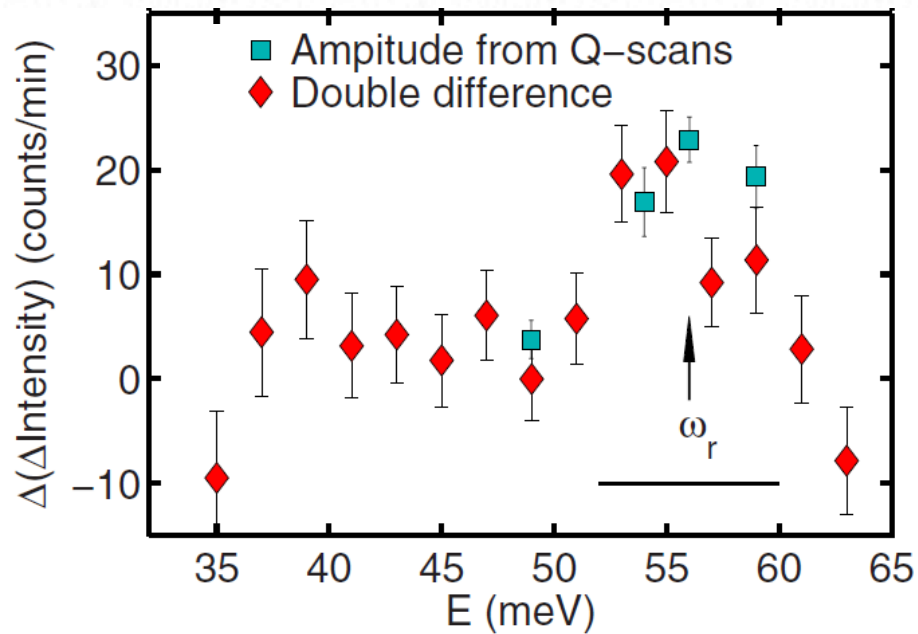


Inosov *et al.*, *Nat. Phys.* **6**, 178 (2010)

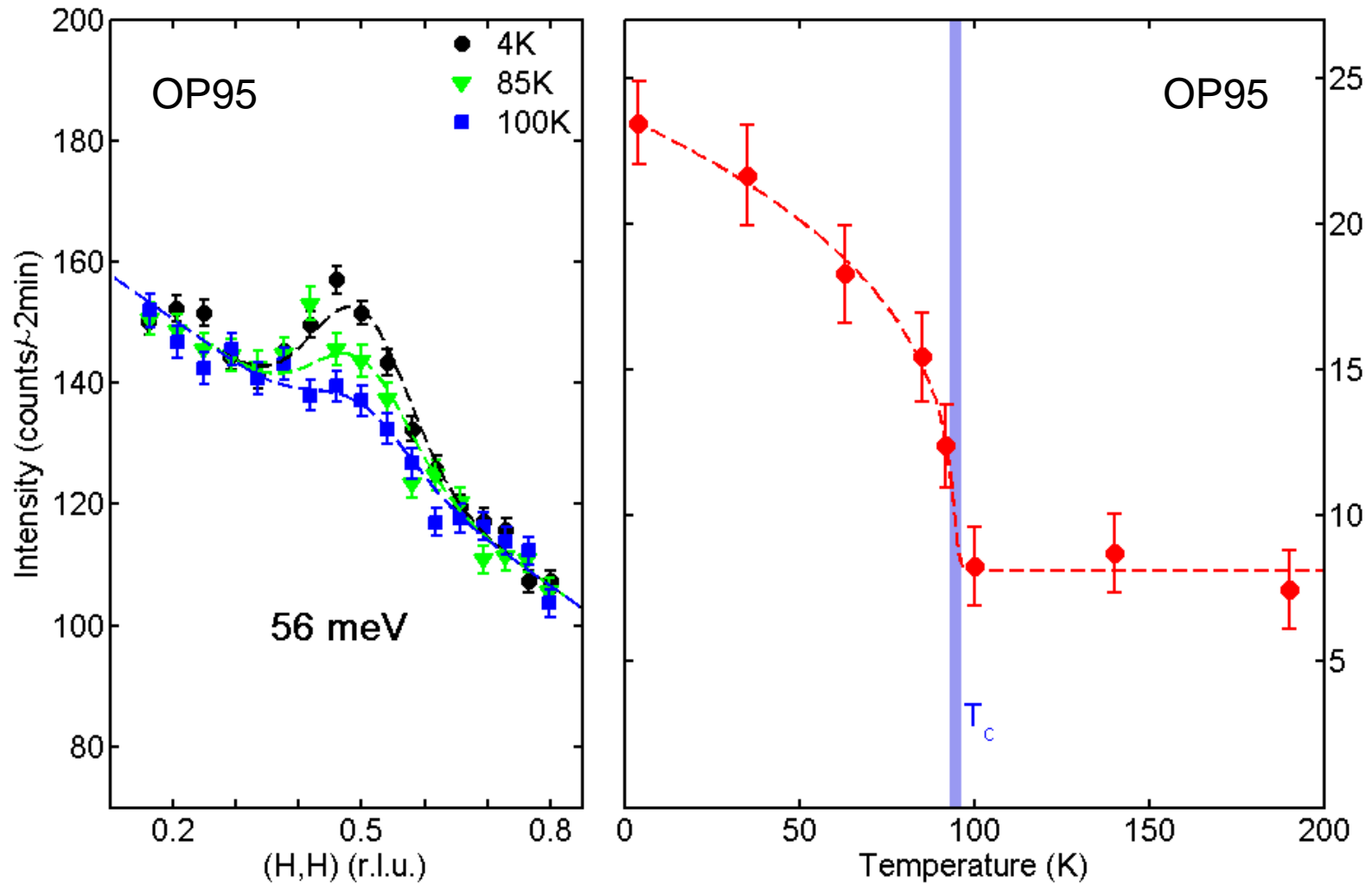


Stock *et al.*, *PRL* **100**, 087001 (2008)

Resonant mode in Hg1201



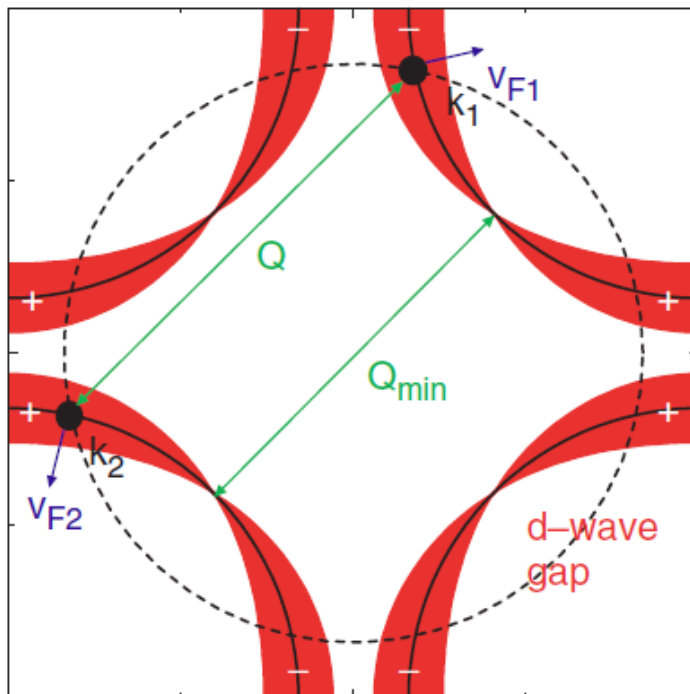
Resonant mode in Hg1201



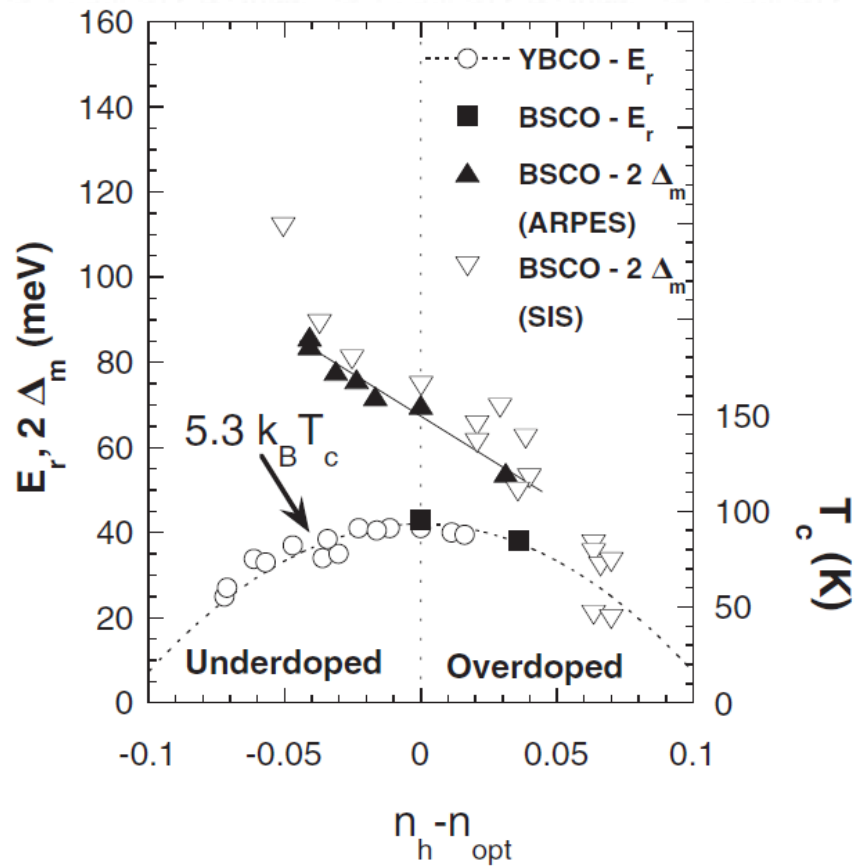
Resonant mode in Hg1201

- We confirmed the universal presence of the resonant mode
- Sign-changing Δ_{sc} connected by \mathbf{q}_{res} : as expected from *d*-wave

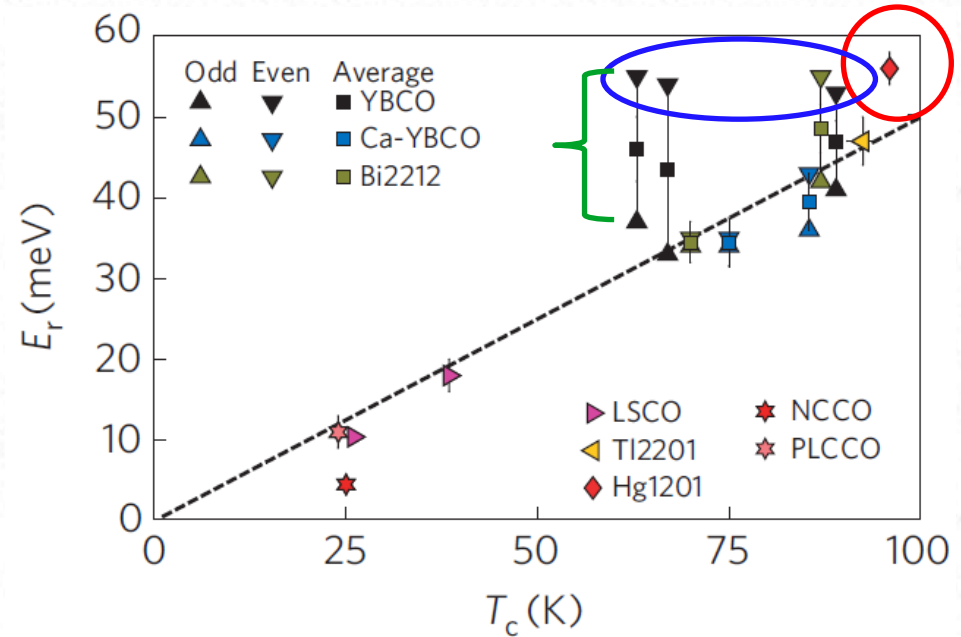
$$\text{Coherence factor: } \frac{1}{2} \left(1 - \frac{\Delta(k)\Delta(k+q^*)}{\mathcal{E}(k)\mathcal{E}(k+q^*)} \right)$$



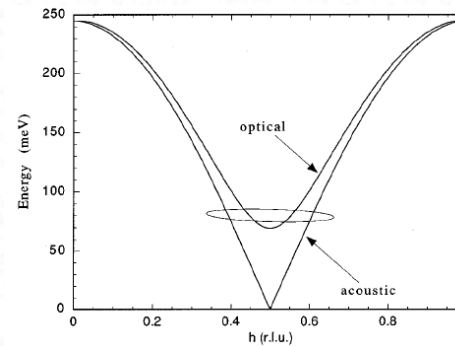
Conventional wisdom: $E_r \propto T_c$



Sidis *et al.*, *Phys. Stat. Sol.* **241**, 1204 (2004)



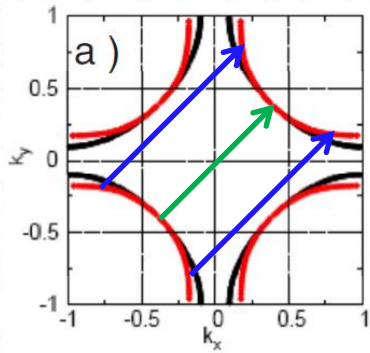
Yu, YL *et al.*, *Nature Physics* **5**, 873 (2009)



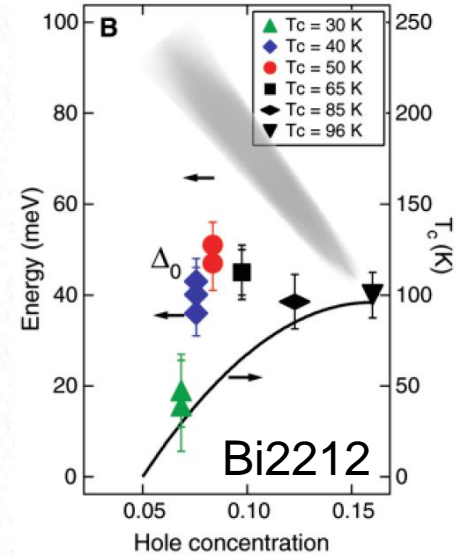
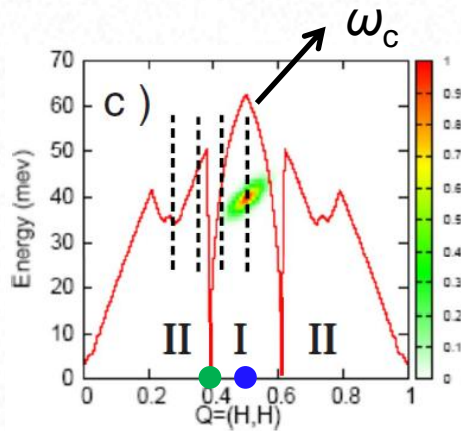
Consistent with
 $J_{\perp} \sim 10 \text{ meV}$

Reznik *et al.*,
PRB **53**, R14741 (1996)

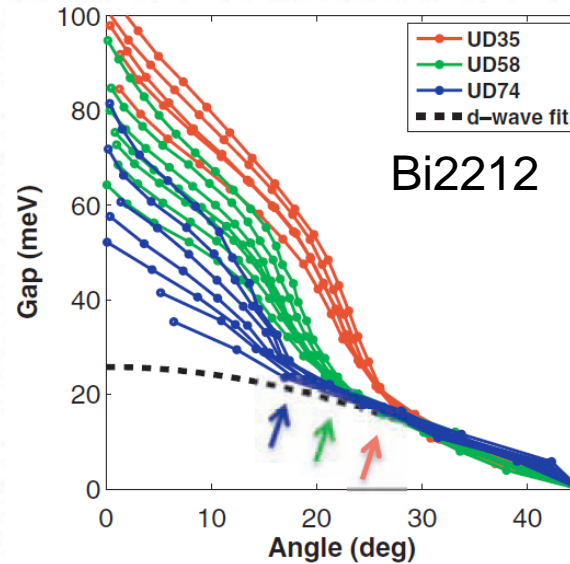
Superconducting gap: Δ_{sc}



Fauque *et al.*, *PRB* **76**, 214512 (2007)



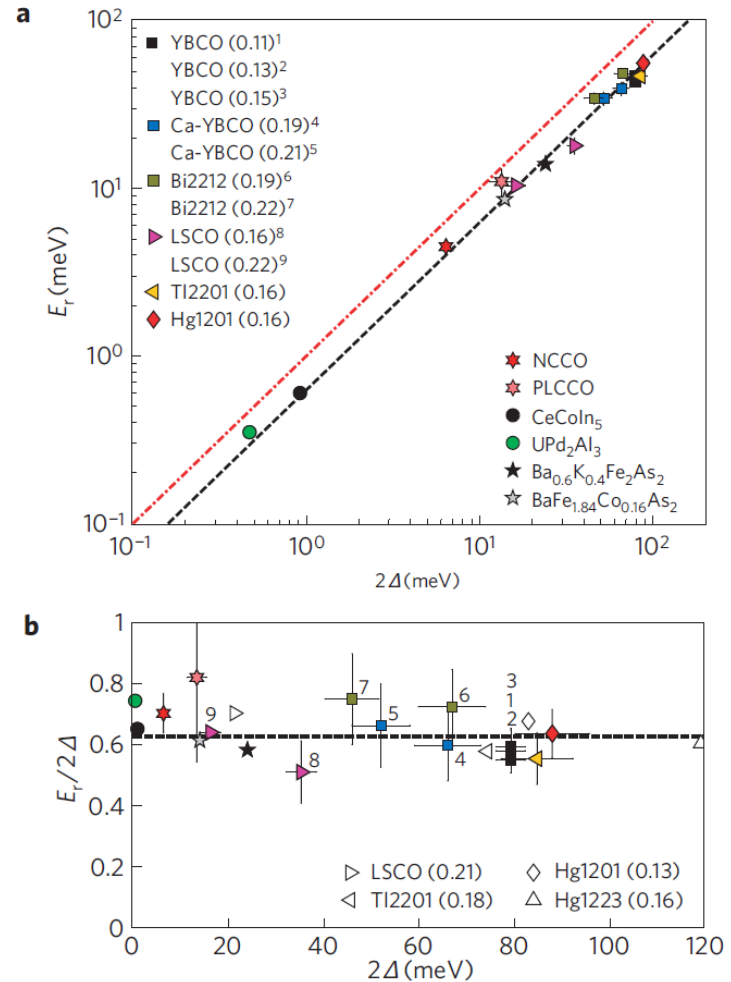
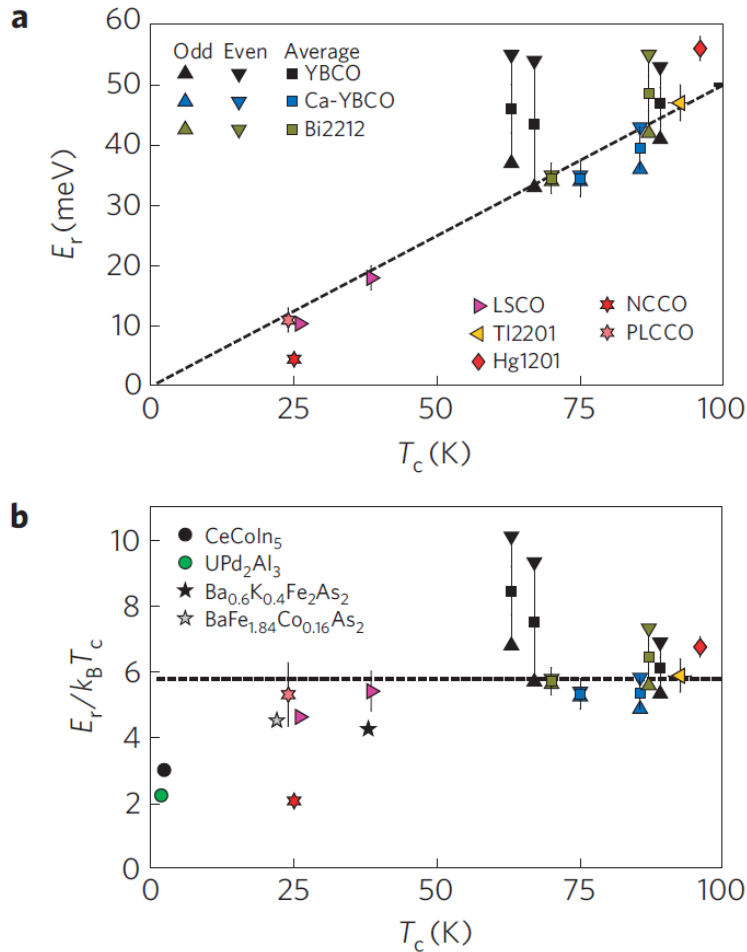
Tanaka *et al.*,
Science **314**,
1910 (2006)



Pushp *et al.*,
Science **324**,
1689 (2009)

Universal E_r - Δ_{SC} scaling

- Δ is not proportional to T_c in underdoped systems
- One should consider both resonant modes in bilayer systems

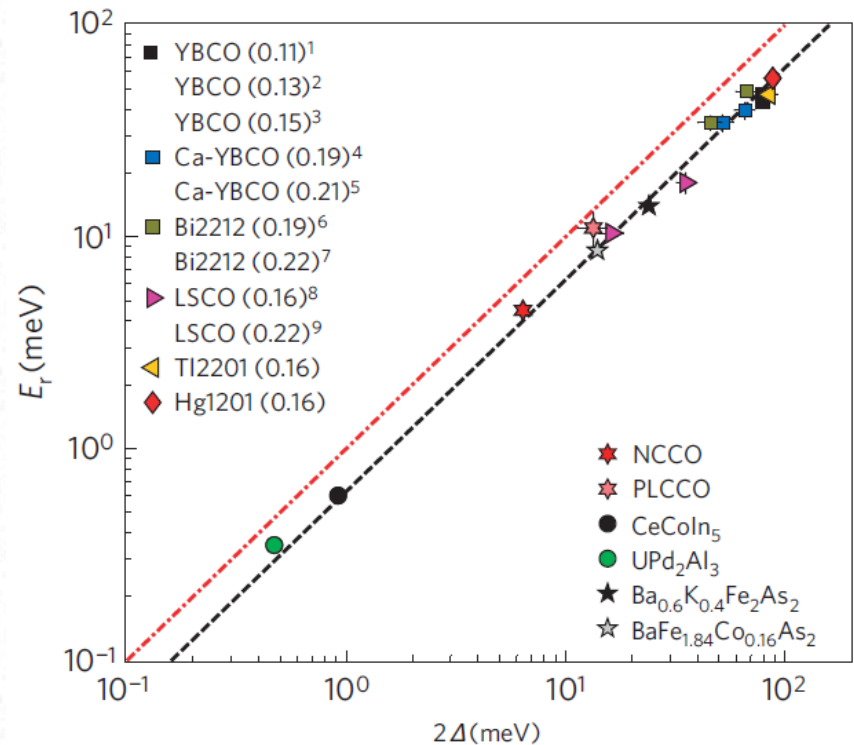


Implication

❑ Unexpected from a simple RPA excitonic picture

$$\chi(q, \omega) = \frac{\chi_0(q, \omega)}{1 + J(q) \chi_0(q, \omega)}$$

❑ Implies a much deeper connection between magnetic fluctuations (entire spectrum) and superconductivity



Yu, YL *et al.*, *Nature Physics* **5**, 873 (2009)

VOLUME 88, NUMBER 25

PHYSICAL REVIEW LETTERS

24 JUNE 2002

Spin-1 Neutron Resonance Peak Cannot Account for Electronic Anomalies in the Cuprate Superconductors

Hae-Young Kee,^{1,2} Steven A. Kivelson,¹ and G. Aeppli³

Outline

□ Introduction

- HTSC and the cuprates
- Spectroscopic methods applied to the high- T_c problem

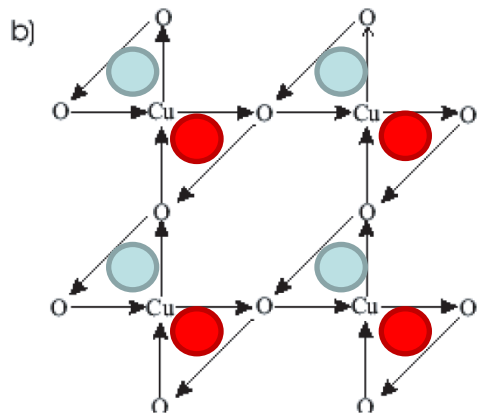
□ Model system $\text{HgBa}_2\text{CuO}_{4+\delta}$

□ Topics:

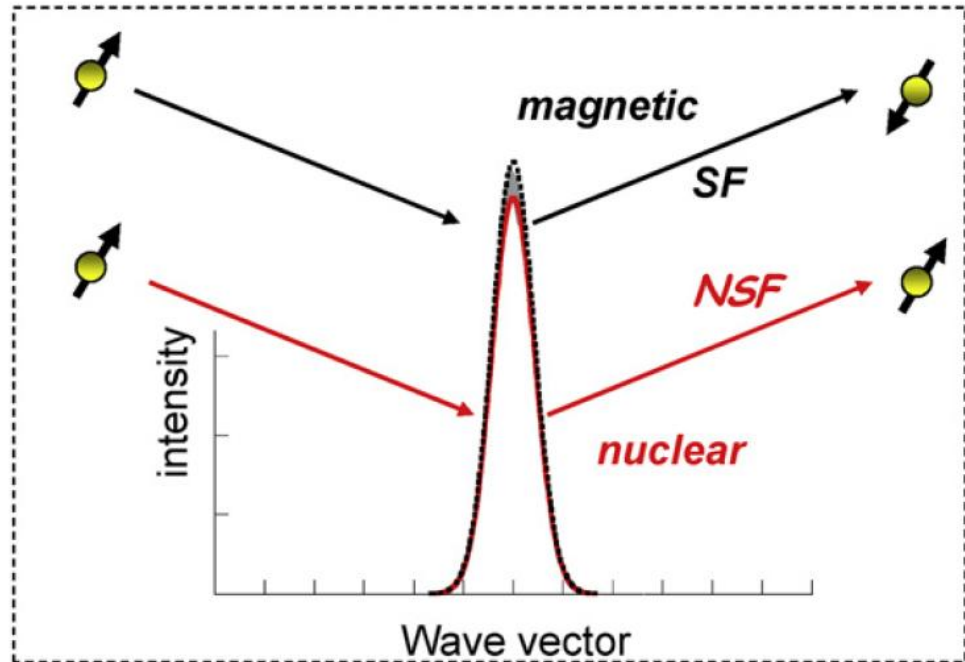
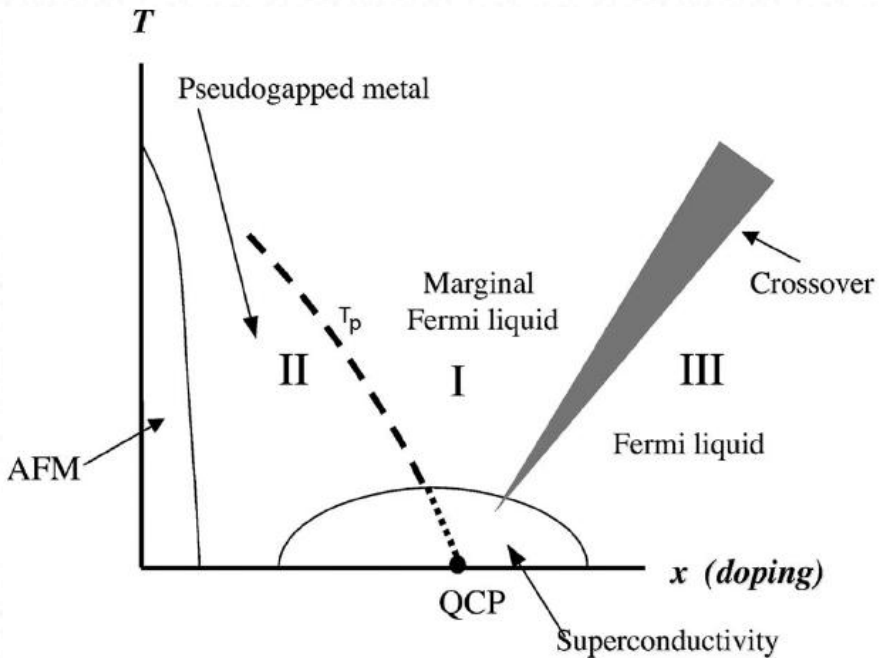
1. The neutron resonant mode
2. Pseudogap magnetism
3. Energy $2\Delta_{\text{sc}}$ and above

□ Summary

“Orbital current” order



Varma, *PRB* **73**, 155113 (2006)



Bourges & Sidis, *C.R. Physique* **12**, 461 (2011)

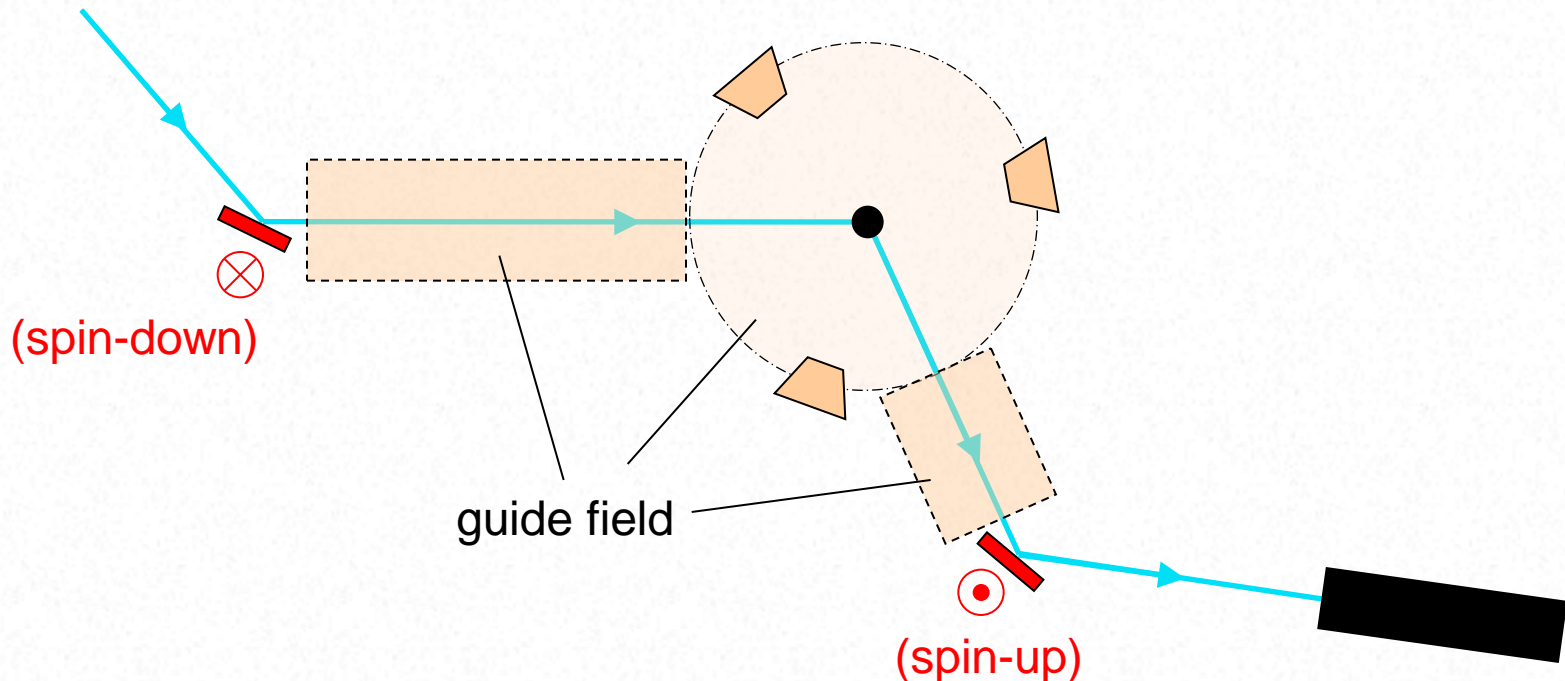
Spin-polarized neutron scattering

Properties of neutron

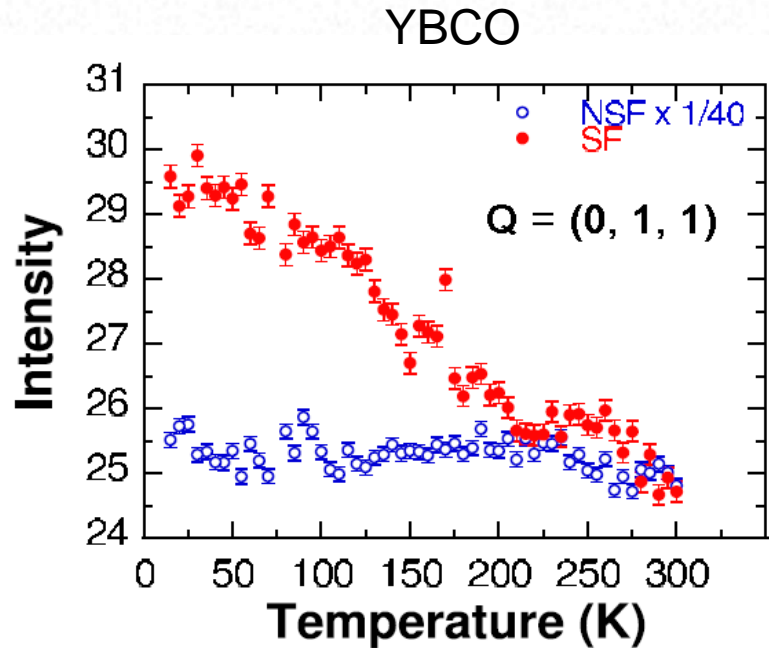
charge 0, spin 1/2
magnetic moment (P), energy (E)
and momentum (k)

scattering due to nuclear and
electromagnetic interaction

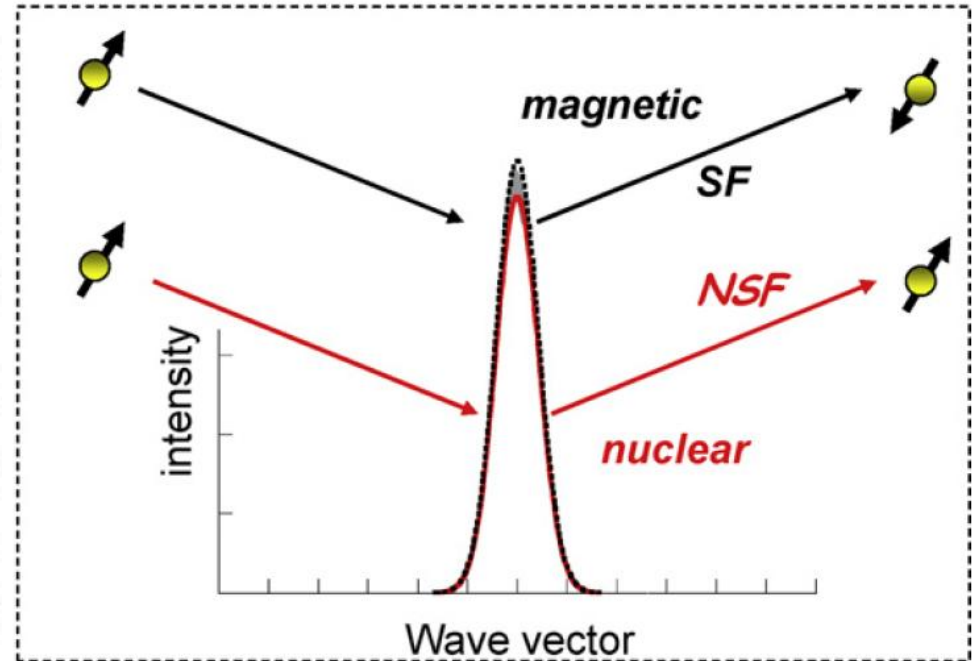
Spin-flip scattering all comes
from electromagnetic interaction



Intra-unit-cell order: initial evidence



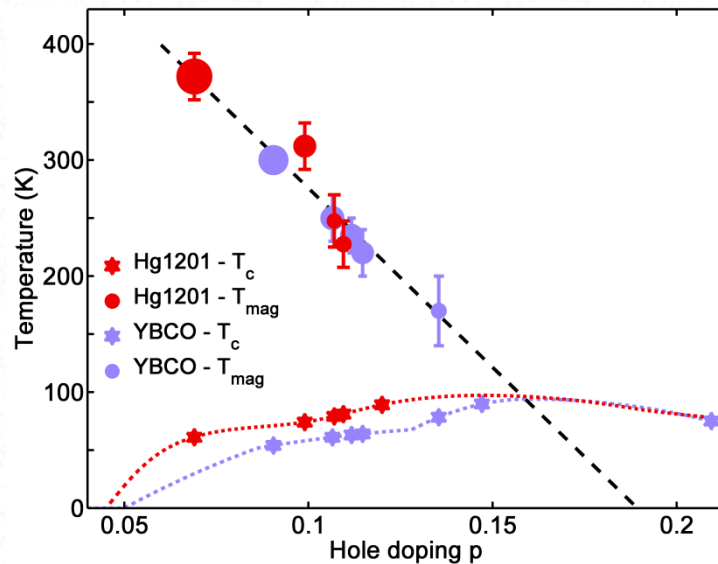
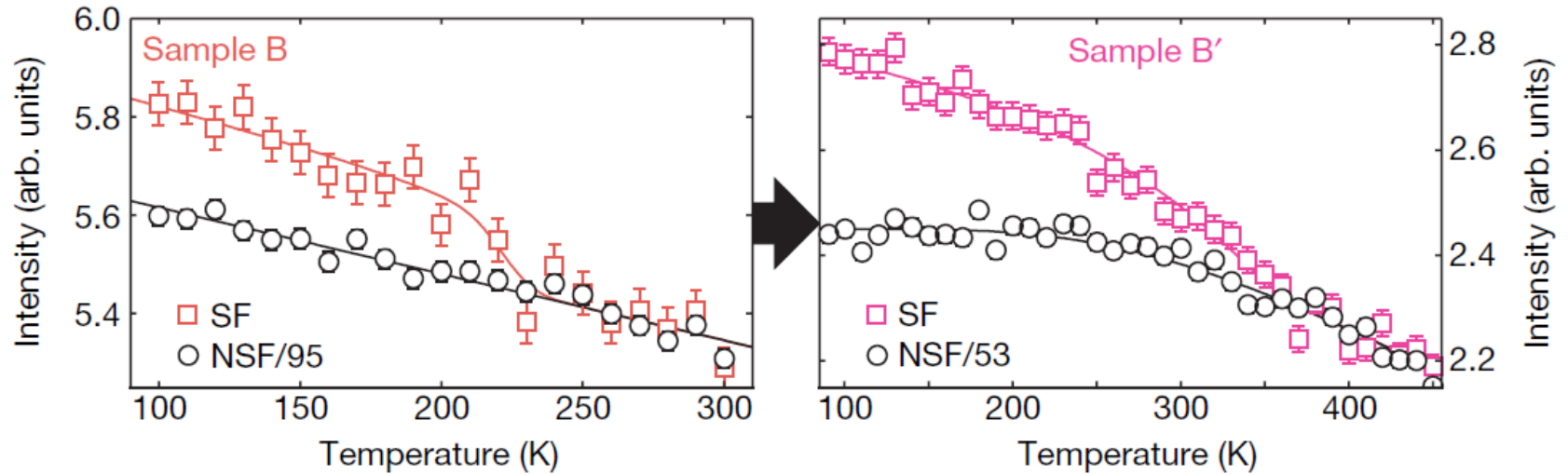
Fauqué *et al.*, *PRL* **96**, 197001 (2006)



Bourges & Sidis, *C.R. Physique* **12**, 461 (2011)

Intra-unit-cell order: confirmed in Hg1201

(1 0 1) Bragg peak

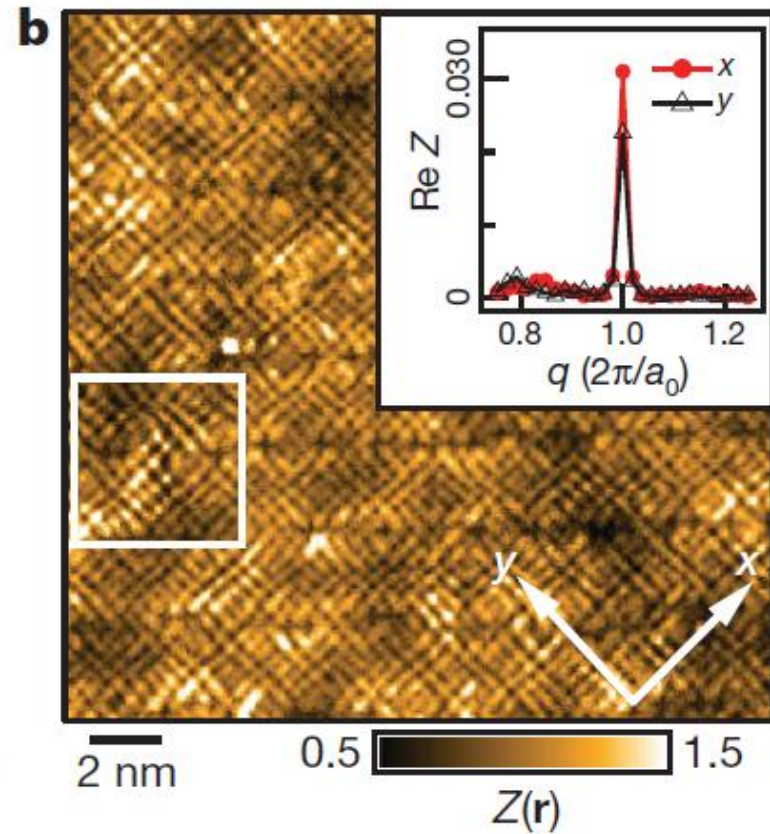
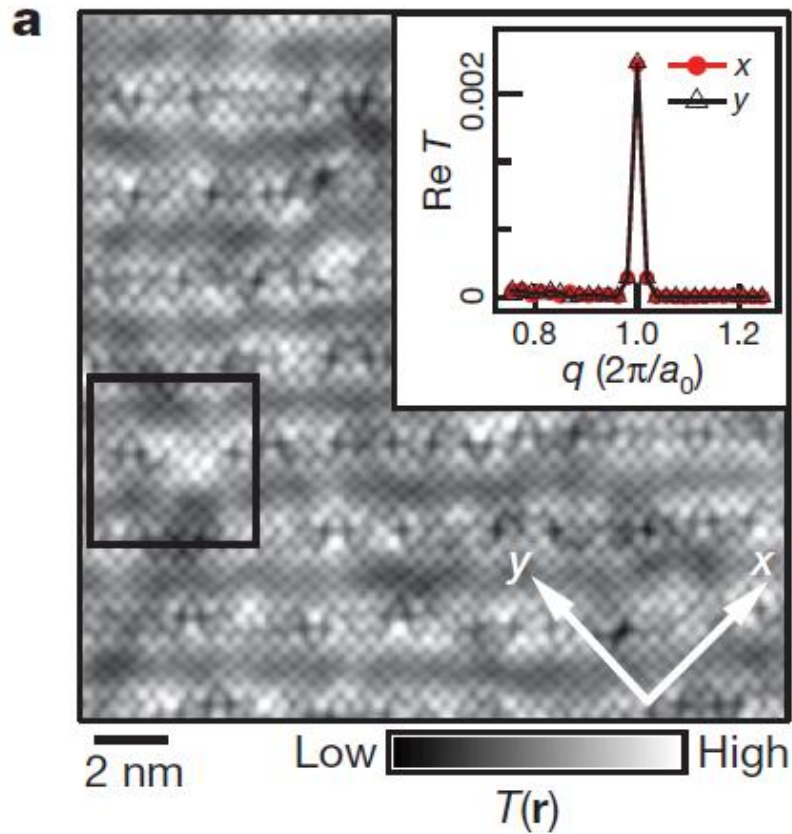


YL *et al.*, *Nature* **455**, 372 (2008)

YL *et al.*, *PRB* **84**, 224508 (2012)

Intra-unit-cell order: evidence from STM/STS

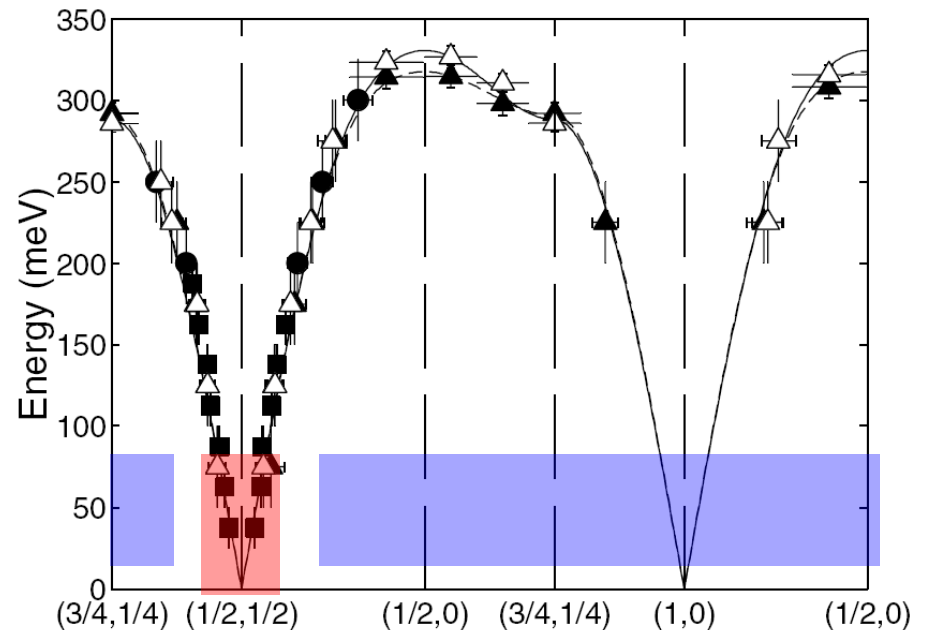
Lawler *et al.*, *Nature* **466**, 347 (2010)



New excitations in the pseudogap state

AF-type fluctuations near $(1/2, 1/2)$, including the resonance

New excitations



Spin waves in La_2CuO_4

Coldea *et al.*, *PRL* **86**, 5377 (2001)

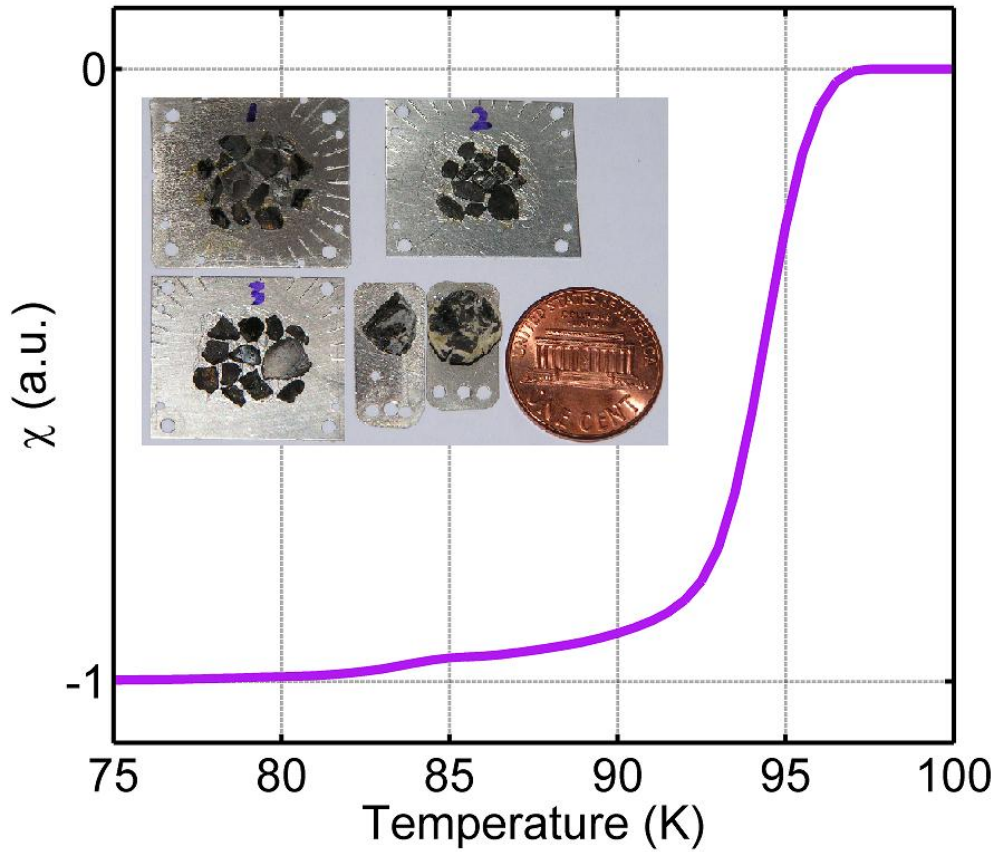
Related publications:

YL *et al.*, *Nature* **468**, 283 (2010)

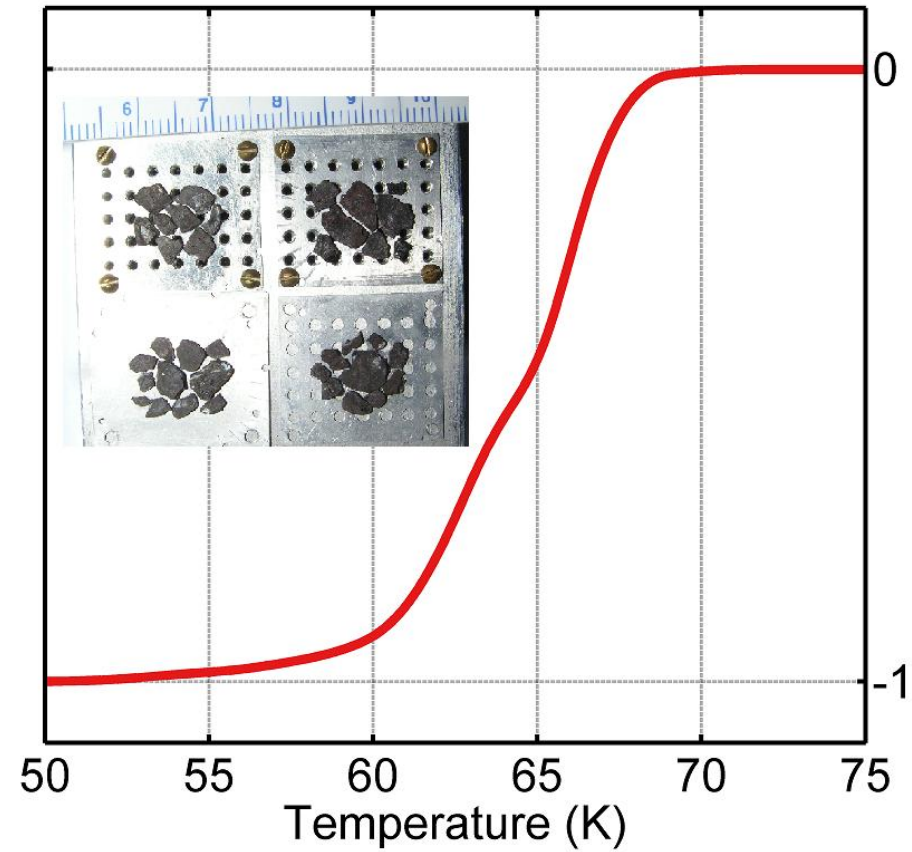
YL *et al.*, *Nat. Phys.* **8**, 404 (2012)

Samples

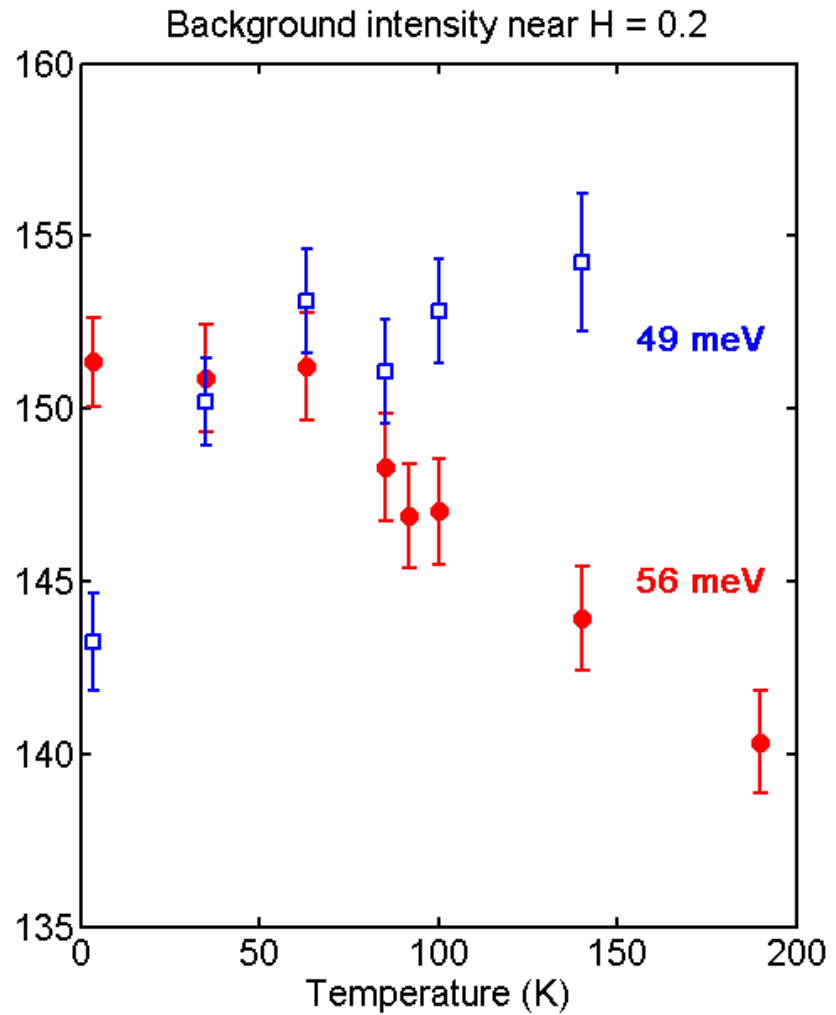
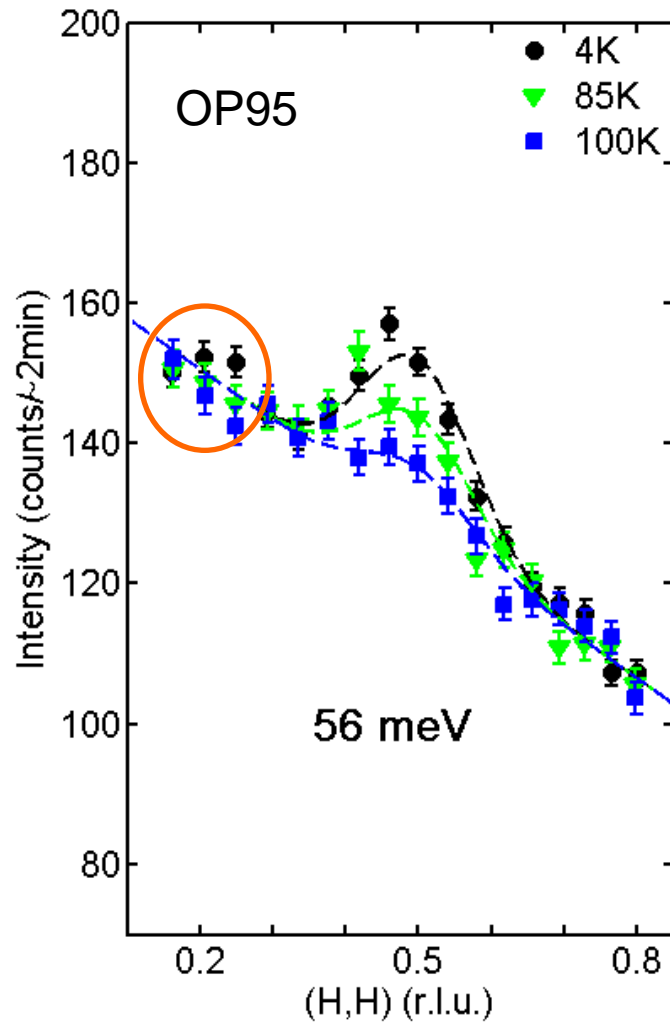
“OP95”



“UD65”

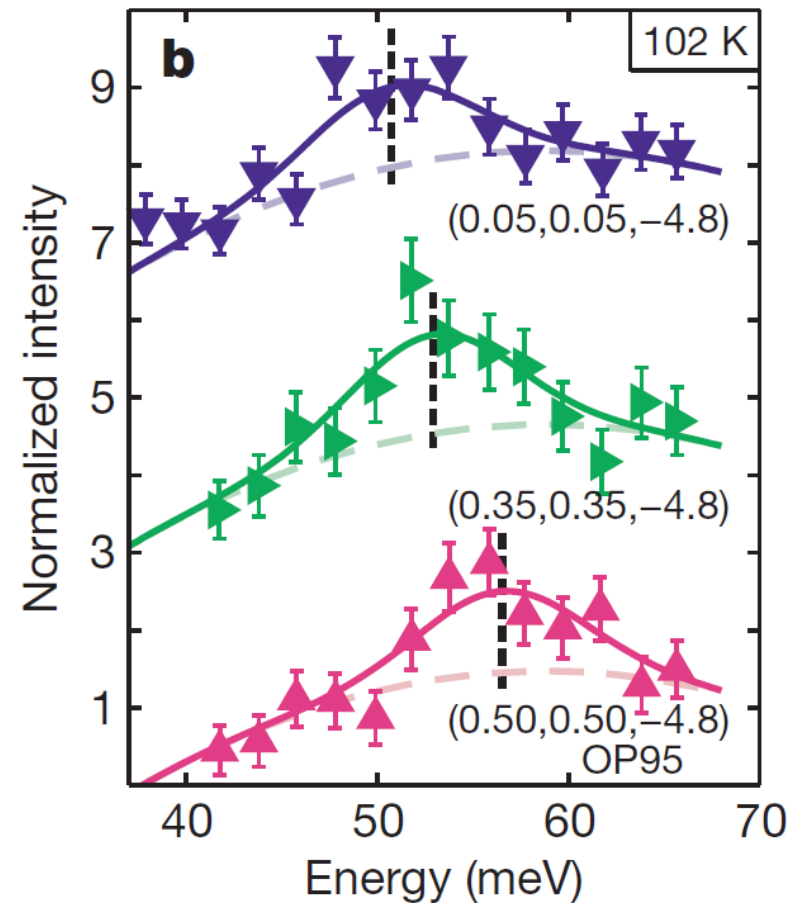
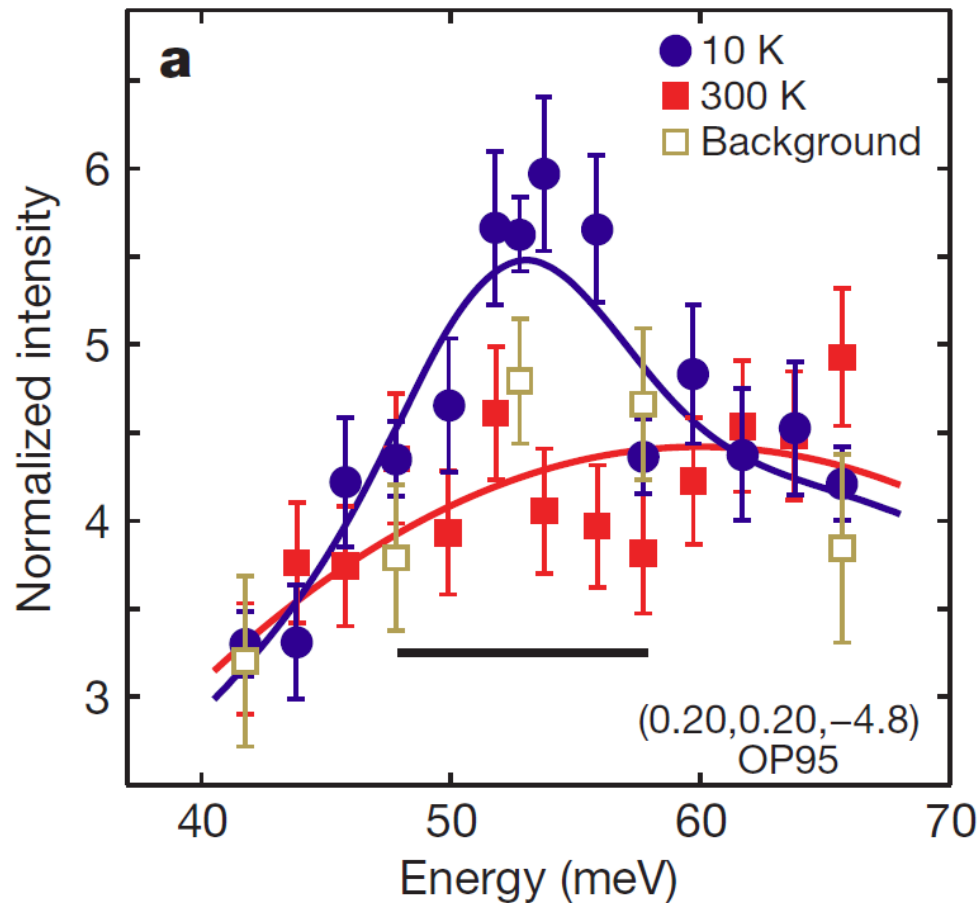


Unusual aspect of the resonance data



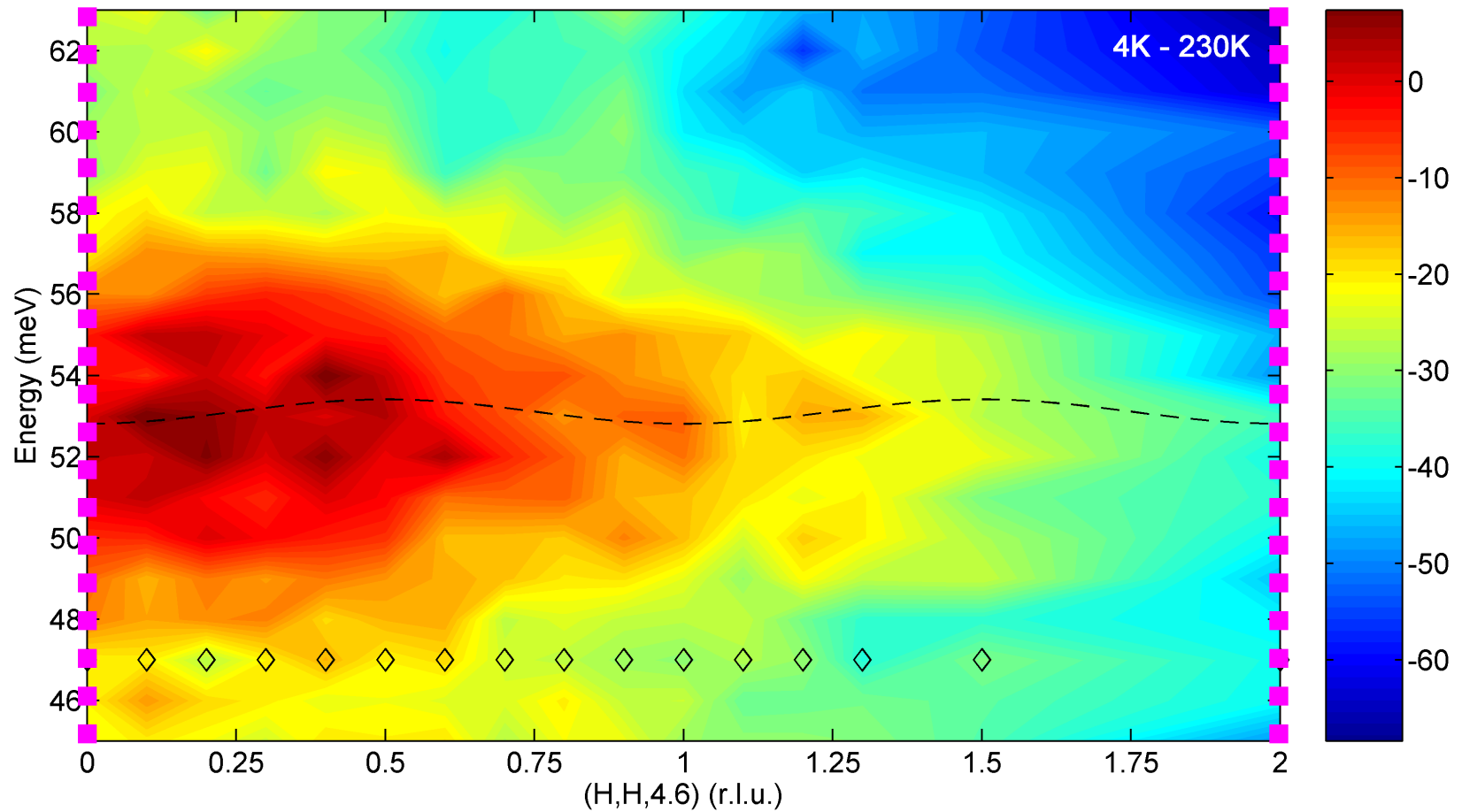
Verification of magnetic origin

Measured in spin-flip geometry

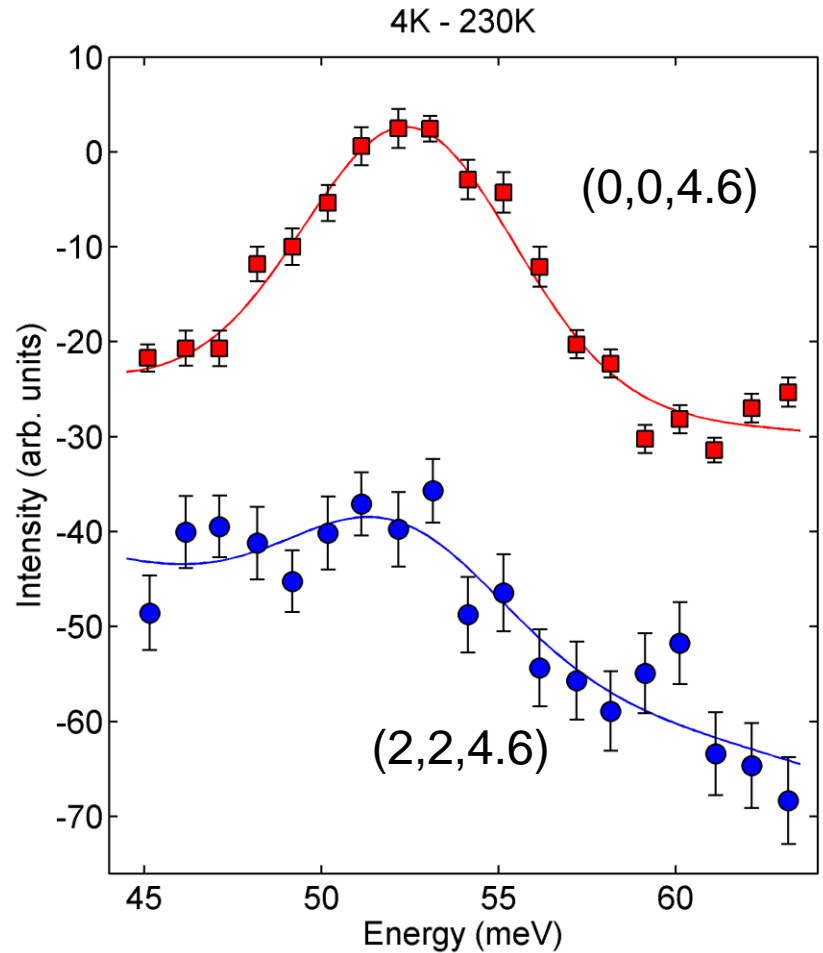
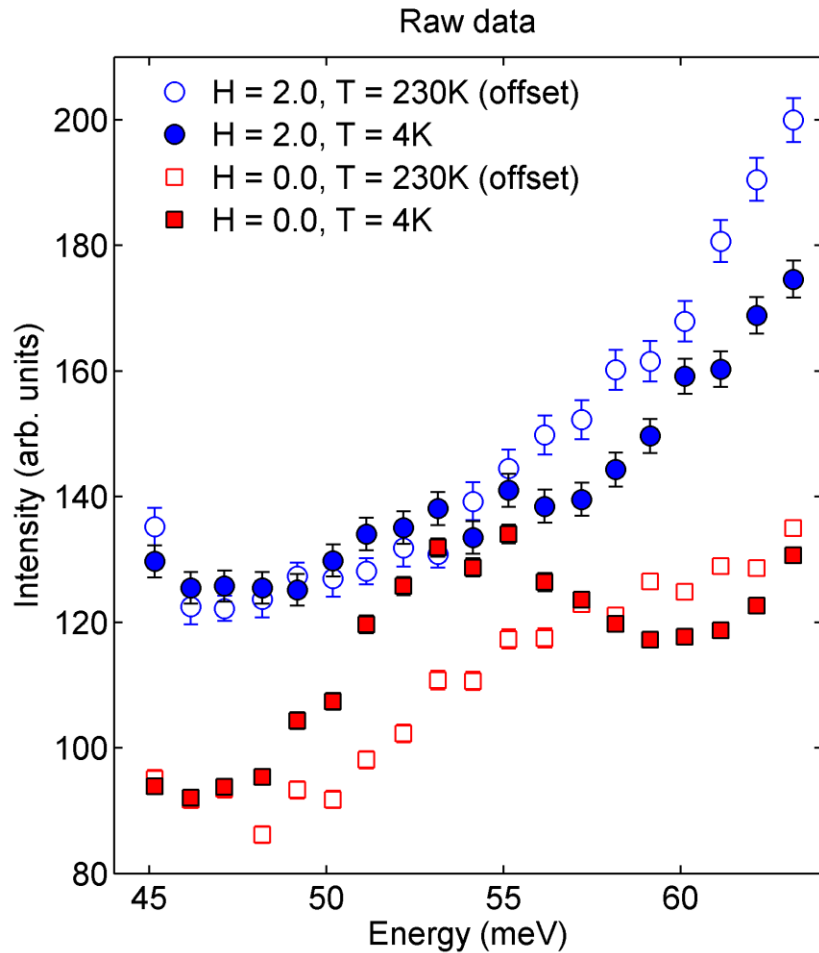


Almost dispersiveless excitation

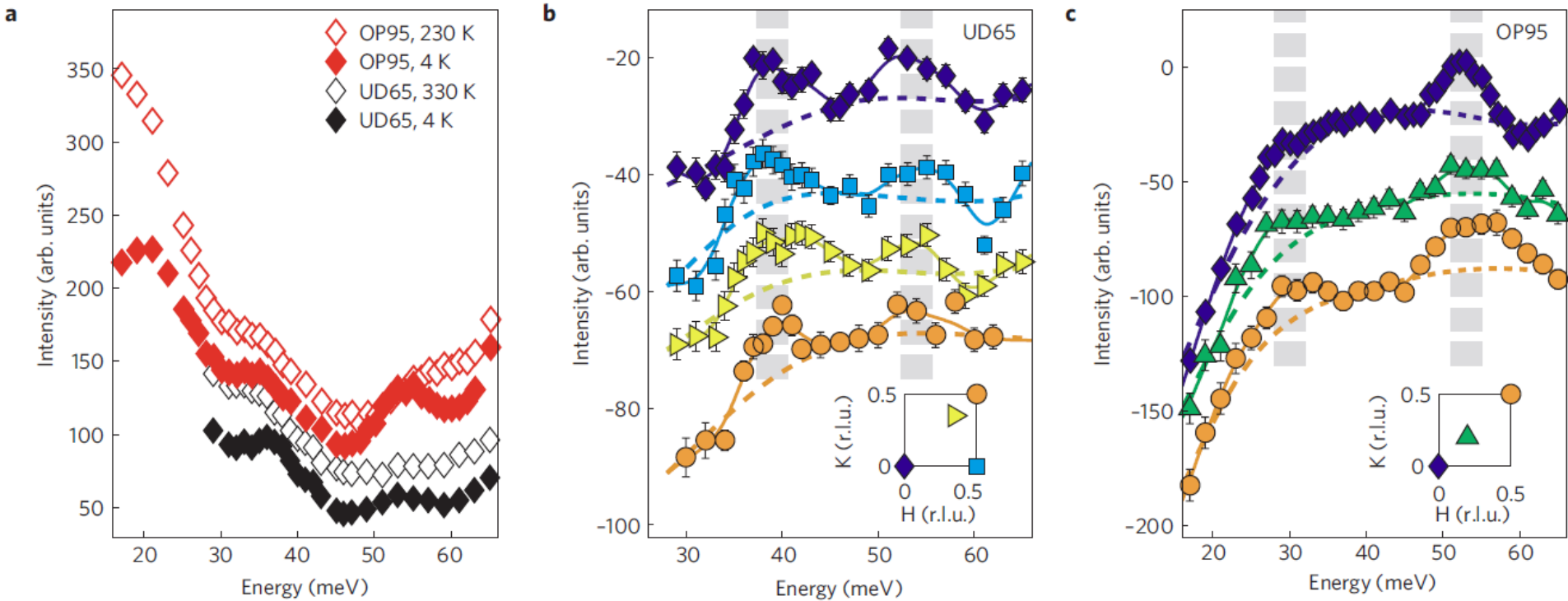
Sample: OP95



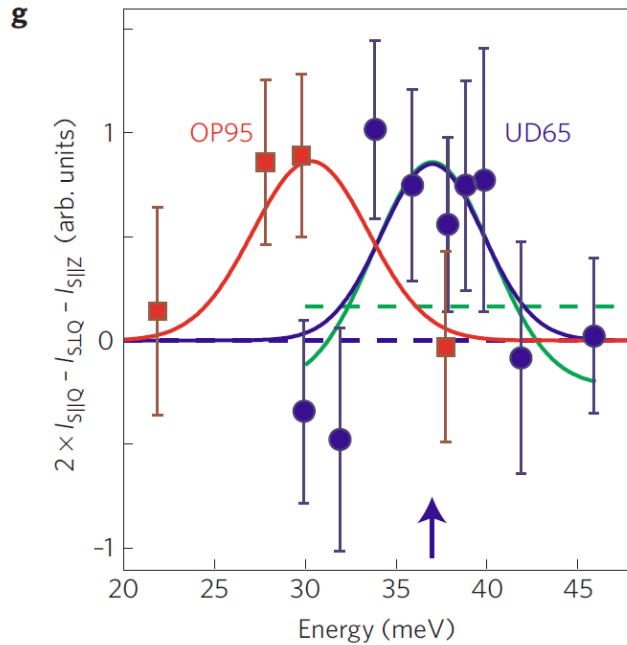
Sample: OP95



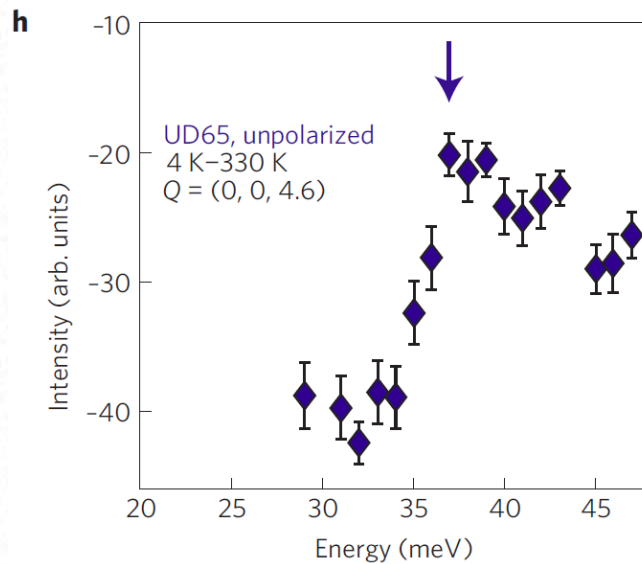
A second excitation branch



Verification of magnetic origin

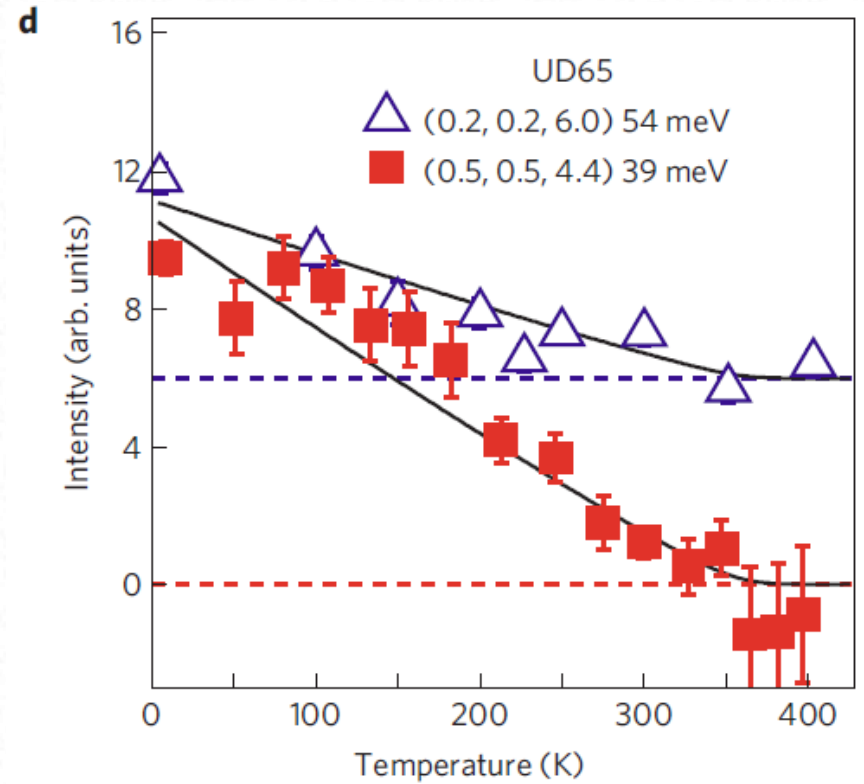
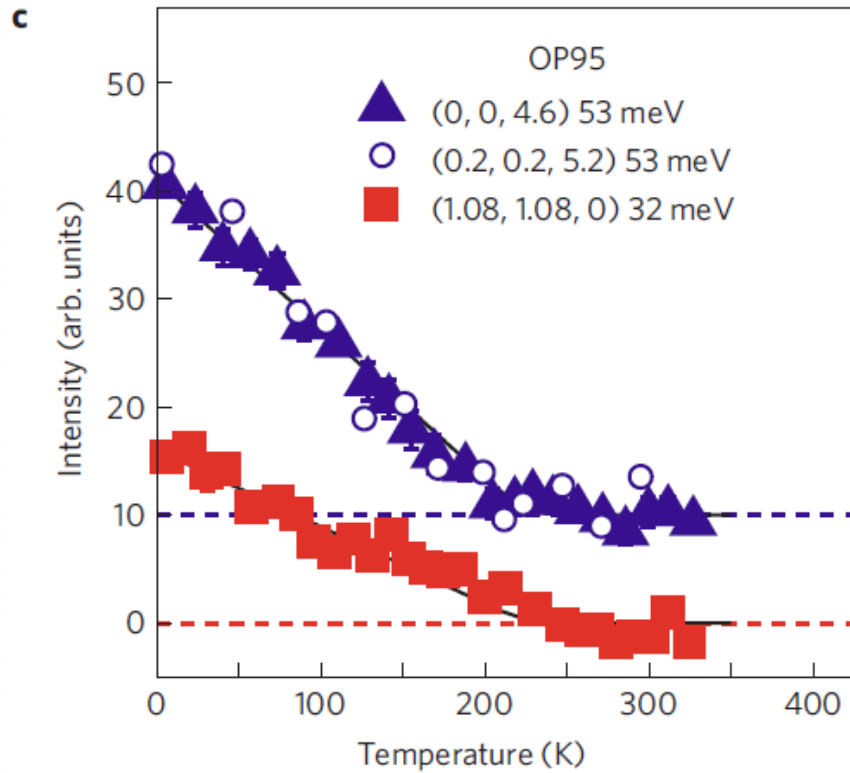


~ 125 hours
(entire beam time)



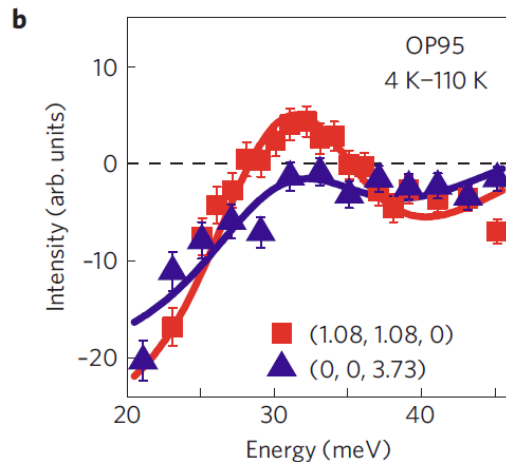
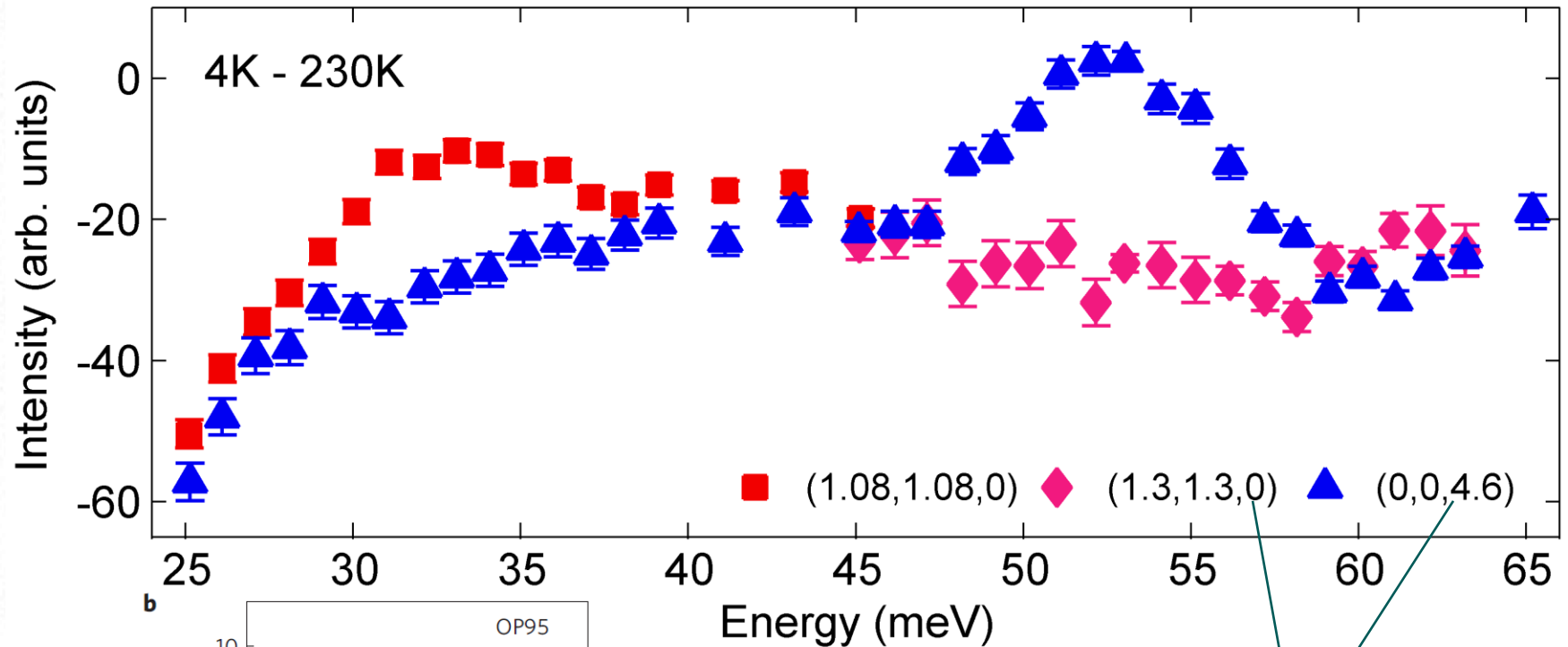
~ 6 hours

T dependence



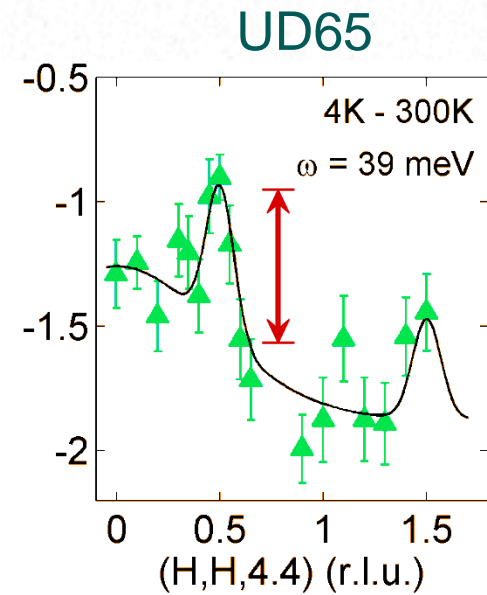
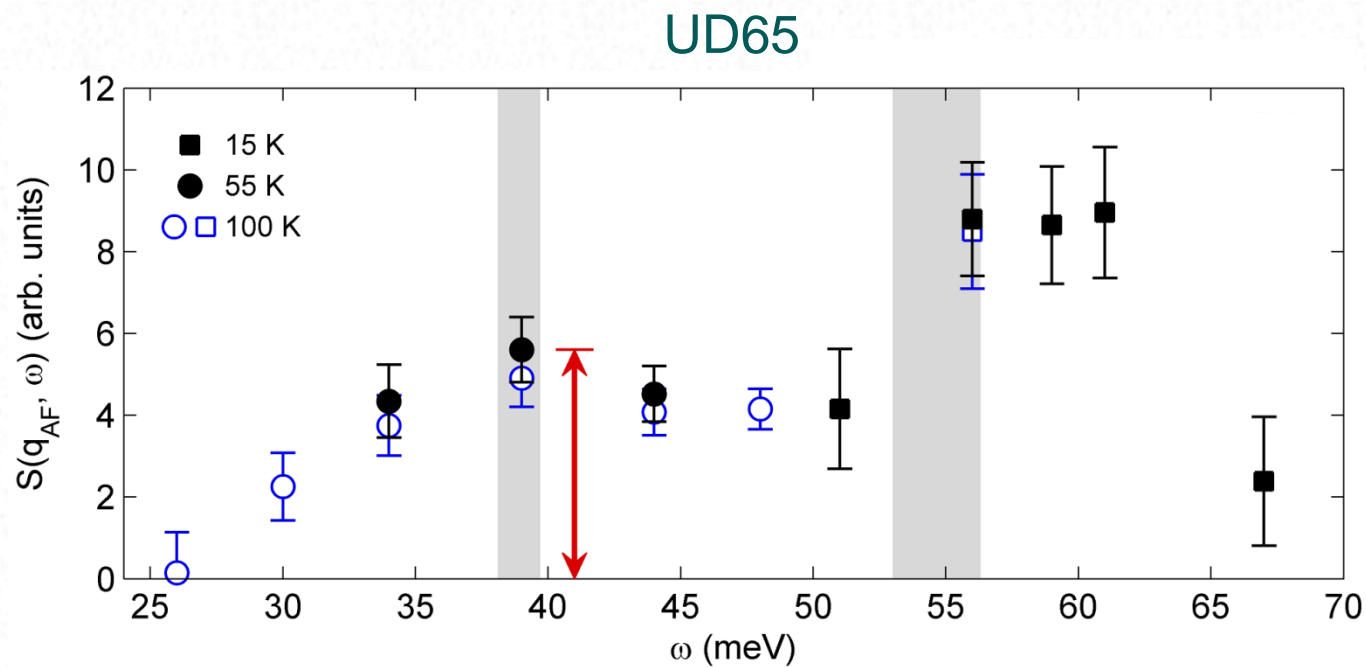
Q dependence

OP95



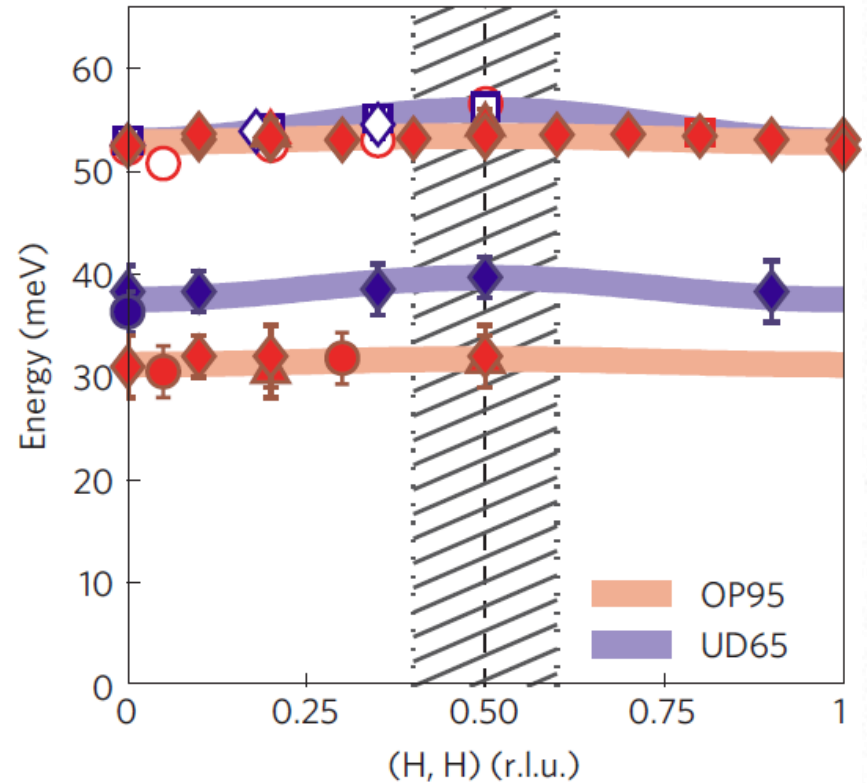
Differ by 90°
sample rotation

Connection to signal maxima at (1/2,1/2)



New excitation summary

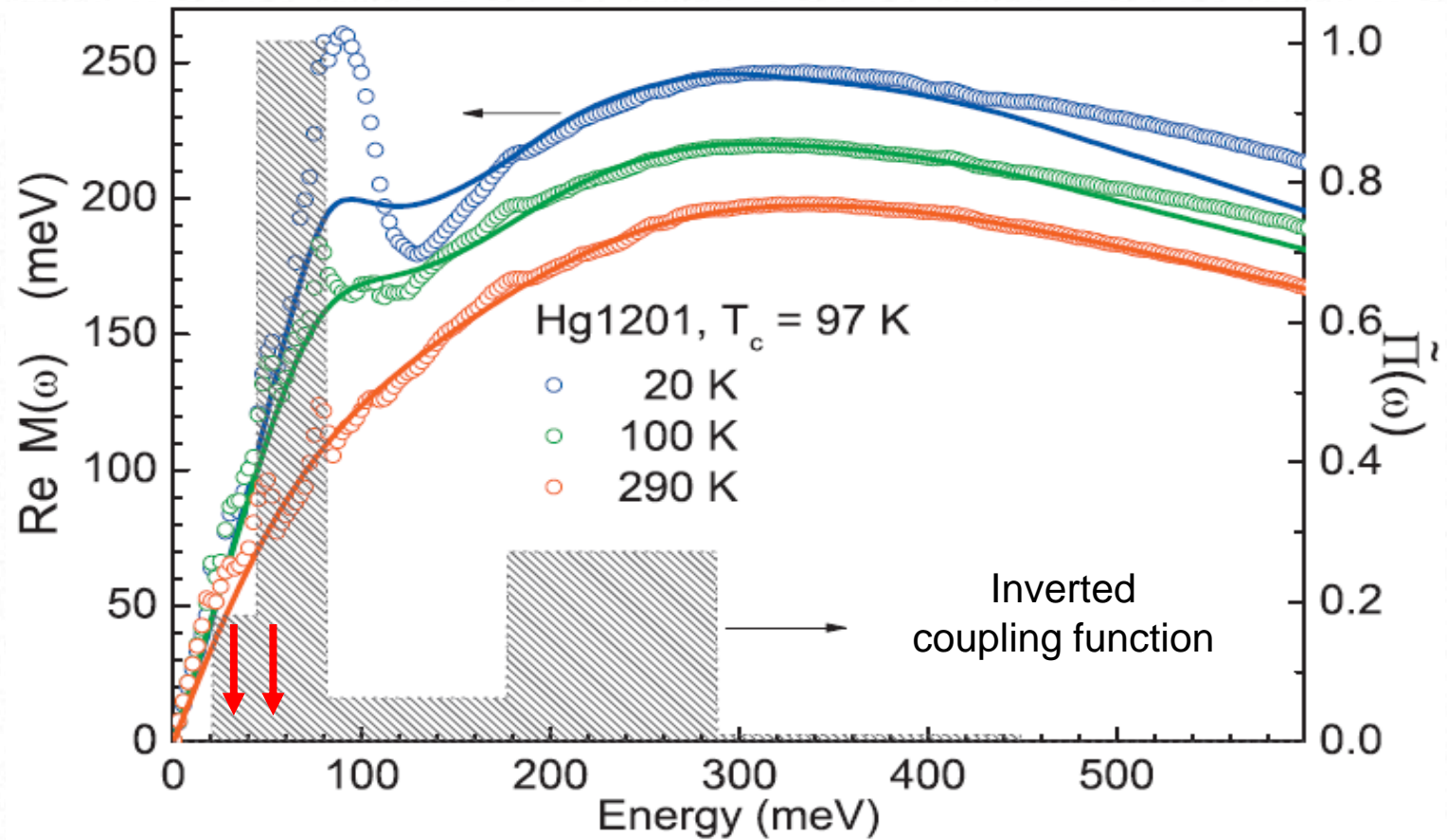
- Two almost dispersive modes
- Verified to be magnetic
- Set in below $\sim T^*$
- One energy decreases with doping
- Mysterious Q dependence of intensity
- Connection to AF fluctuations



YL *et al.*, *Nature* **468**, 283 (2010)

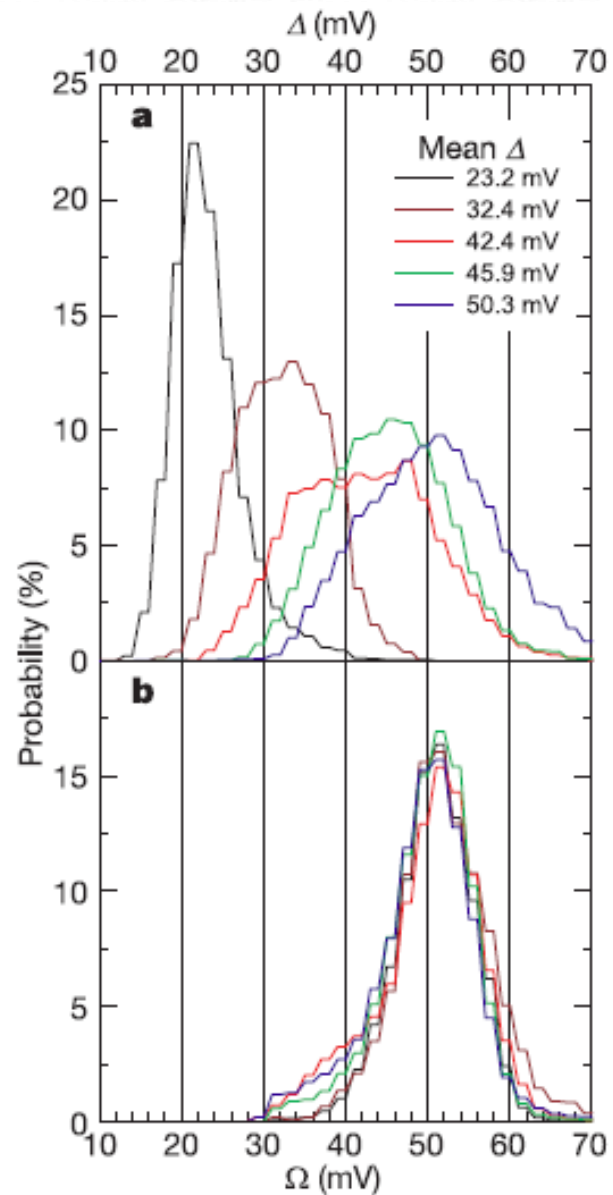
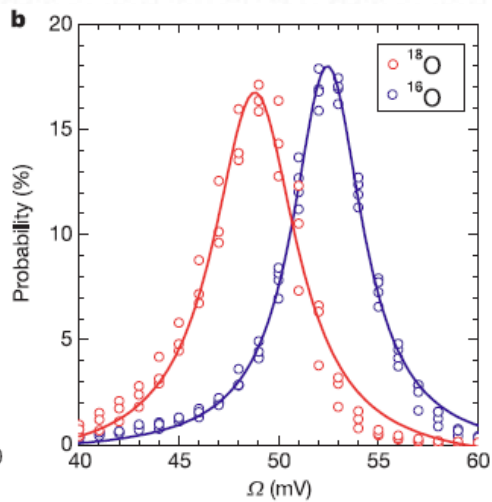
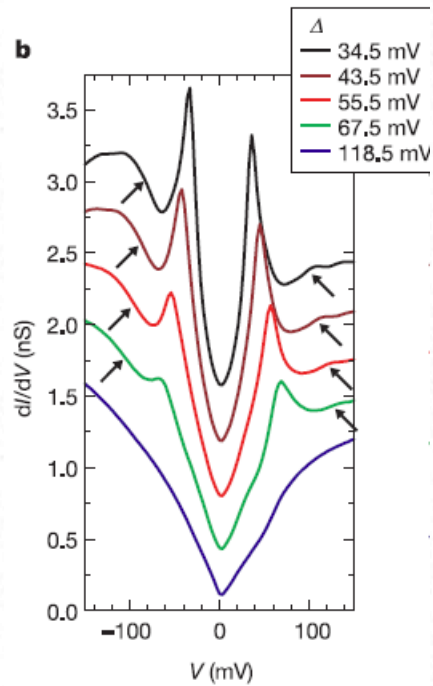
YL *et al.*, *Nat. Phys.* **8**, 404 (2012)

Electron-boson coupling



van Heumen *et al.*, *PRB* **79**, 184512 (2009)

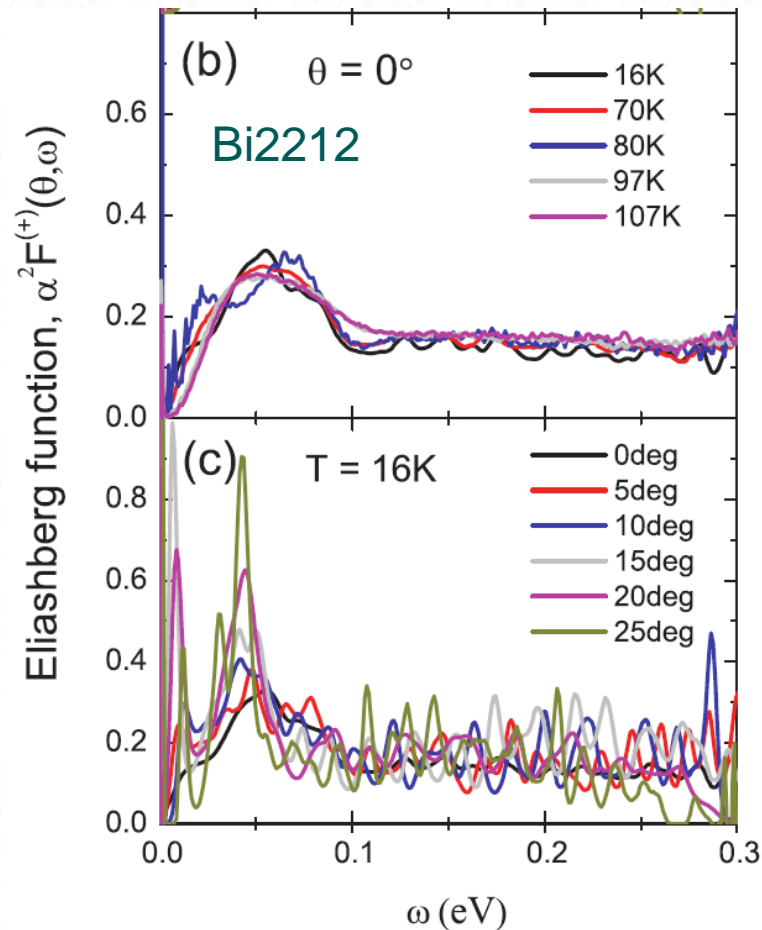
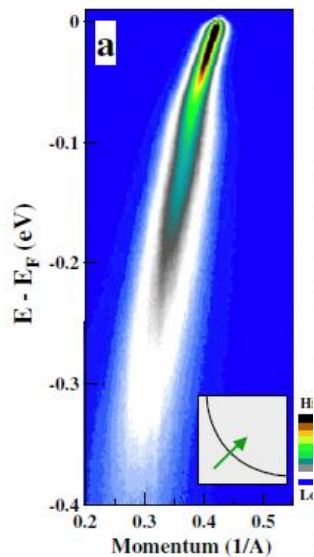
Electron-boson coupling



Bi2212

Lee *et al.*, *Nature*
442, 546 (2006)

Electron-boson coupling



Inverted from high-resolution
ARPES data taken by
Xingjiang Zhou's group

Yun *et al.*, *PRB* **84**, 104521 (2011)

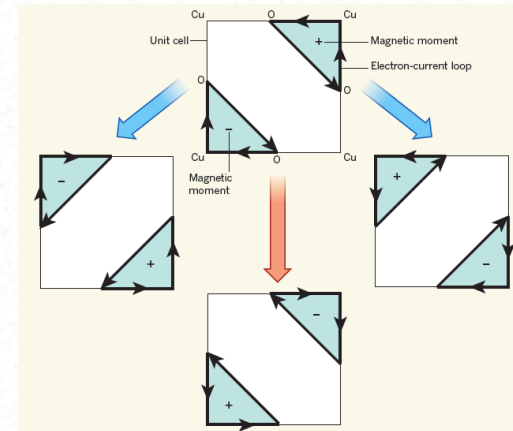
What are these excitations?

1. Excitations from “orbital currents”?

😊 Two modes, same T^* as seen by neutron diffraction

😞 Q-dependence, relation to AF fluctuations

See Varma, *Nature* **468**, 184 (2012)



2. Admixture between AF fluctuations and phonons?

😊 Multiple modes, Q-dependence, coincidence with AF fluctuation maxima

😞 Lack of systematic theory

3. Local modes?

😊 Weak dispersion, Q-dependence

😞 Coincidence with AF fluctuation maxima, large spectral weight

See, e.g., Martin *et al.*, *PRB* **70**, 224514 (2004)

Outline

□ Introduction

- HTSC and the cuprates
- Spectroscopic methods applied to the high- T_c problem

□ Model system $\text{HgBa}_2\text{CuO}_{4+\delta}$

□ Topics:

1. The neutron resonant mode
2. Pseudogap magnetism
3. Energy $2\Delta_{\text{sc}}$ and above

□ Summary

Phonon-mediated superconductivity

Lattice vibration

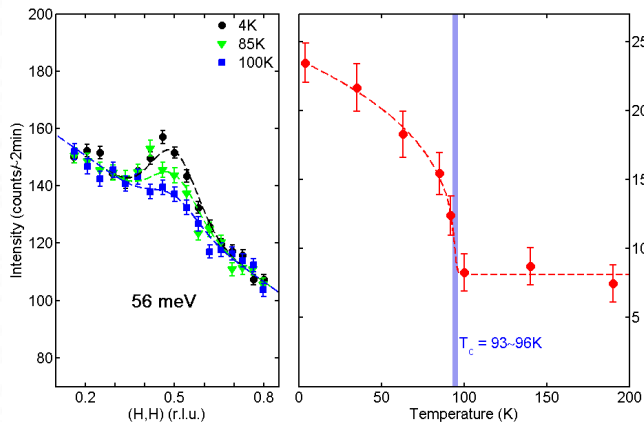


Magnetic fluctuation mediated superconductivity



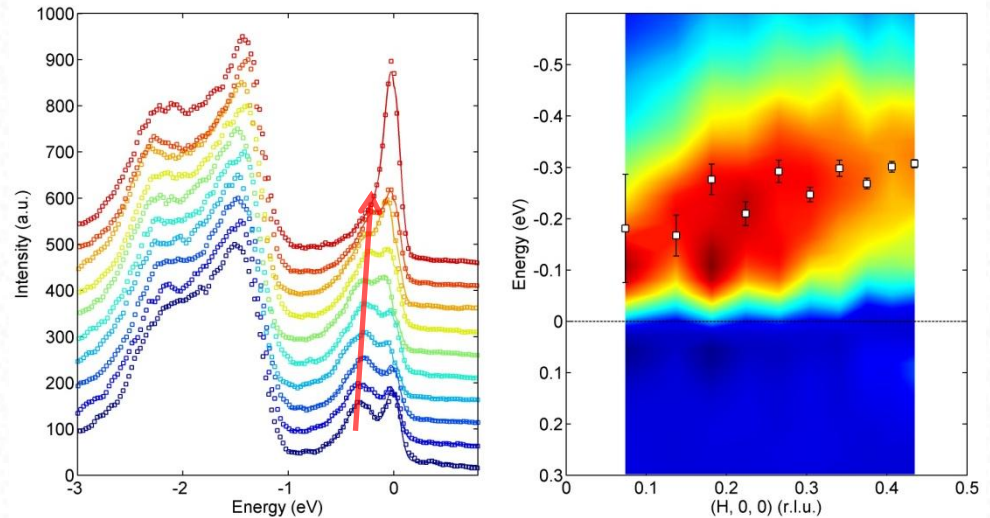
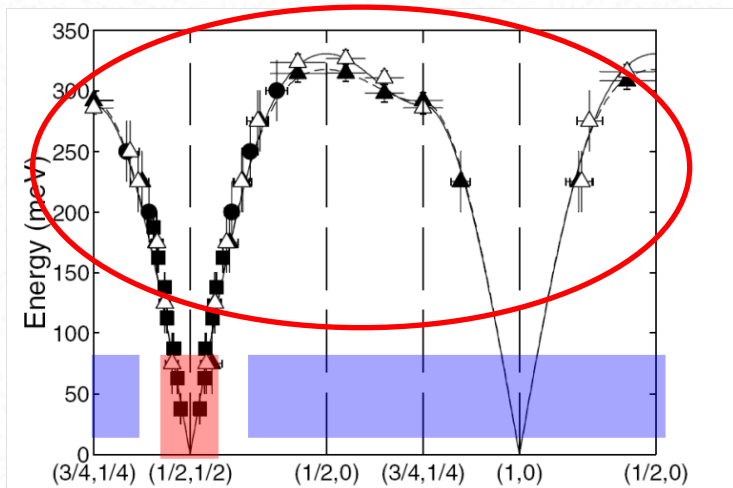
Desire to form pairs

Magnetism

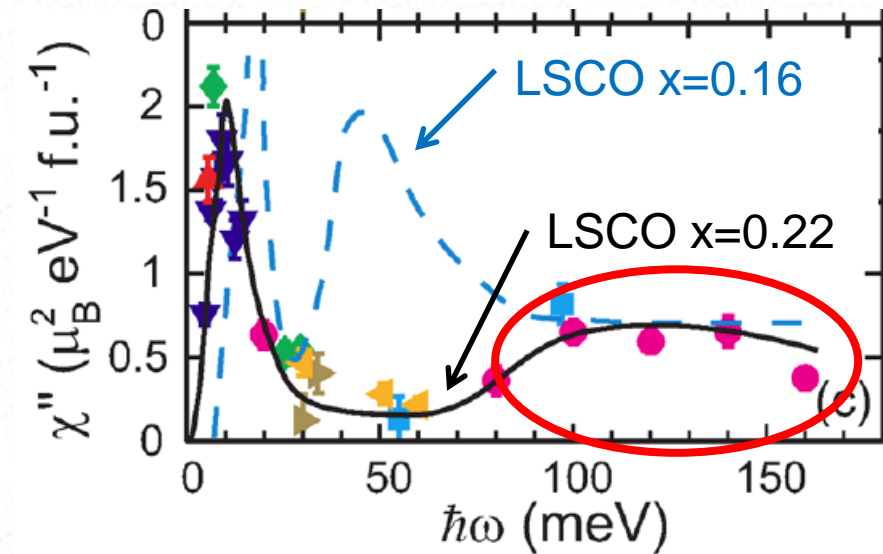


A feedback effect due to pairing can be expected on the magnetic fluctuations

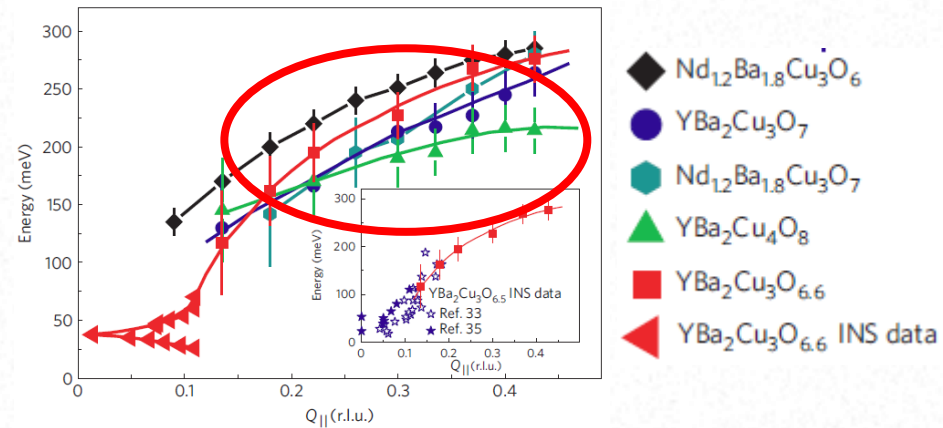
More "juice" at higher energy



Hg1201, data taken last week at SLS with Le Tacon, Tabis, Braicovich



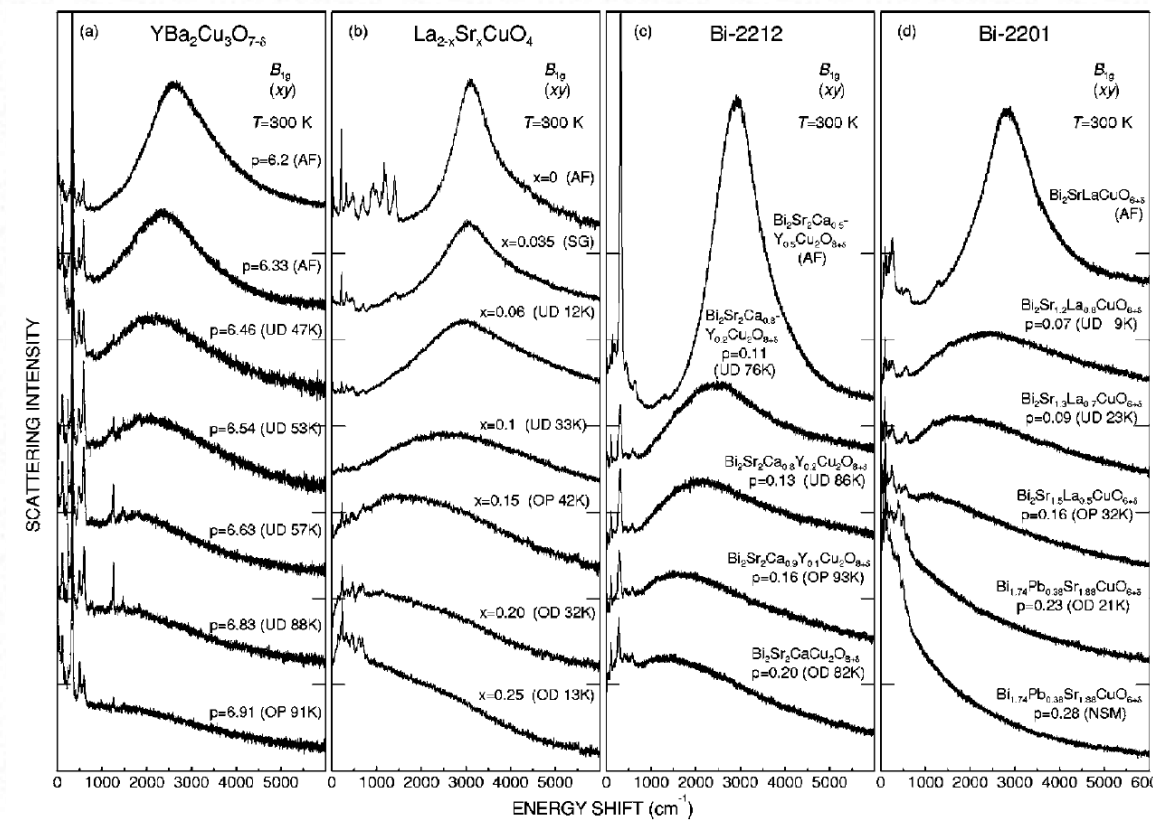
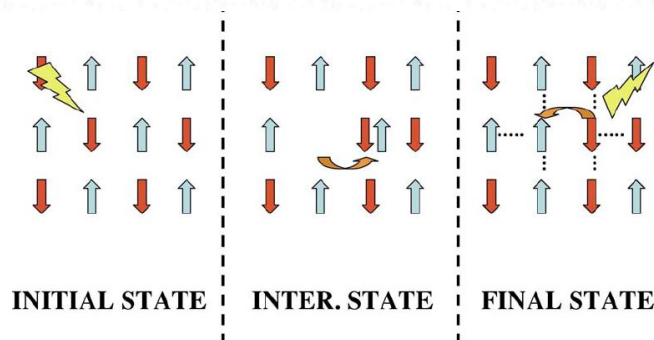
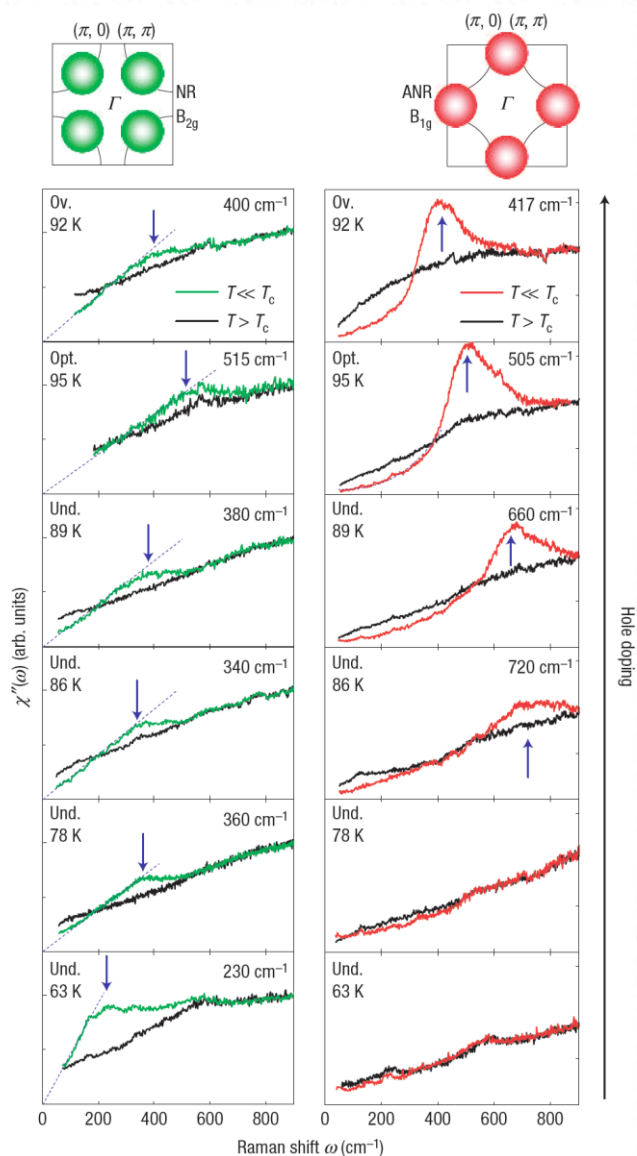
Lipscombe *et al.*, *PRL* **99**, 067002 (2004)



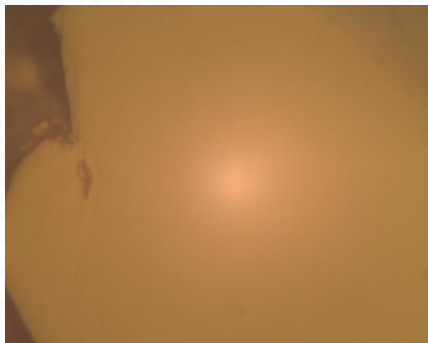
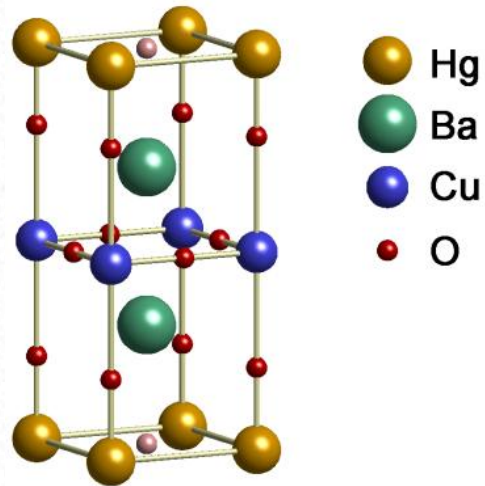
Le Tacon *et al.*, *Nat. Phys.* **7**, 725 (2011)

How about correlation between high-energy magnetic excitations and SC as we change temperature and doping?

Raman scattering

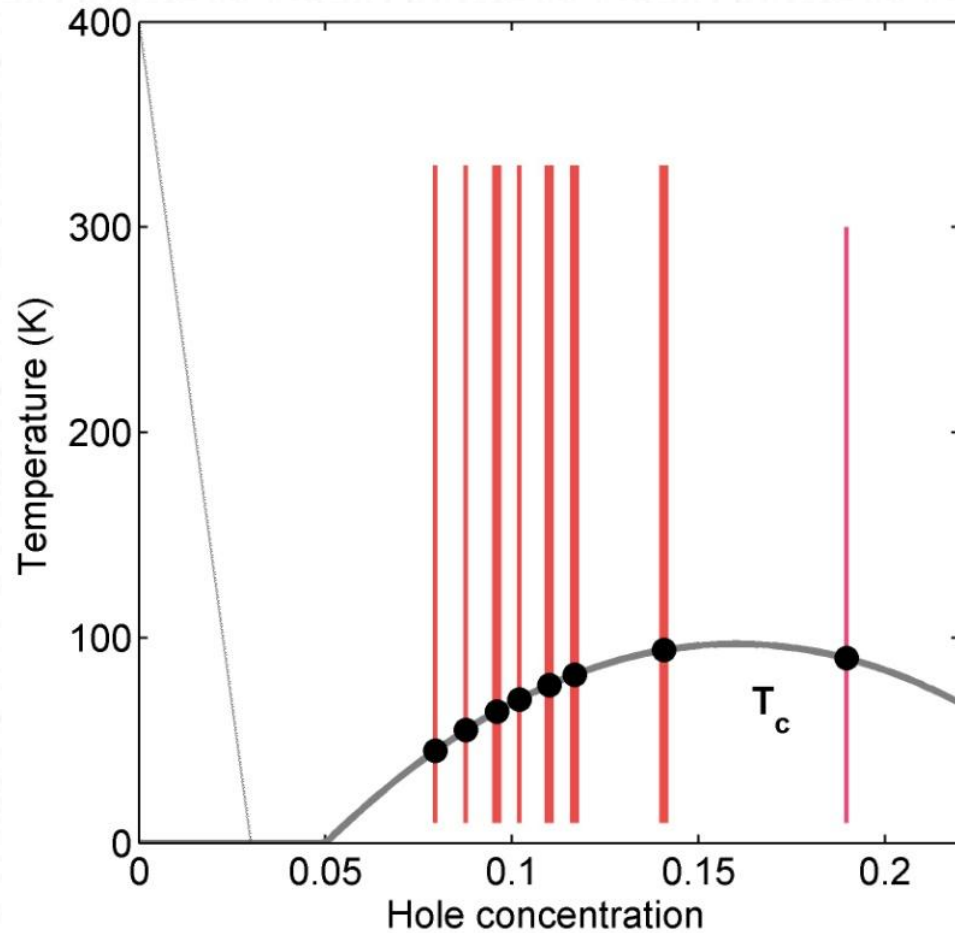


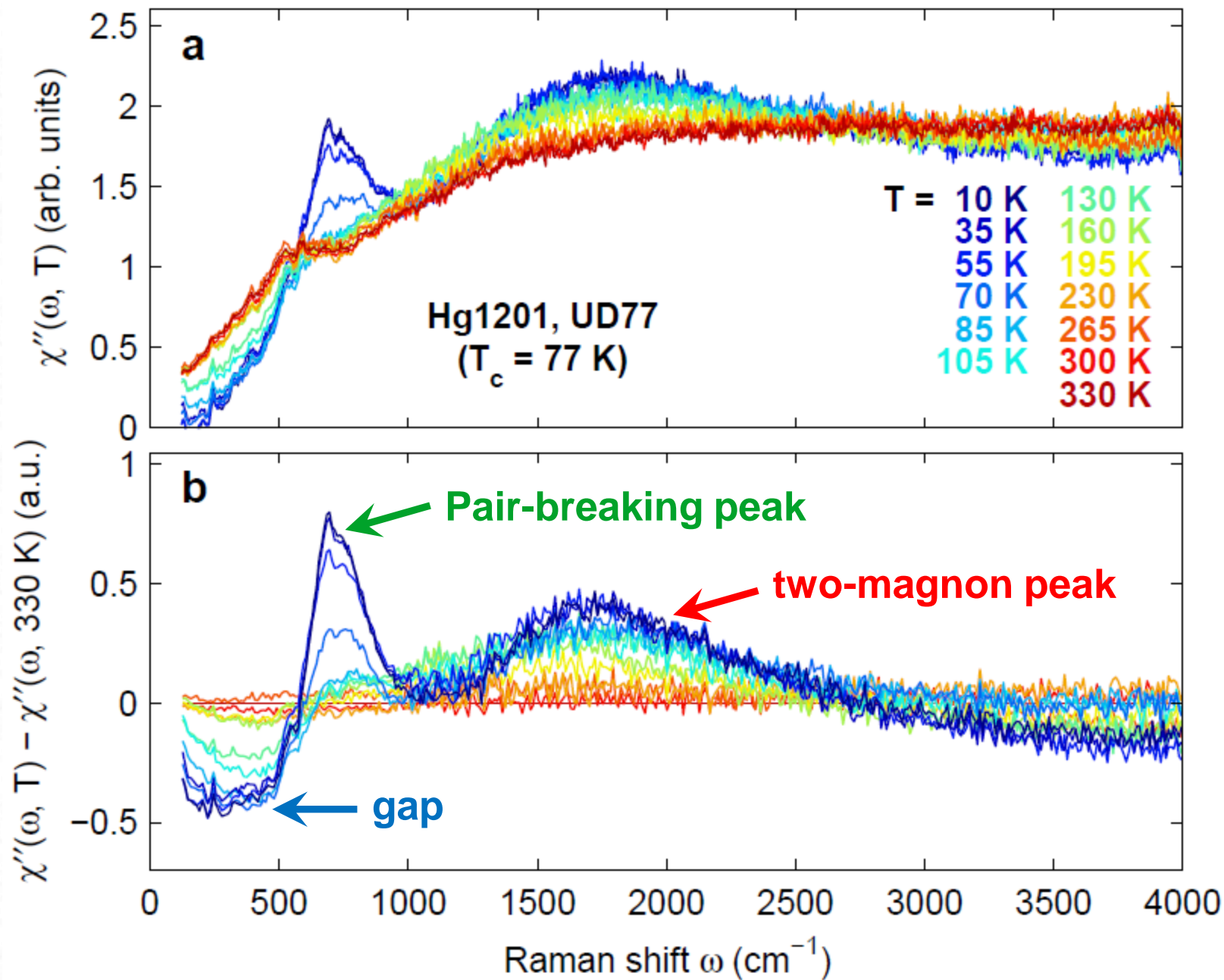
Samples

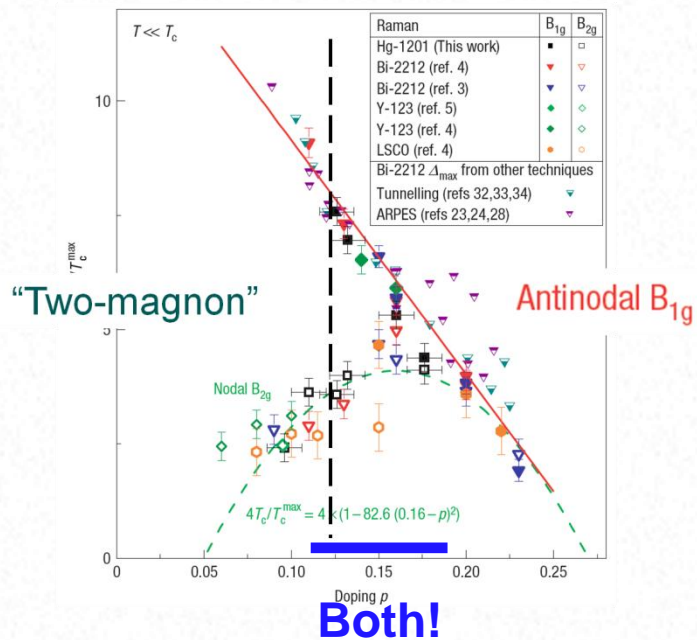
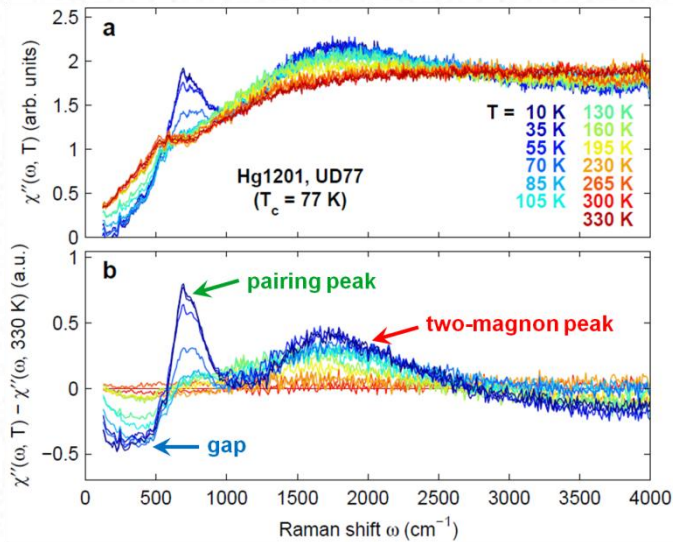


Freshly prepared sample surface (50x)

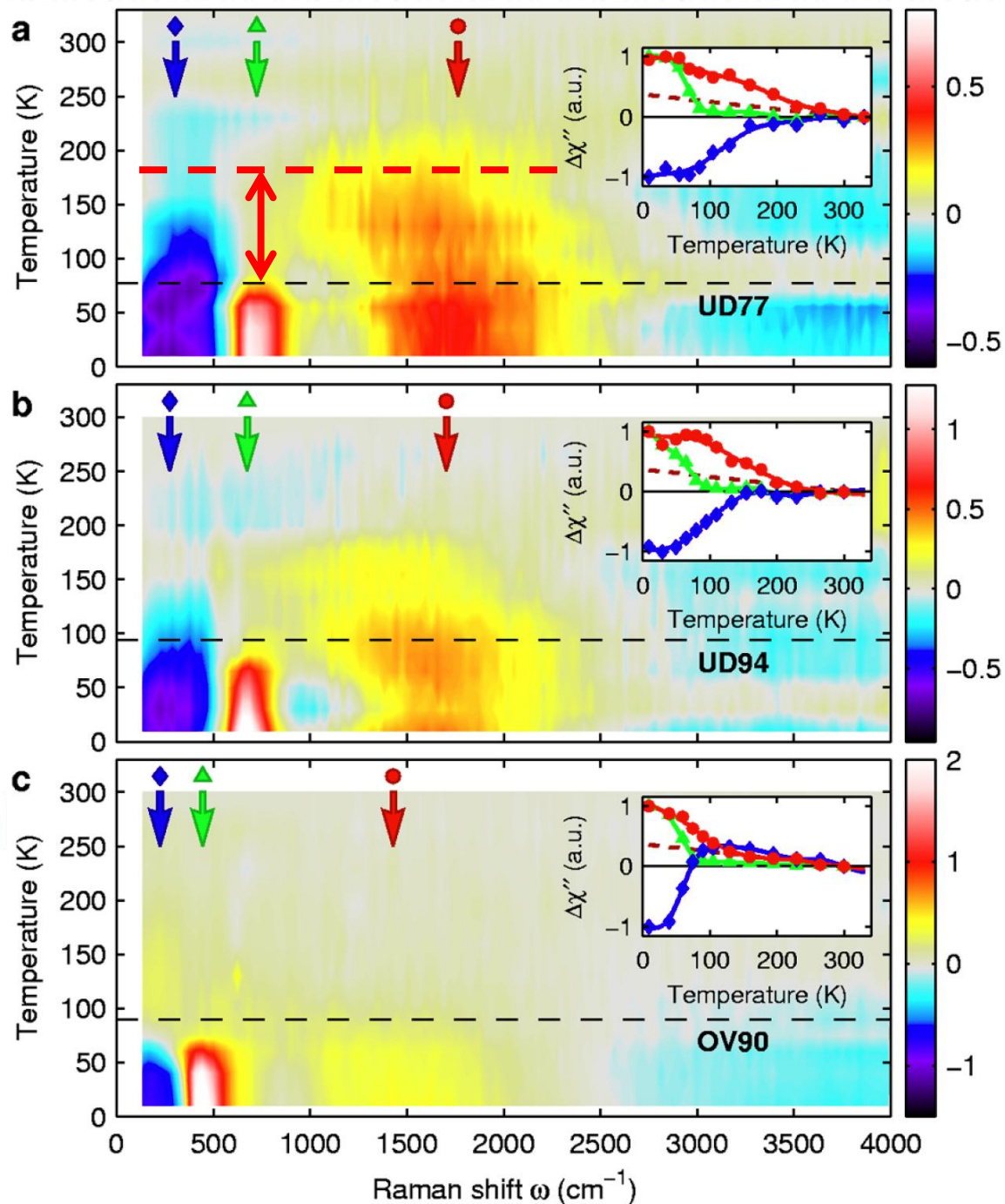
Our p- and T-range

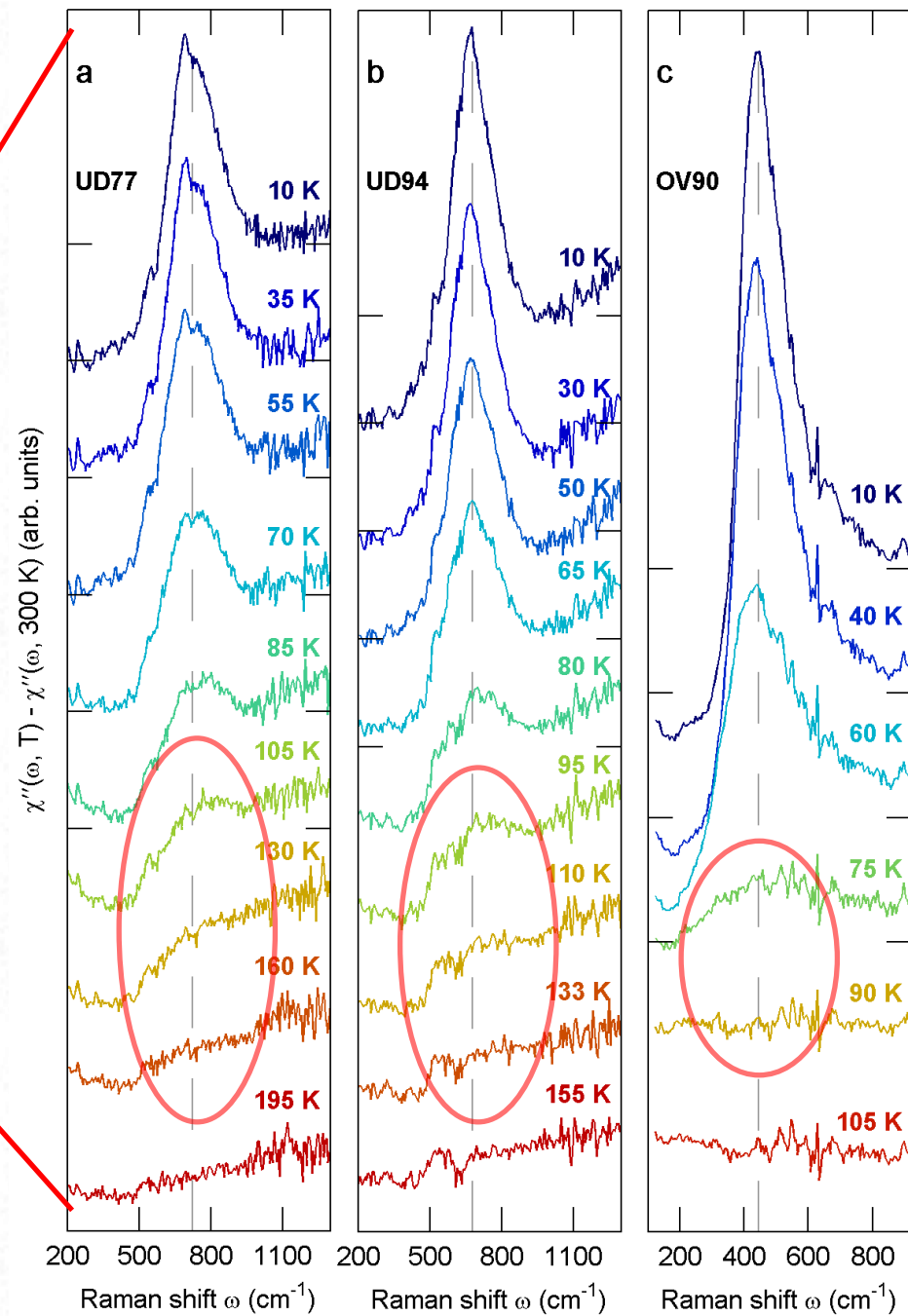
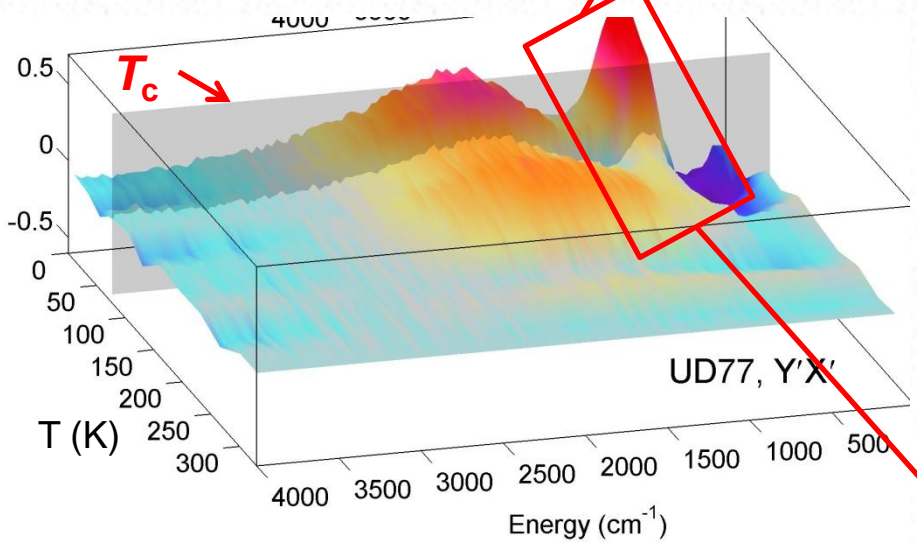
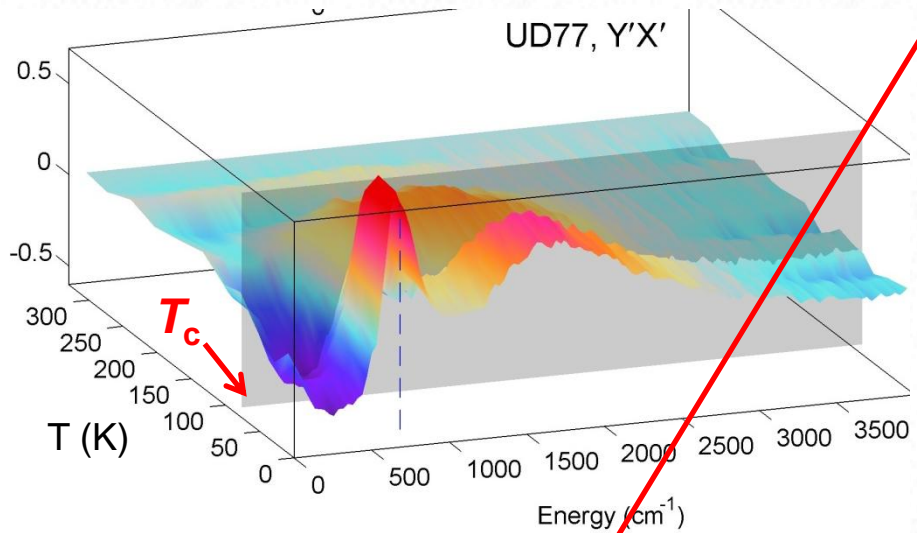






Le Tacon et al., Nat. Phys. 2, 537 (2006)





High-energy feedback effect

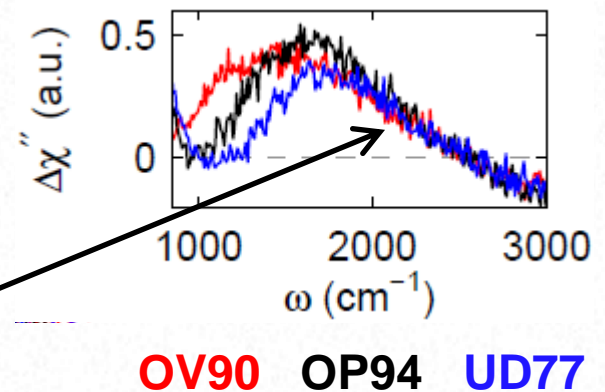
- ❑ Enhancement of two-magnon peak when the gap opens
- ❑ Pre-formed pairs observed around the same temperature



High-energy feedback effect similar to the resonant mode!

Reasons for the “two-magnon” name:

- ❑ Selection rule is correct (B_{1g})
- ❑ Energy agrees with reported values
- ❑ “Leading edge” insensitive to doping



High-energy feedback effect

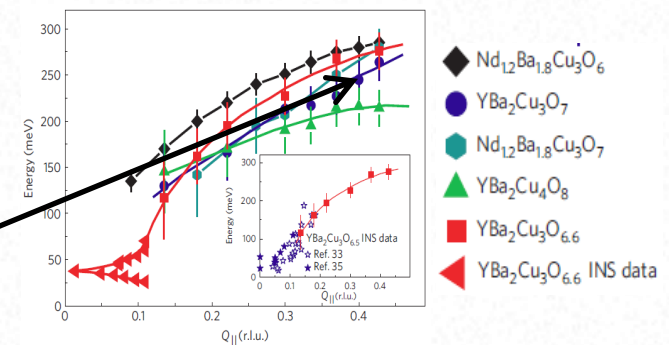
- ❑ Enhancement of two-magnon peak when the gap opens
- ❑ Pre-formed pairs observed around the same temperature



High-energy feedback effect similar to the resonant mode!

Reasons for the “two-magnon” name:

- ❑ Selection rule is correct (B_{1g})
- ❑ Energy agrees with reported values
- ❑ “Leading edge” insensitive to doping



YL *et al.*, *Phys. Rev. Lett.* **108**, 227003 (2012)

Outline

□ Introduction

- HTSC and the cuprates
- Spectroscopic methods applied to the high- T_c problem

□ Model system $\text{HgBa}_2\text{CuO}_{4+\delta}$

□ Topics:

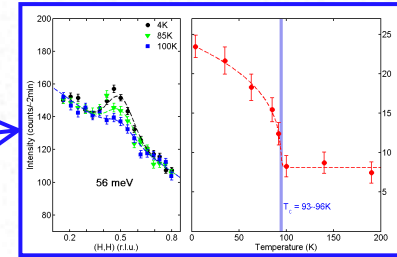
1. The neutron resonant mode
2. Pseudogap magnetism
3. Energy $2\Delta_{\text{sc}}$ and above

□ Summary

Some important questions

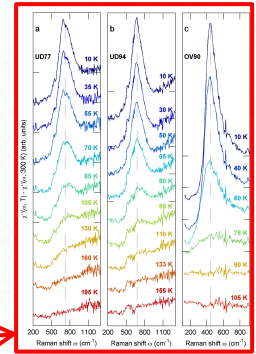
❑ Q: What's the pairing symmetry?

A: *d*-wave.



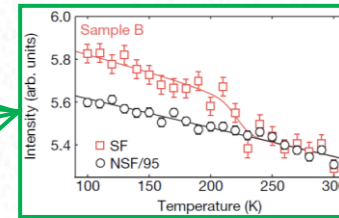
❑ Q: What causes the pseudogap above T_c ?

A: Evidence for pre-formed pairs and competing order.



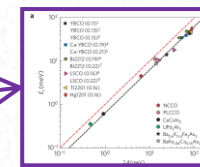
❑ Q: Is there a competing order other than AFM?

A: CDW, SDW, intra-unit-cell order are all possible.

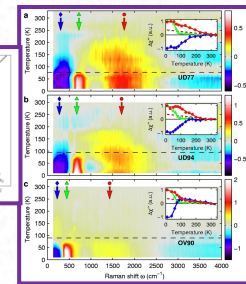
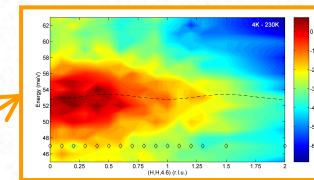


❑ Q: Which bosonic modes are important?

A: Magnetic excitations, phonons, AND

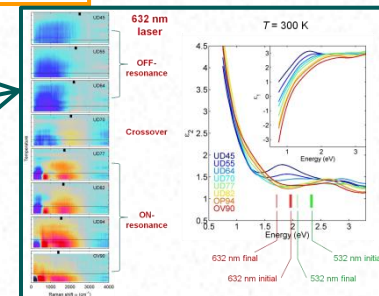


perhaps modes with mixed degrees of freedom.



❑ Q: What's the minimal microscopic model?

A: Single-band models may be insufficient.



Collaborators

Neutron Scattering

Guichuan Yu (U. Minnesota)

Martin Greven (U. Minnesota)

Paul Steffens (ILL, Grenoble)

Richard A. Mole (FRM-II, Garching)

Klaudia Hradil (FRM-II, Garching)

Nikola Egentermeyer (PSI, Villigen)

Jorge Gavilano (PSI, Villigen)

Victor Balédent (LLB, Saclay)

Yvan Sidis (LLB, Saclay)

Philippe Bourges (LLB, Saclay)

Raman Scattering

Mathieu Le Tacon (MPI, Stuttgart)

Mohammad Bakr (MPI, Stuttgart)

Bernhard Keimer (MPI, Stuttgart)

Rudi Hackl (WMI, Garching)

Optical Ellipsometry

Yulia Matiks (MPI, Stuttgart)

Alexander V. Boris (MPI, Stuttgart)

Theory

Damien Terrade (MPI, Stuttgart)

Dirk Manske (MPI, Stuttgart)

Alexander Yaresko (MPI, Stuttgart)

Samples and Characterization

Mun K. Chan (U. Minnesota)

Lina Ji (U. Minnesota)

Neven Barišić (U. Minnesota)

Xudong Zhao (U. Minnesota, Jilin Univ.)

Toshinao Loew (MPI, Stuttgart)

Chengtian Lin (MPI, Stuttgart)

Thank you!